

# Young stars in the Galactic bulge?

A mystery explored using modern isochrones,  
careful statistics, and model uncertainties

Seminar  
Uppsala Universitet  
13 October, 2022

 @MeridithJoyceGR  
[www.meridithjoyce.com](http://www.meridithjoyce.com)

[github.com/mjoyceGR](https://github.com/mjoyceGR)

\*is on the faculty job market!  
[meridith.joyce@csfk.org](mailto:meridith.joyce@csfk.org)

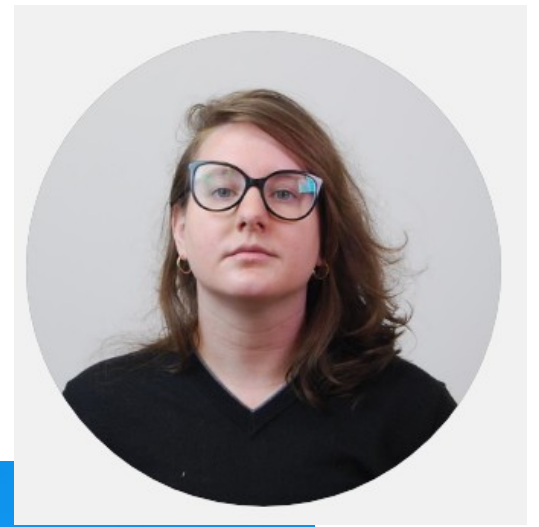
Dr Meridith Joyce\*

Marie Curie Widening Fellow: MATISSE  
CSFK Konkoly Observatory, Budapest

**MESA** Developers

# About Me:

I have enjoyed work and life all over the world, and now I've joined you in Europe!



# MATISSE: Measuring Ages Through Isochrones, Seismology, and Stellar Evolution

Timeline of Project	Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8
<b>WP1—Asteroseismic dating</b>								
Stage 1: Understanding MESA systematics		M1	WP1.1					
Stage 2: Identification, characterization of seismic targets								
Stage 3: MLT calibrations to seismic binaries, etc.						WP1.2		
Stage 4: Implementation of empirical convective formalism								WP1.3
<b>WP2—Isochrone dating</b>								
Stage 1: Building the MISTiC database	WP2.1							
Stage 2: Applying MISTiC to <i>Gaia</i> GCs			M2	WP2.2				
Stage 3: Applying MISTiC to special stars				WP2.3				
<b>WP3: Characterizing high-mass variables</b>								
Secondment: KU Leuven					KUL			
Stage 1: Enrichment timescales from TP-AGB stars							WP3.1	
Stage 2: Evolutionary dating with chemical yields						M3		
<b>Conferences, workshops, press releases</b>	R			Mesa, C	R		PR	Mesa, PR, C

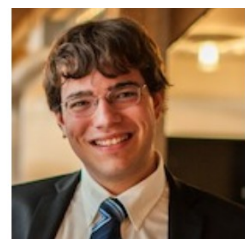
Key: WP work package; WP X.Y science deliverable Y for WP X; M milestone; Q quarter of the annual (3 months)

# The MESA developers team

(Modules for Experiments in Stellar Astrophysics)



Josiah Schwab



Adam Jermyn



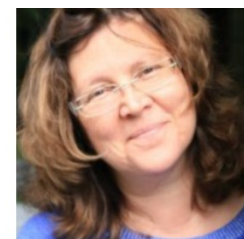
Meredith Joyce



Evan Bauer



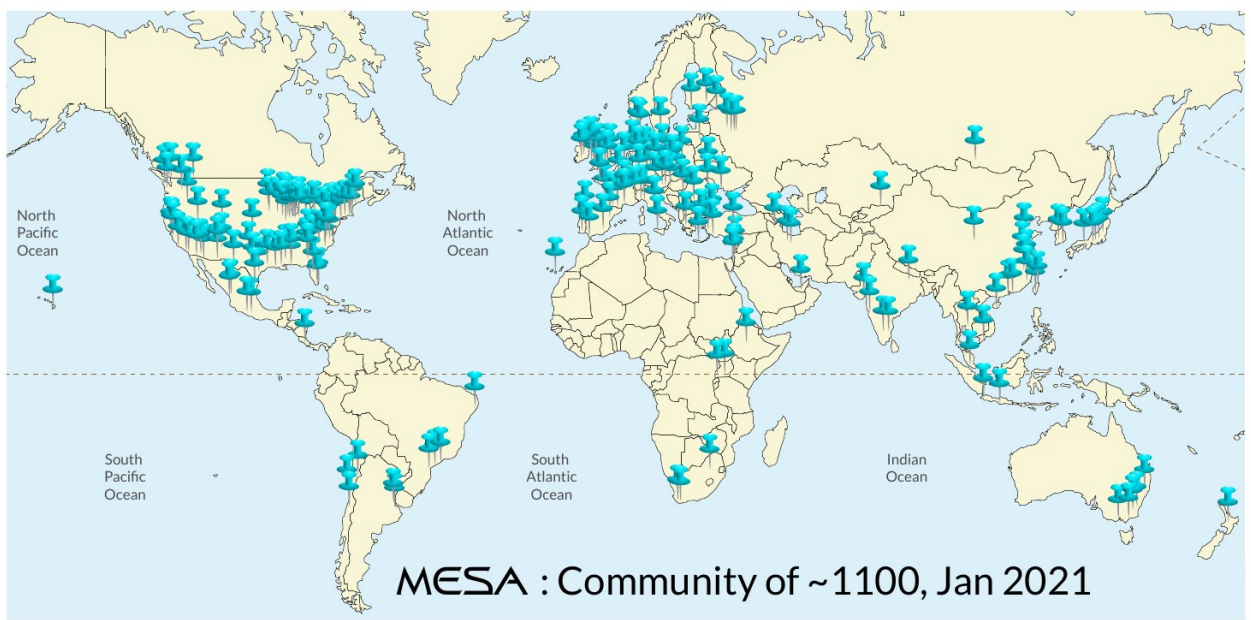
Earl Bellinger



Anne Thoul



Radek Smolec



Bill Wolf



Rob Farmer



Pablo Marchant



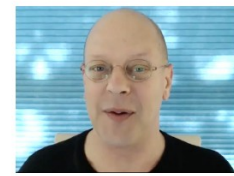
Warrick Ball



Aaron Dotter



Rich Townsend



Frank Timmes



Bill Paxton



Lars Bildsten



Matteo Cantiello

# The project I will discuss today was done in collaboration with



Dr Christian Johnson (STScI)



Dr Tommaso Marchetti (ESO)

and

Prof R Michael Rich (UCLA)

Dr Iulia Simion (Shanghai Key Lab for Astrophysics)

Dr John Bourke (MSP Berkeley)

In 2017, a catalog of ages for 91 micro-lensed subdwarfs was put forth by T. Bensby and collaborators

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**Chemical evolution of the Galactic bulge as traced  
by microlensed dwarf and subgiant stars**

**VI. Age and abundance structure of the stellar populations  
in the central sub-kpc of the Milky Way<sup>★,★★</sup>**

T. Bensby<sup>1</sup>, S. Feltzing<sup>1</sup>, A. Gould<sup>2,3,4</sup>, J. C. Yee<sup>5</sup>, J. A. Johnson<sup>4</sup>, M. Asplund<sup>6</sup>, J. Meléndez<sup>7</sup>, S. Lucatello<sup>8</sup>,  
L. M. Howes<sup>1</sup>, A. McWilliam<sup>9</sup>, A. Udalski<sup>10,★★★</sup>, M. K. Szymański<sup>10,★★★</sup>, I. Soszyński<sup>10,★★★</sup>, R. Poleski<sup>10,4,★★★</sup>,  
Ł. Wyrzykowski<sup>10,★★★</sup>, K. Ulaczyk<sup>10,11,★★★</sup>, S. Kozłowski<sup>10,★★★</sup>, P. Pietrukowicz<sup>10,★★★</sup>, J. Skowron<sup>10,★★★</sup>,  
P. Mróz<sup>10,★★★</sup>, M. Pawlak<sup>10,★★★</sup>, F. Abe<sup>12,★★★★</sup>, Y. Asakura<sup>12,★★★★</sup>, A. Bhattacharya<sup>13,★★★★</sup>, I. A. Bond<sup>14,★★★★</sup>,  
D. P. Bennett<sup>15,★★★★</sup>, Y. Hirao<sup>16,★★★★</sup>, M. Nagakane<sup>16,★★★★</sup>, N. Koshimoto<sup>16,★★★★</sup>,  
T. Sumi<sup>16,★★★★</sup>, D. Suzuki<sup>15,★★★★</sup>, and P. J. Tristram<sup>17,★★★★</sup>

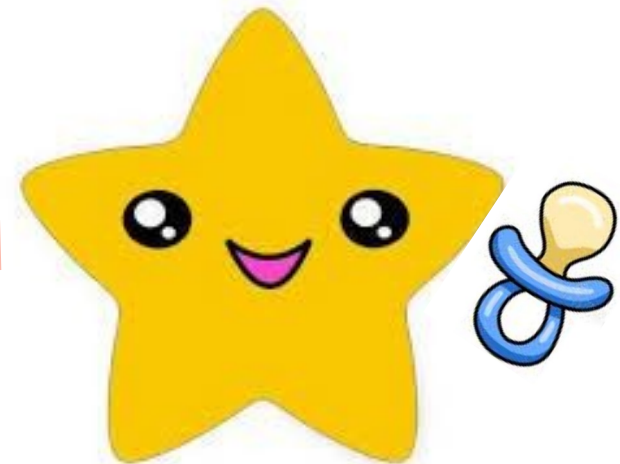
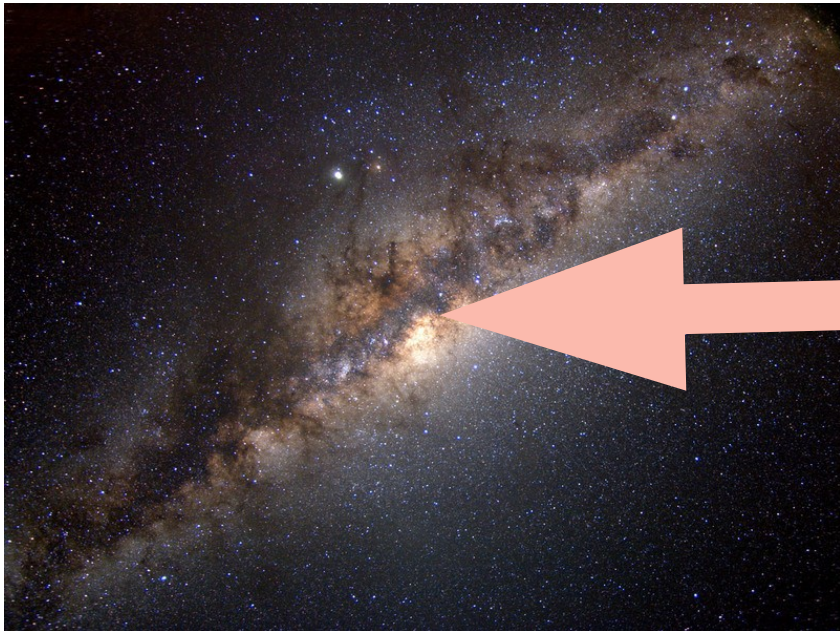
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Basically, prolonged star formation.

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- we must then answer: how did young stars get there?
- an overabundance of young stars in this region thus calls into question the formation history of the Galaxy and galaxy evolution mechanisms more generally

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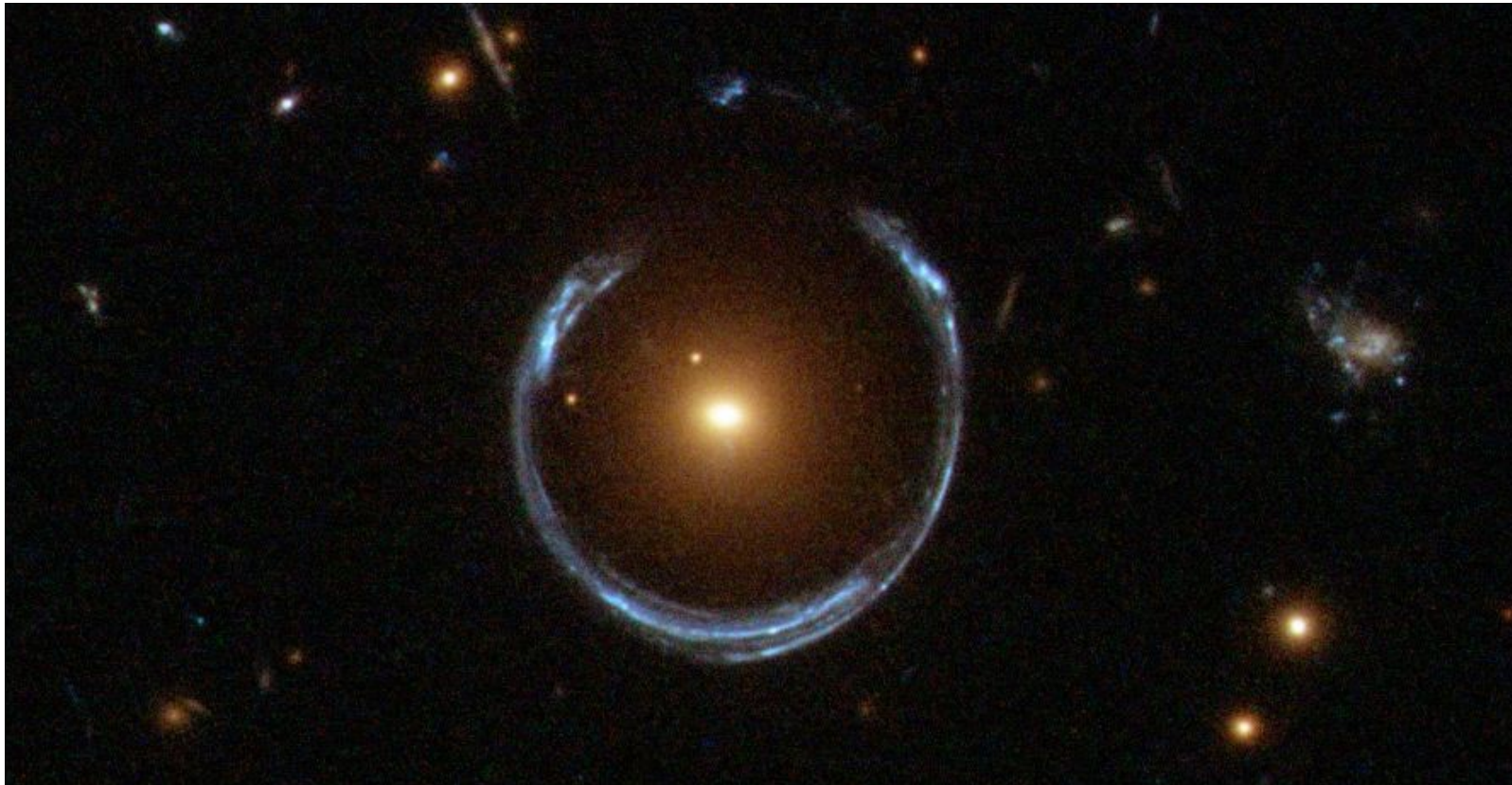
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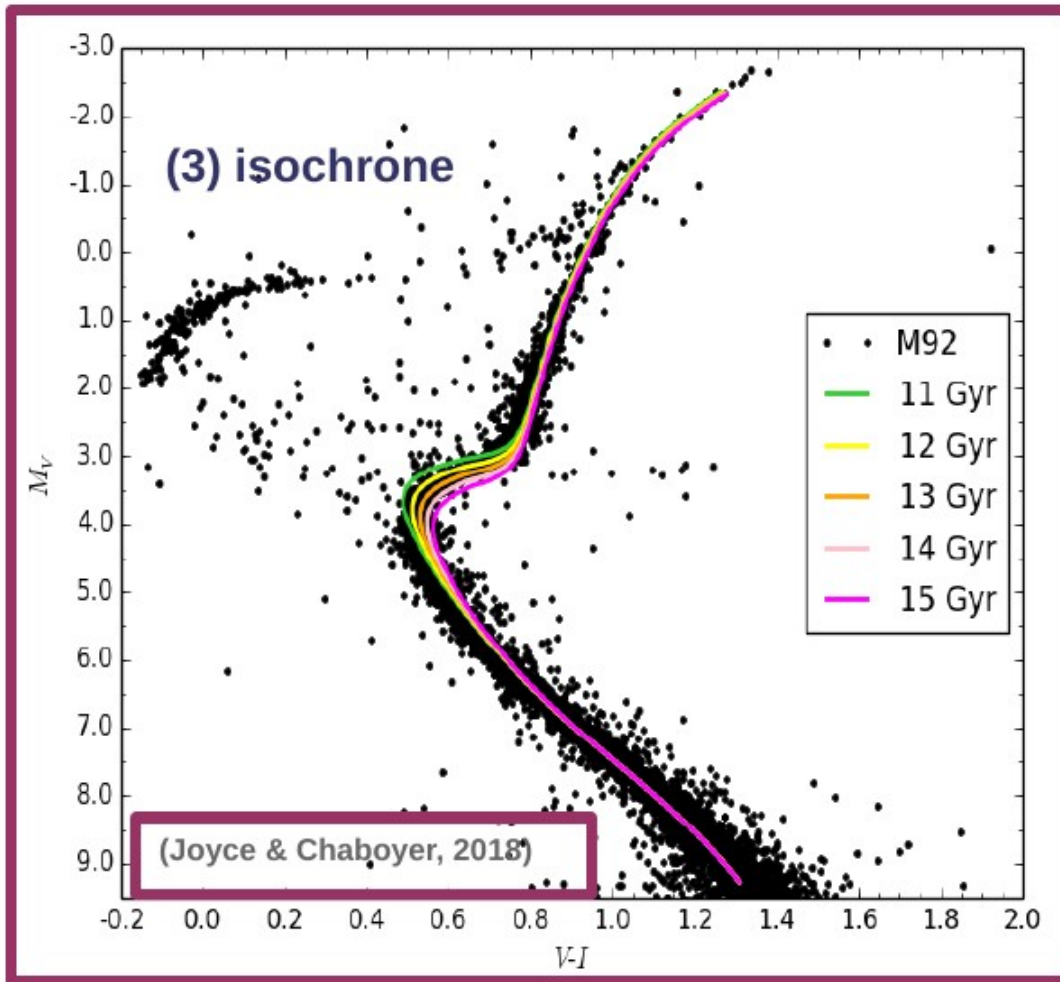
...but in order for something to be true, it must be true regardless of inference method

# A rare and powerful dataset

Microensing permits the direct inference of physical, spectroscopic coordinates ( $T_{\text{eff}}$ ,  $\log g$ ) of faint, cool stars due to the 10-1000x brightness magnification they experience during these events



# Isochrone review



Derive fundamental parameters for both individual stars and stellar populations

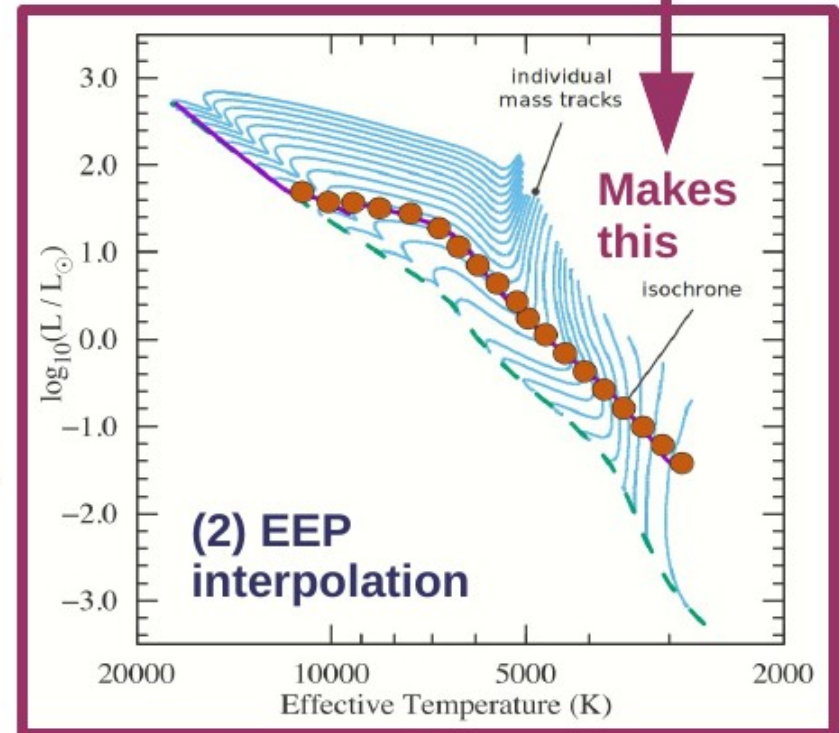
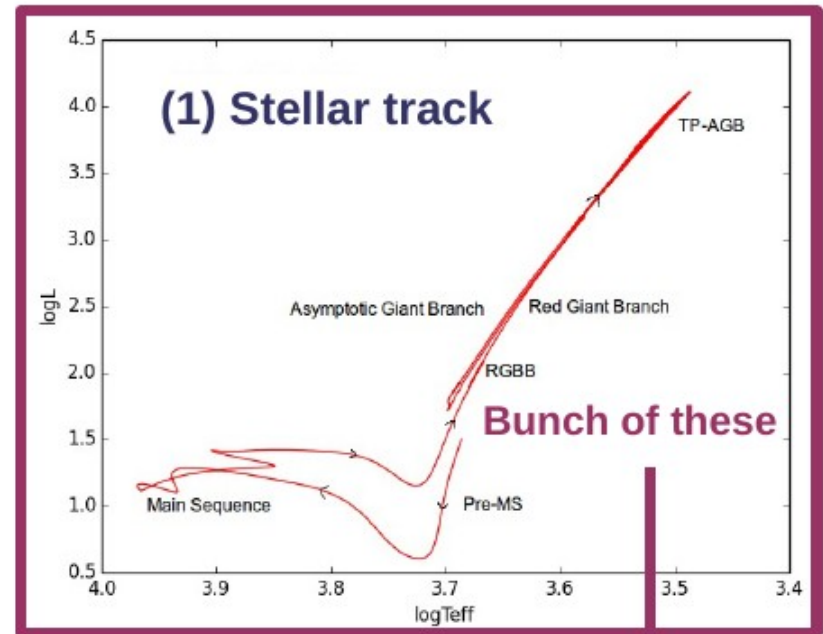
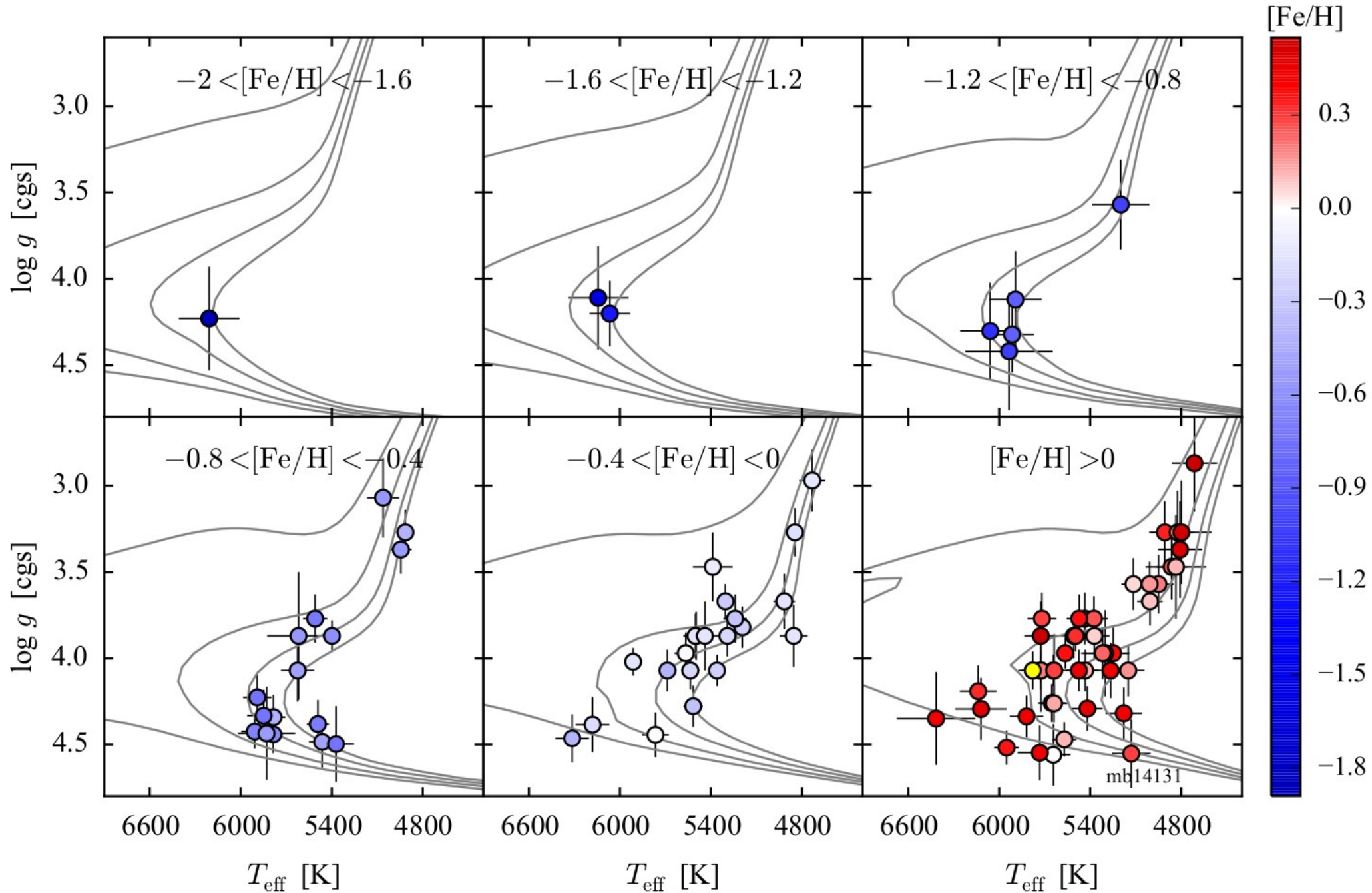
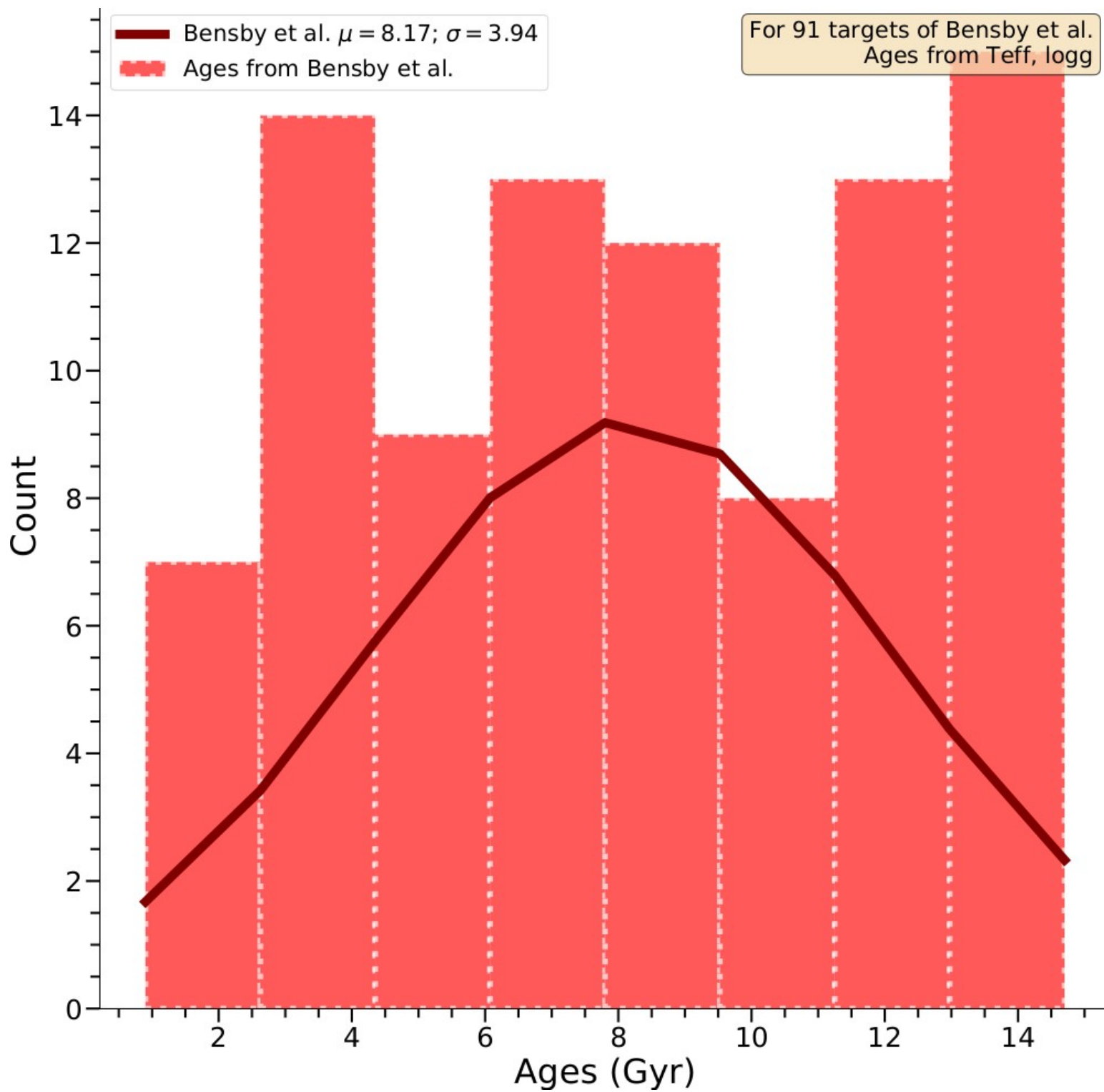




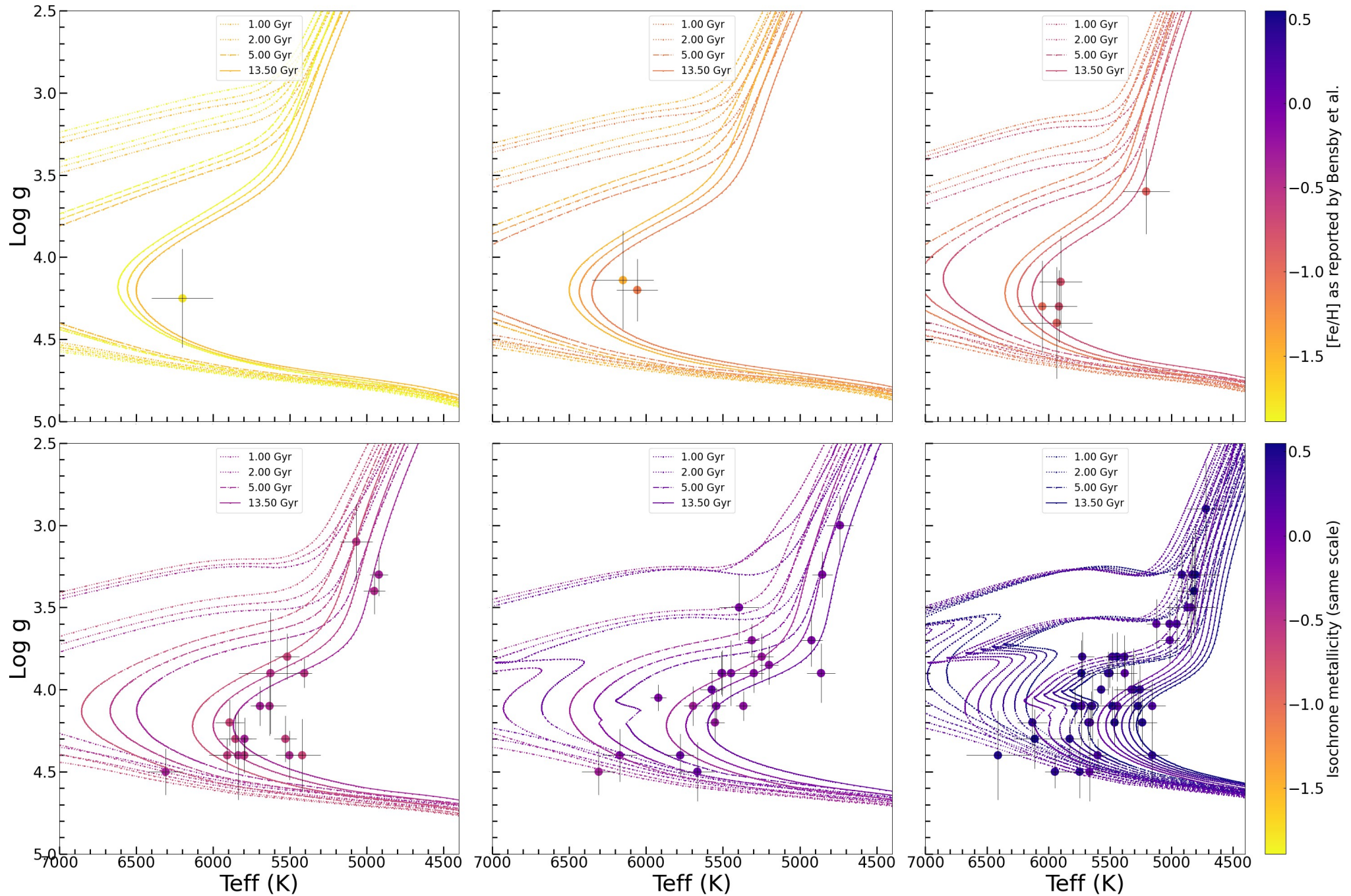
Fig 6, Bensby et al. 2017: 91 stars on Yale isochrones



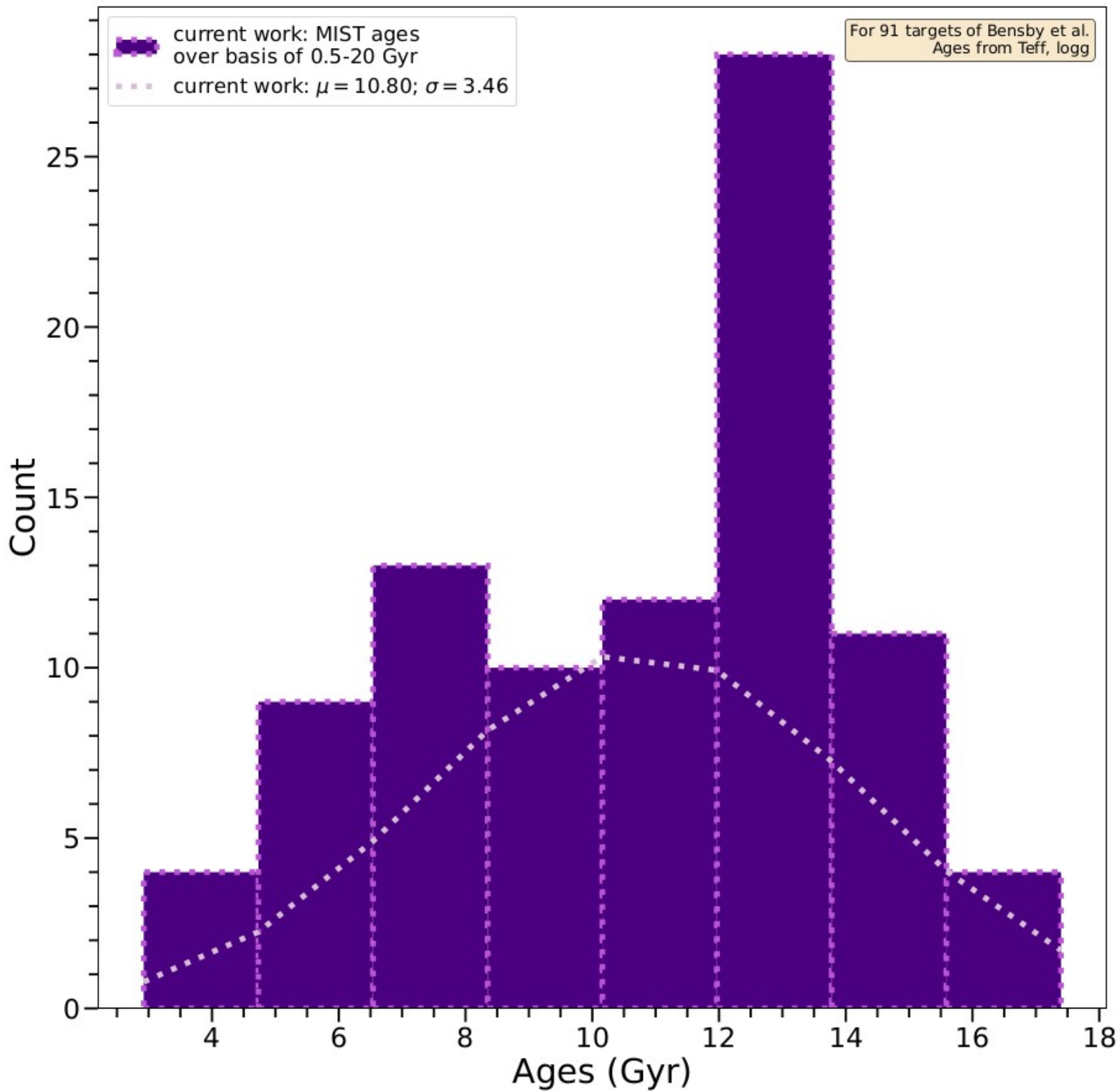
# Resulting age distribution (Bensby et al.; Yale)



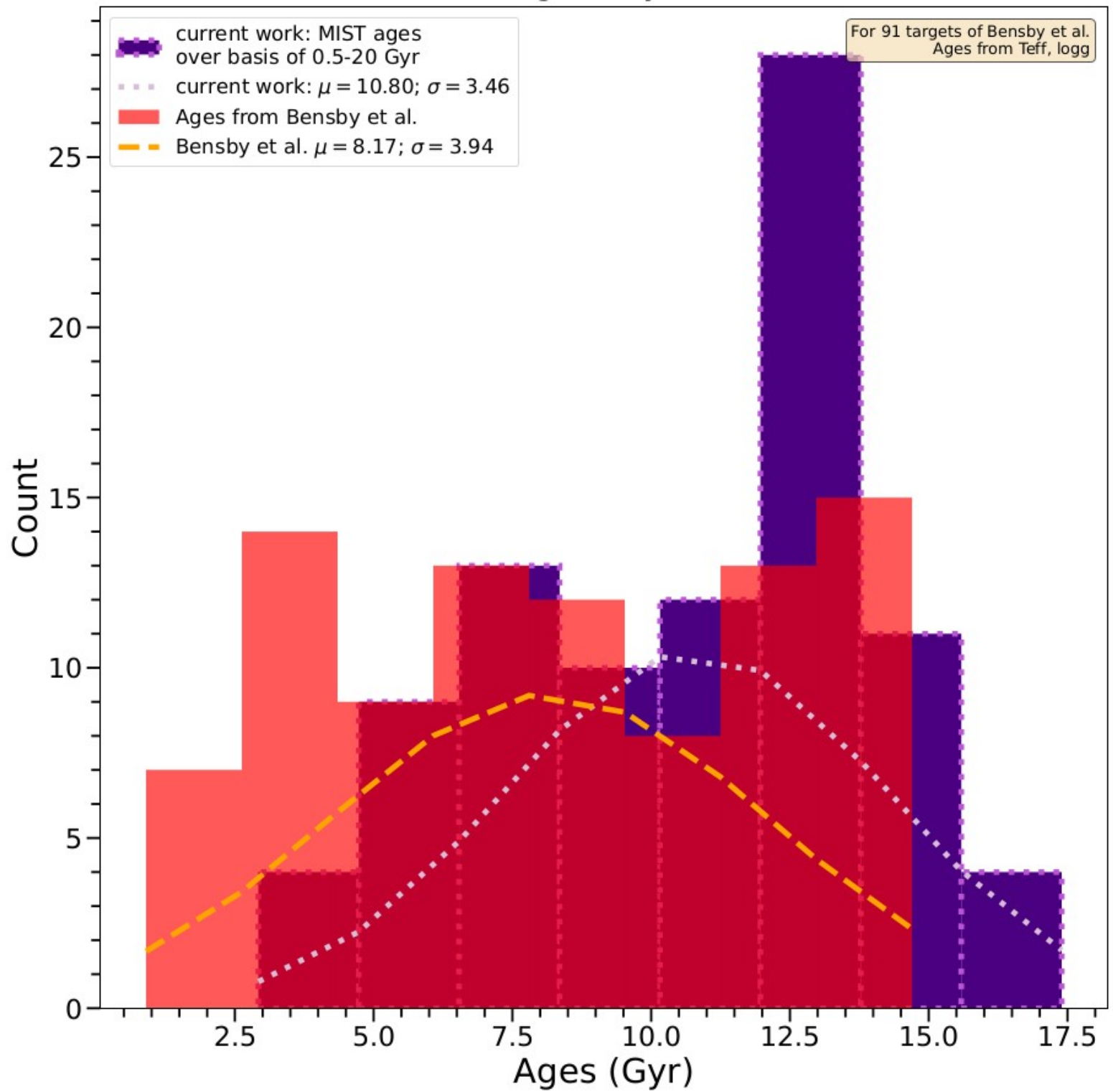
# Reproduction with MIST isochrones

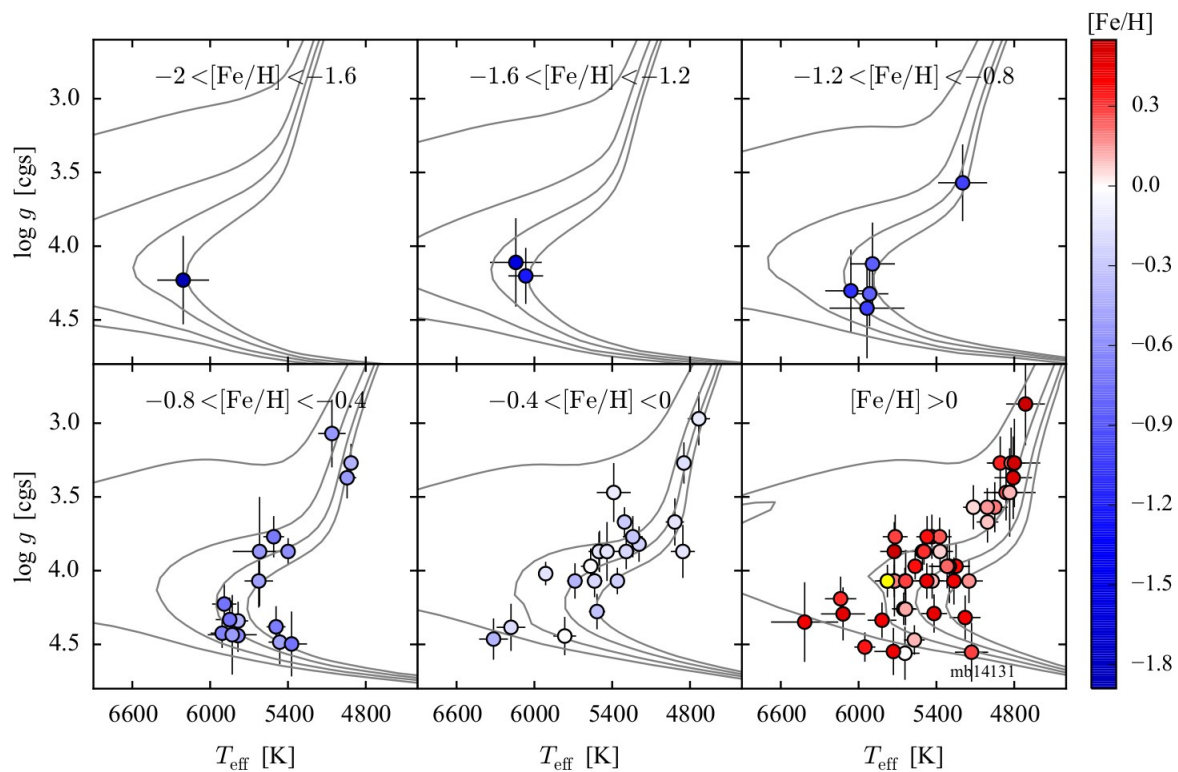


# Resulting age distribution (Joyce et al; MIST)

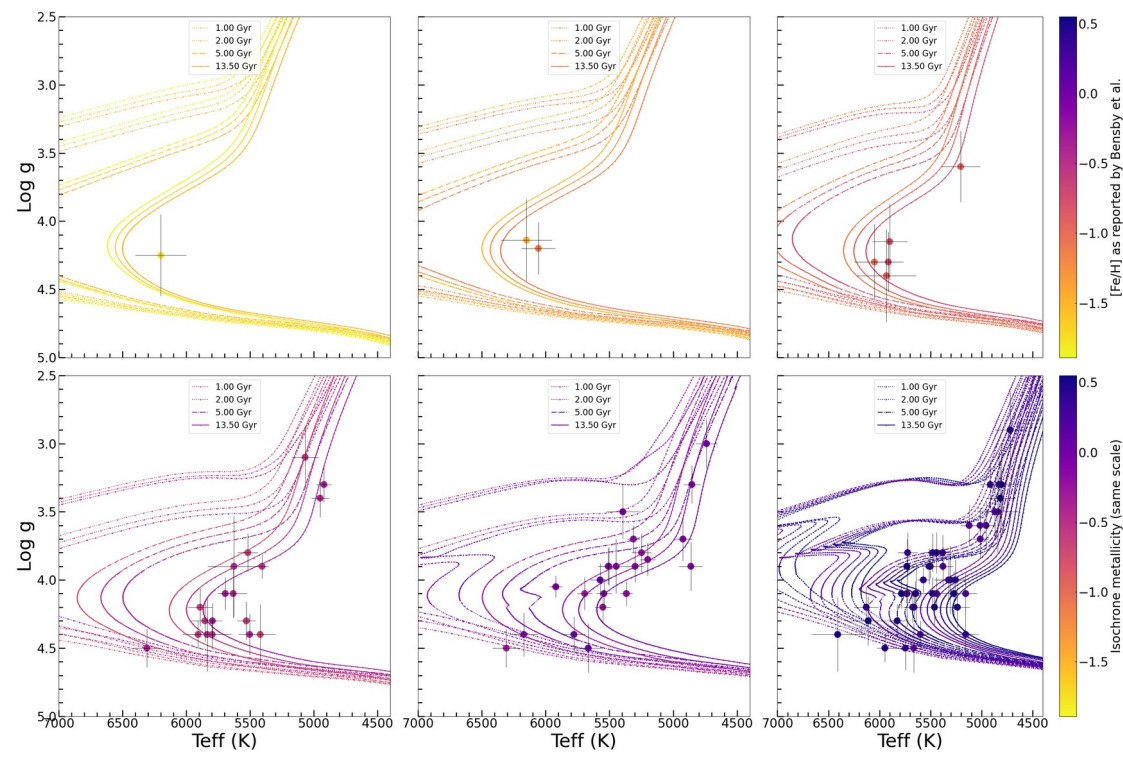


# Distributions overlaid





**They're the same picture.**

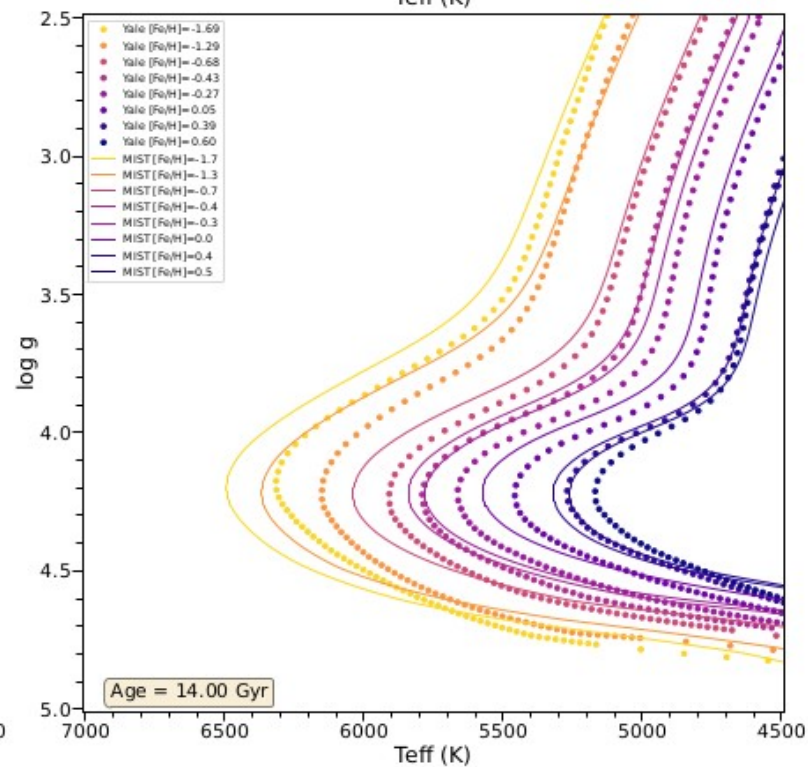
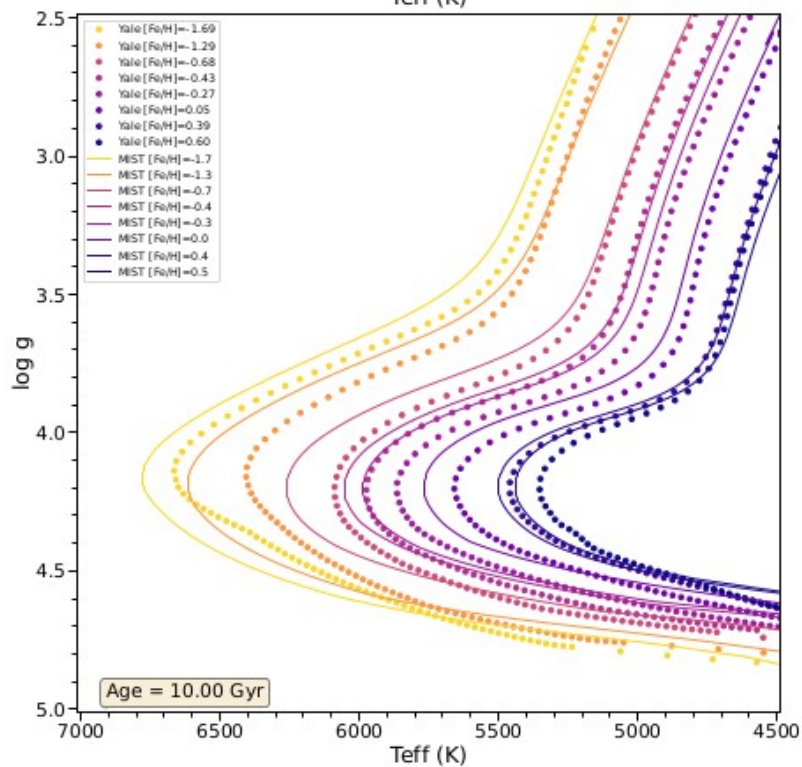
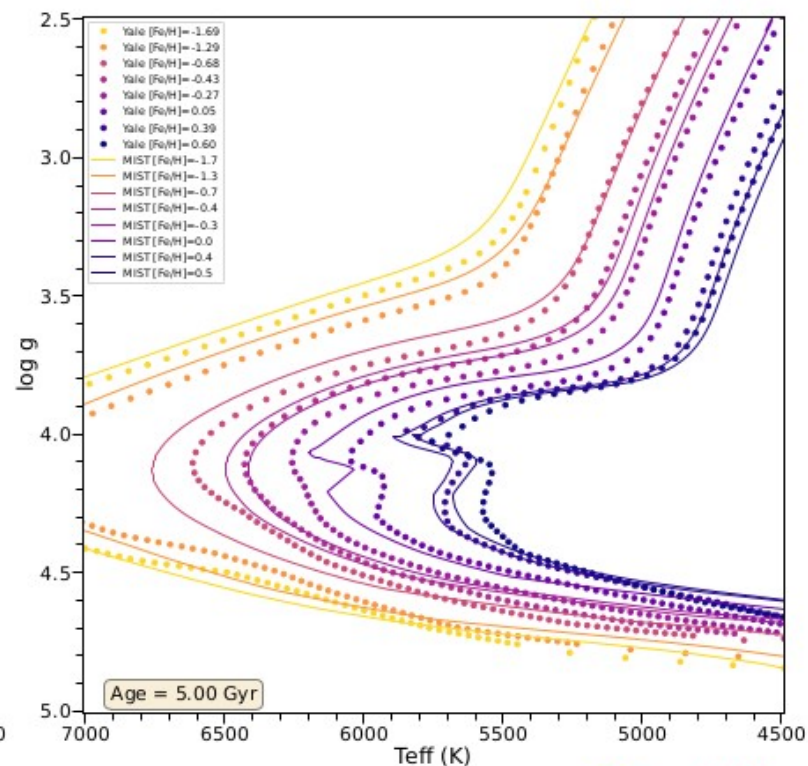
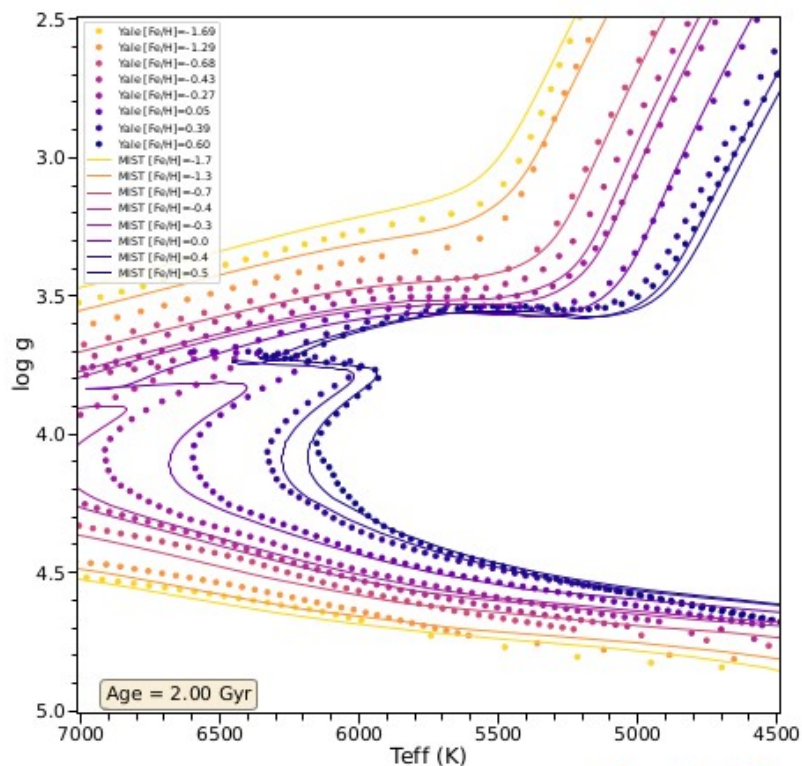


???

# One could reasonably ask...

Is it because the MIST and Yale models use wildly different physics and therefore yield different ages?

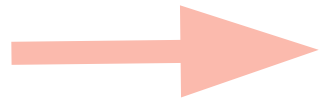
# Yale vs MIST





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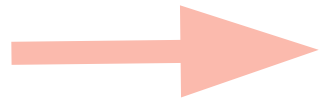
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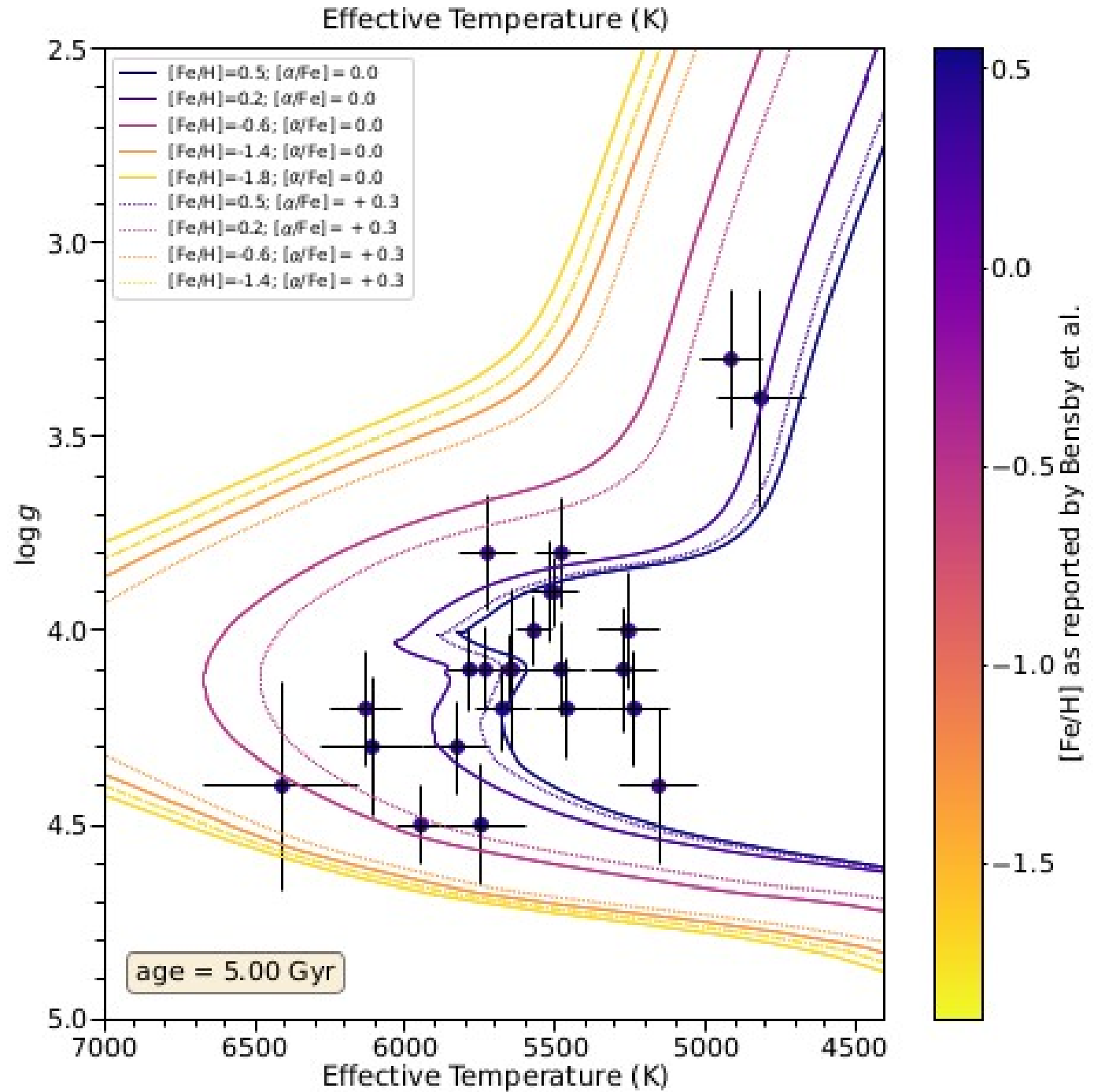


No

Is it because we consider alpha-element enhancement as a function of metallicity (Christian I. Johnson+, 2022) in the isochrones and the other age determinations do not?


# Effects of alpha-element enhancement

Example: MIST neutral  
vs MIST alpha-scaled



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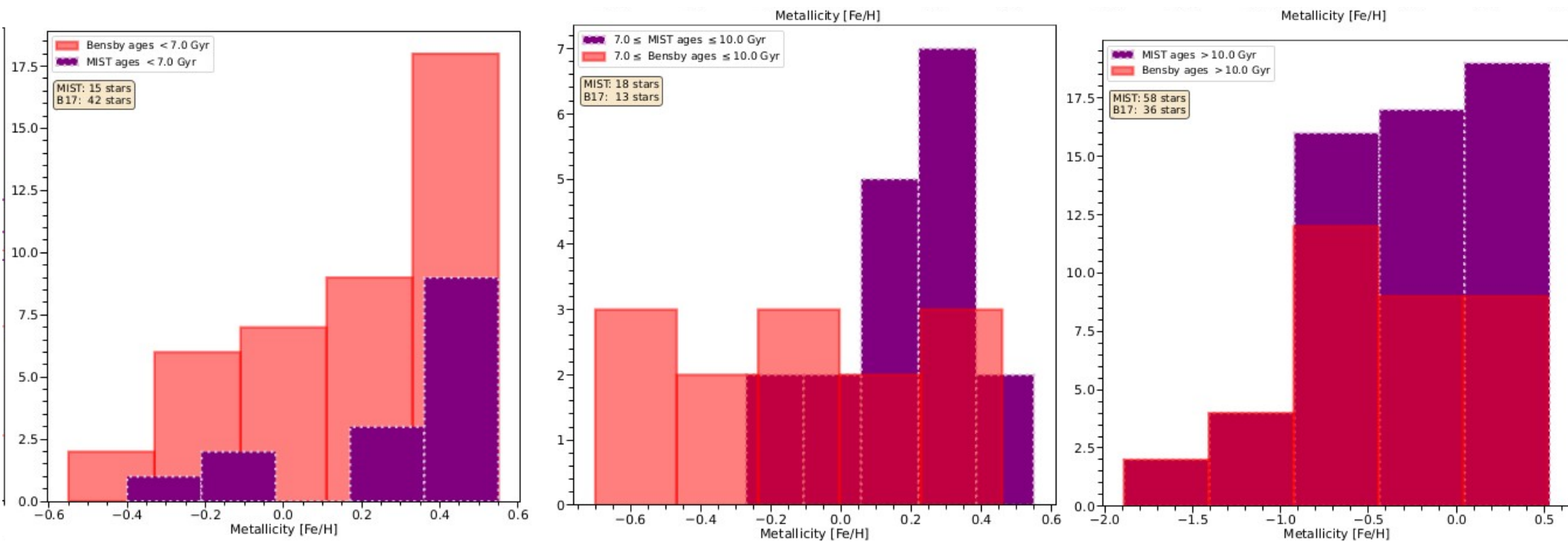
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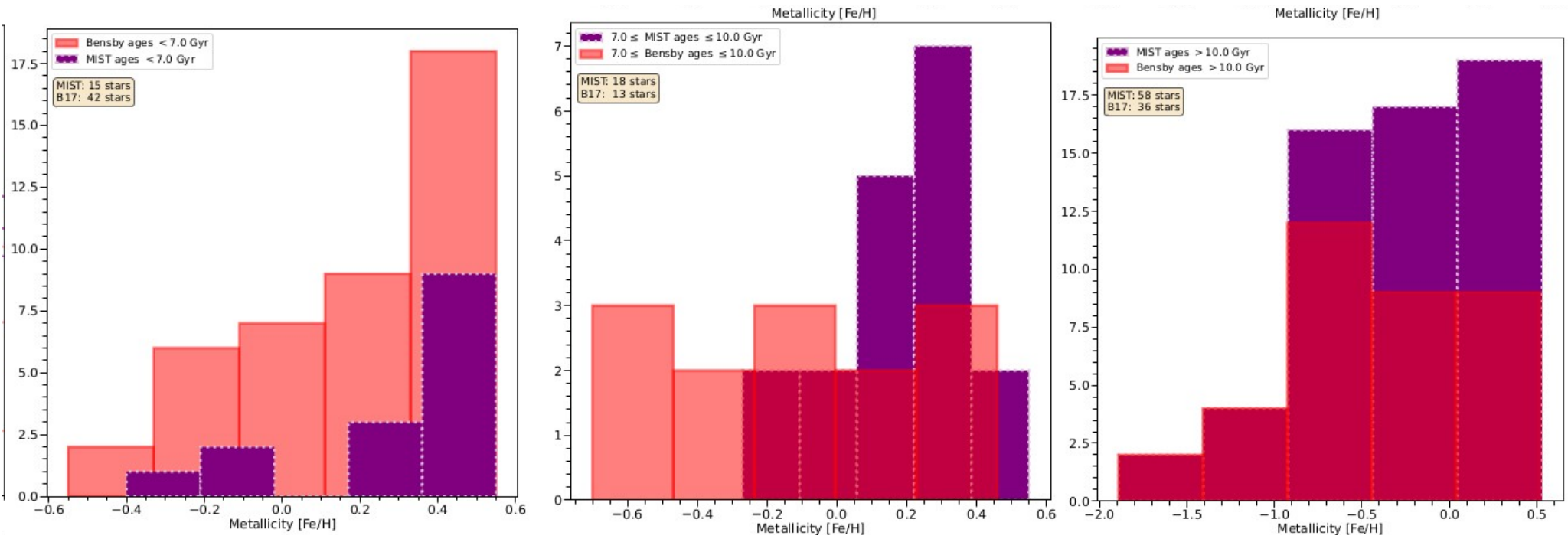
 Also no

\*see full paper (arXiv: 2205.07964) for rigorous demonstration of this using actual math & histograms

# Punchline: we (Joyce + MIST) do not find an abundance of young stars at high metallicities

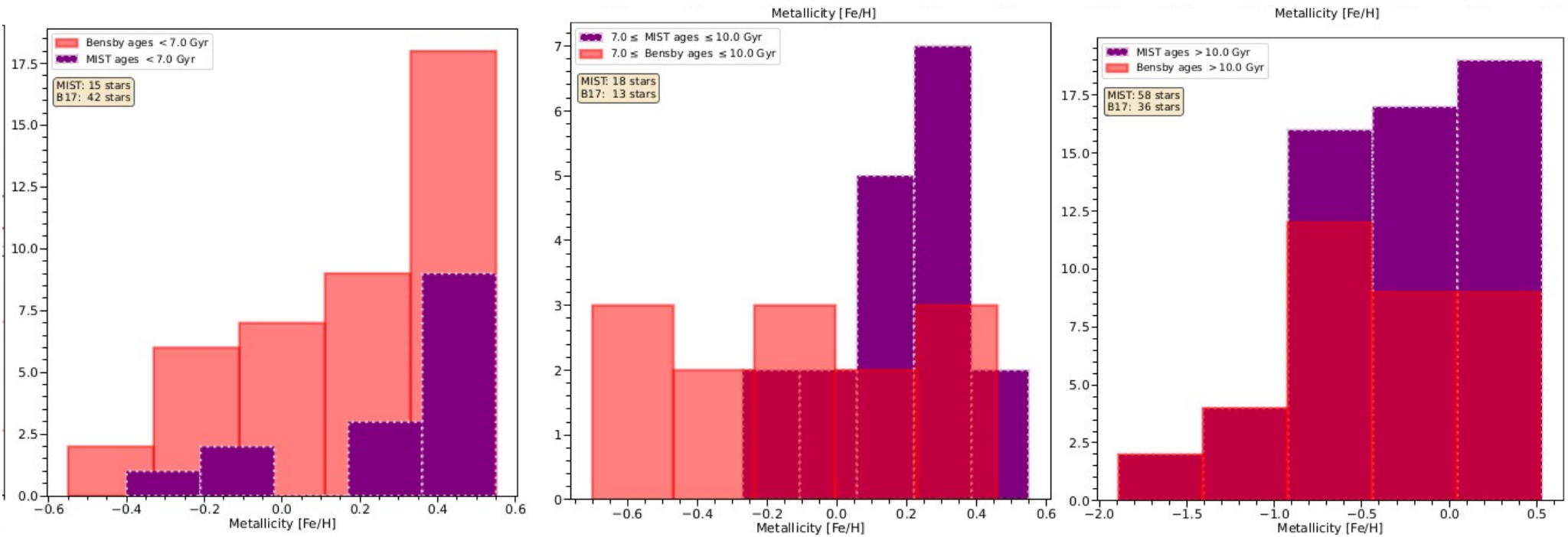


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**Bensby+ :** 42 stars <7 Gyr, all [Fe/H]>-0.6  
13 stars >7, <10 Gyr  
36 stars >10 Gyr

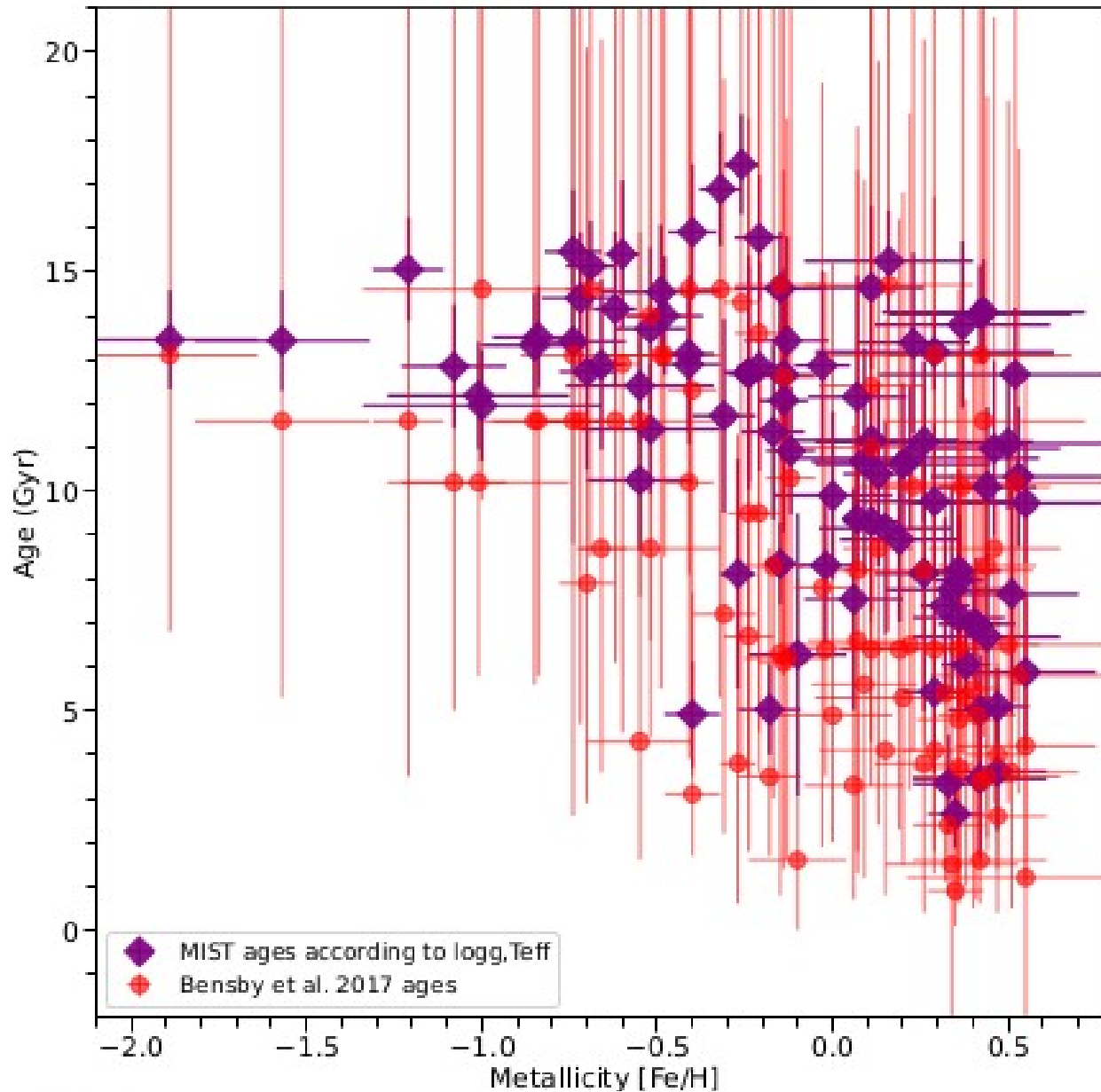
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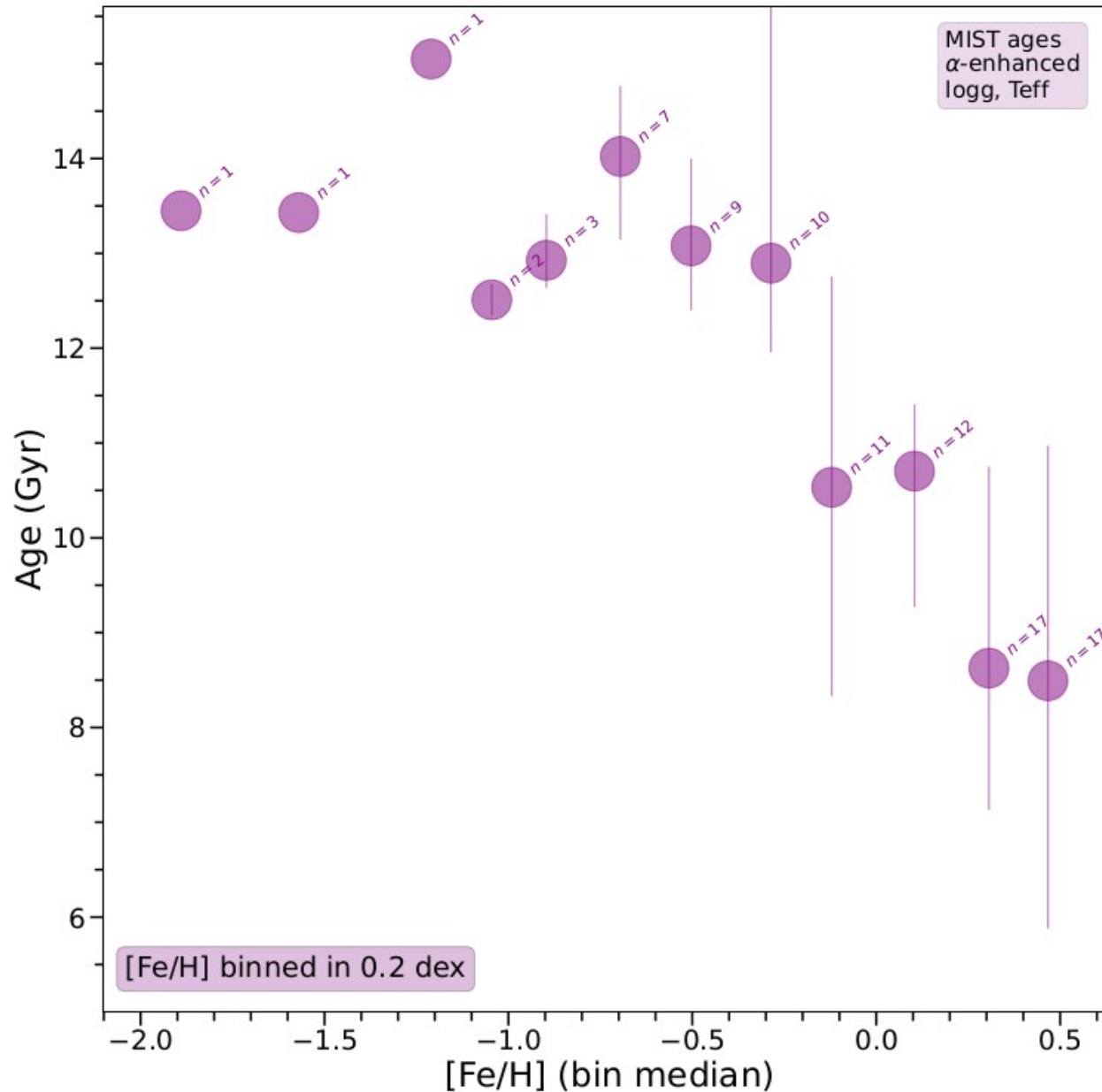
**Joyce+ :** 15 stars <7 Gyr, all [Fe/H]>-0.3  
18 stars >7, <10 Gyr  
58 stars >10 Gyr

**Punchline:** we (Joyce + MIST) **do not** find an abundance of young stars at high metallicities...**nor** do we find young or intermediate-age stars at metallicities below  $\sim$ solar  $[\text{Fe}/\text{H}]$



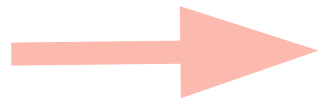


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**Why should you believe Joyce+MIST  
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# Why should you believe Joyce+MIST over the previous result?



Carefully considered  
hybrid statistical techniques

# Age determination algorithm

## Challenges:



Though it is straightforward to fit an isochrone to an observation “by eye,” it is much more difficult to construct a mathematically rigorous definition of a best-fitting model. This is especially true in a situation where:

1. many observations are plausibly consistent with a large number of isochrones (i.e., the isochrone falls within the star’s  $1\sigma$  uncertainties);
2. the isochrones are discretely spaced in age and metallicity and thus limited in resolution; and
3. the models contain their own intrinsic uncertainties that are both difficult to quantify and highly variant over different parameter regimes—a point to which we will return in later discussion.

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$$\chi^2_{\text{for } i \text{ DoF}} = \sum_i \frac{(o_i - t_i)^2}{\sigma_i^2}$$

(1) For a given star, compute the (3 DoF) chisq score for the fit of that star's observational parameters to **every** point along a candidate model (e.g. isochrone)

$$\chi^2_{\text{B17}} = \frac{(\log g_o - \log g_t)^2}{\sigma_{\log g,o}^2} + \frac{(T_{\text{eff},o} - T_{\text{eff},t})^2}{\sigma_{T_{\text{eff},o}}^2} + \frac{(Z_o - Z_t)^2}{\sigma_{Z,o}^2},$$

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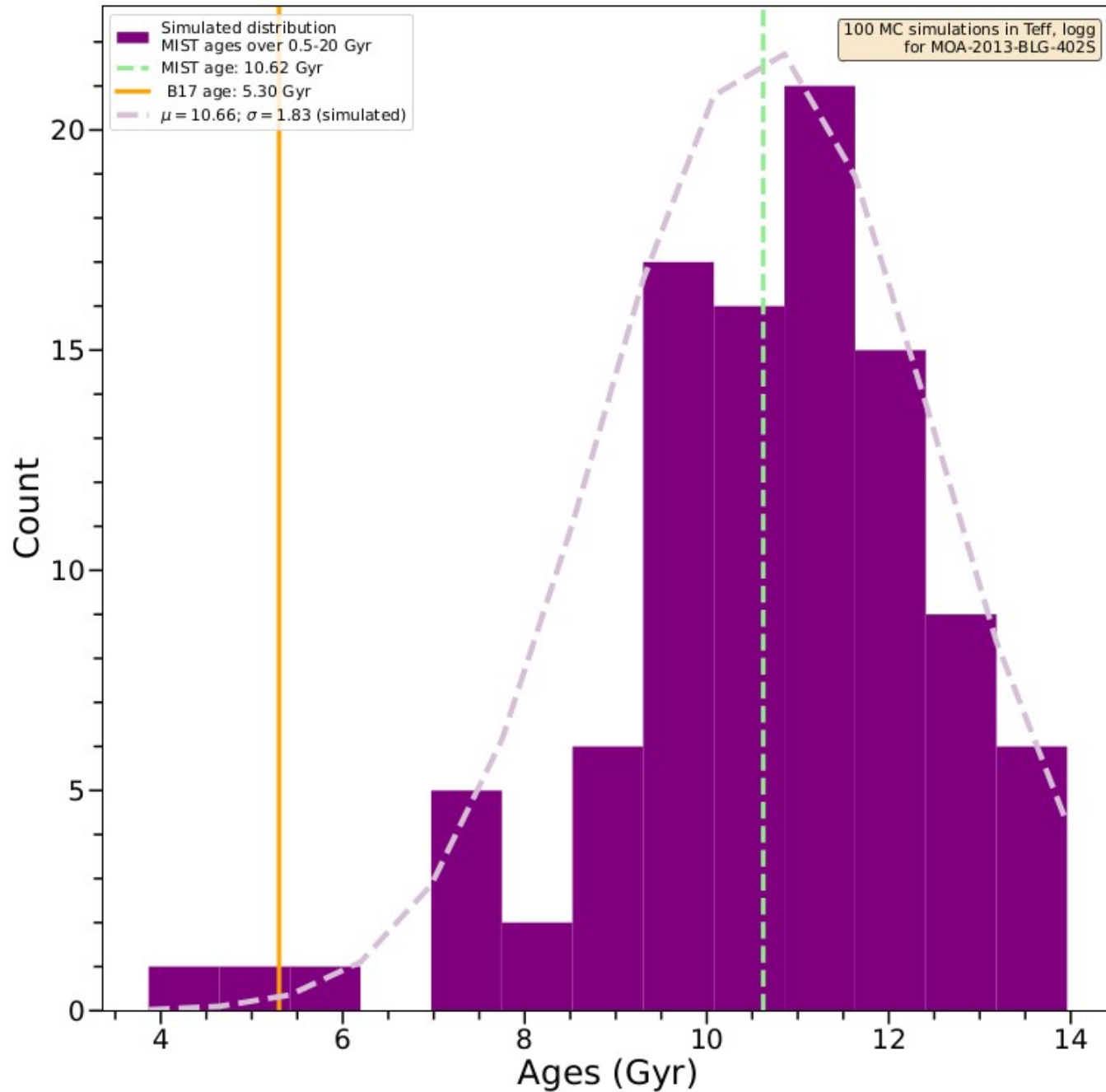
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(3) - Compute a weighted average over all candidate hypotheses (each point on each isochrone)  
- A point with age  $t_n$  is weighted by its likelihood,  $p_n$ , of being an appropriate fit to the star  
- The final weighted average,  $t_s$ , is our estimate for the age of the star

(2) Each chisq score corresponds to a relative likelihood,  $p_n$ , given by the density function of the chi square distribution with 3 DoF at that score.

$$t_s = \frac{\sum_n t_n p_n}{\sum_n p_n},$$

# Error bars: Monte Carlo resampling



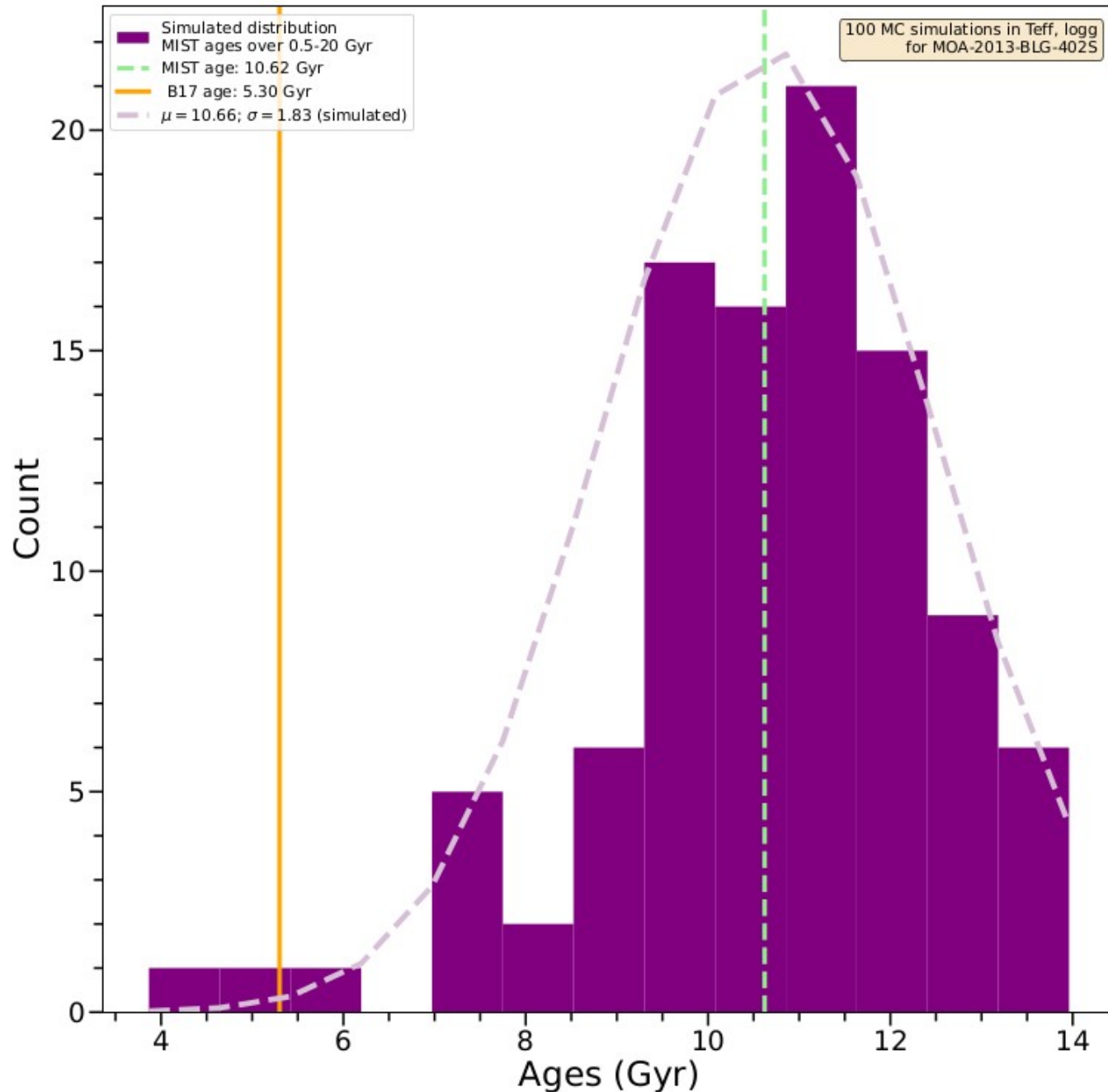
Construct three independent normal distributions with densities

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-(x-\mu)^2/2\sigma^2}$$

defined by

$$\begin{aligned} \mu &= T_{\text{eff},S}, & \sigma &= \sigma_{T_{\text{eff},S}}, \\ \mu &= \log g_S, & \sigma &= \sigma_{\log g_S}, \\ \mu &= Z_S, & \sigma &= \sigma_{Z_S} \end{aligned}$$

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→ the fact that our MC simulations build a distribution **approaching a normal distribution** as number of trials increases suggests that **the assumption of normally distributed variables is reasonable**

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- convective boundaries; how the Schwarzschild/Ledoux criterion is evaluated



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## **Atmospheric boundary conditions:**

- Is it a T-tau relation, & what kind of integration? Eddington vs Krishna-Swamy
- if instead using a table-based treatment from external simulations (e.g. PHOENIX, Kurucz), what solar scale and other physics were used in those simulations? Are they self-consistent with the assumptions in the stellar models?

Point of demonstration: the convective  
mixing length,  $\alpha_{MLT}$

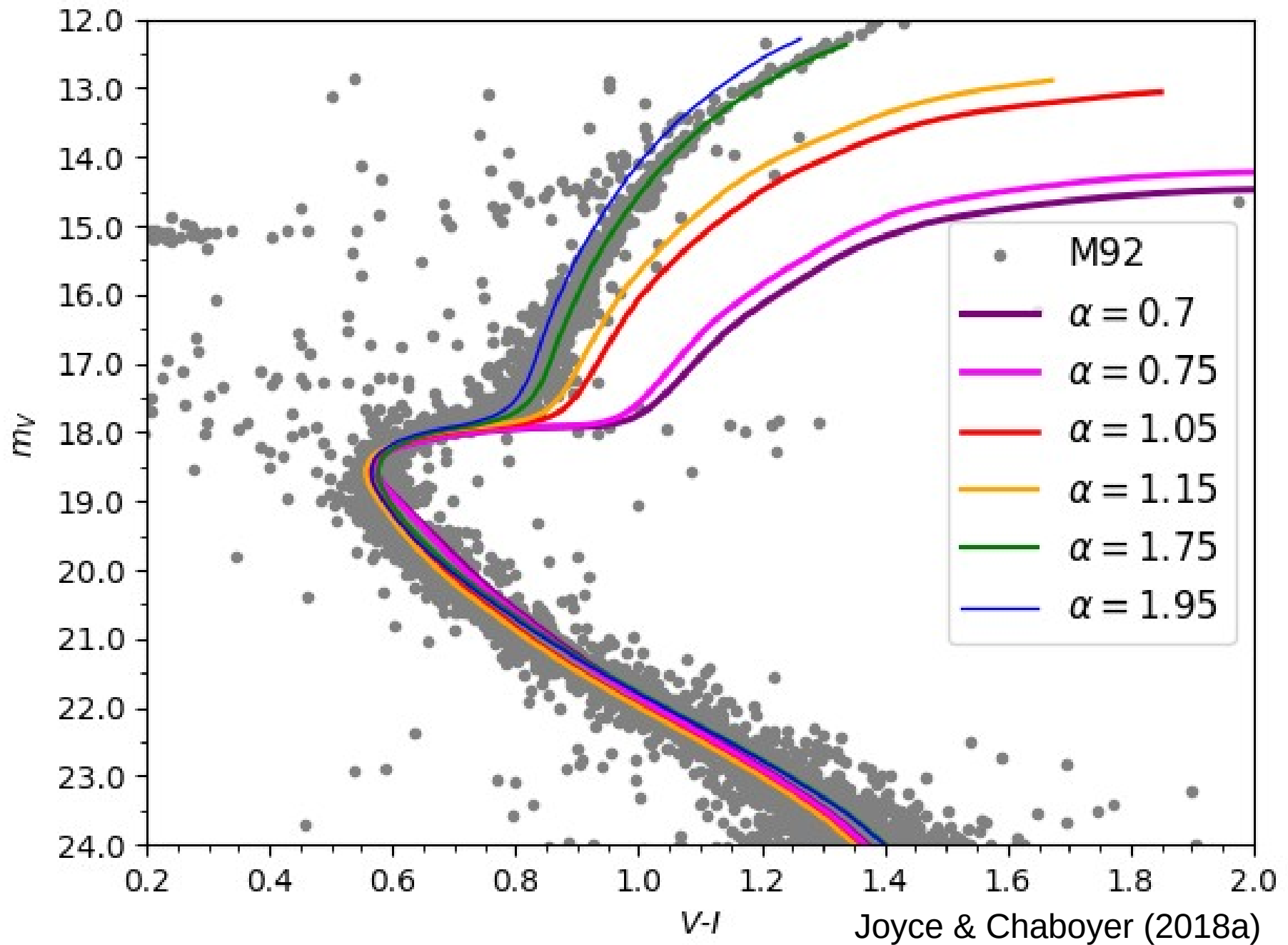
**Why this parameter?**

# Point of demonstration: the convective mixing length, $\alpha_{\text{MLT}}$

## Why this parameter?

- even modest changes to  $\alpha_{\text{MLT}}$  dramatically affect the morphology of isochrones between the MSTO and tip of the red giant branch

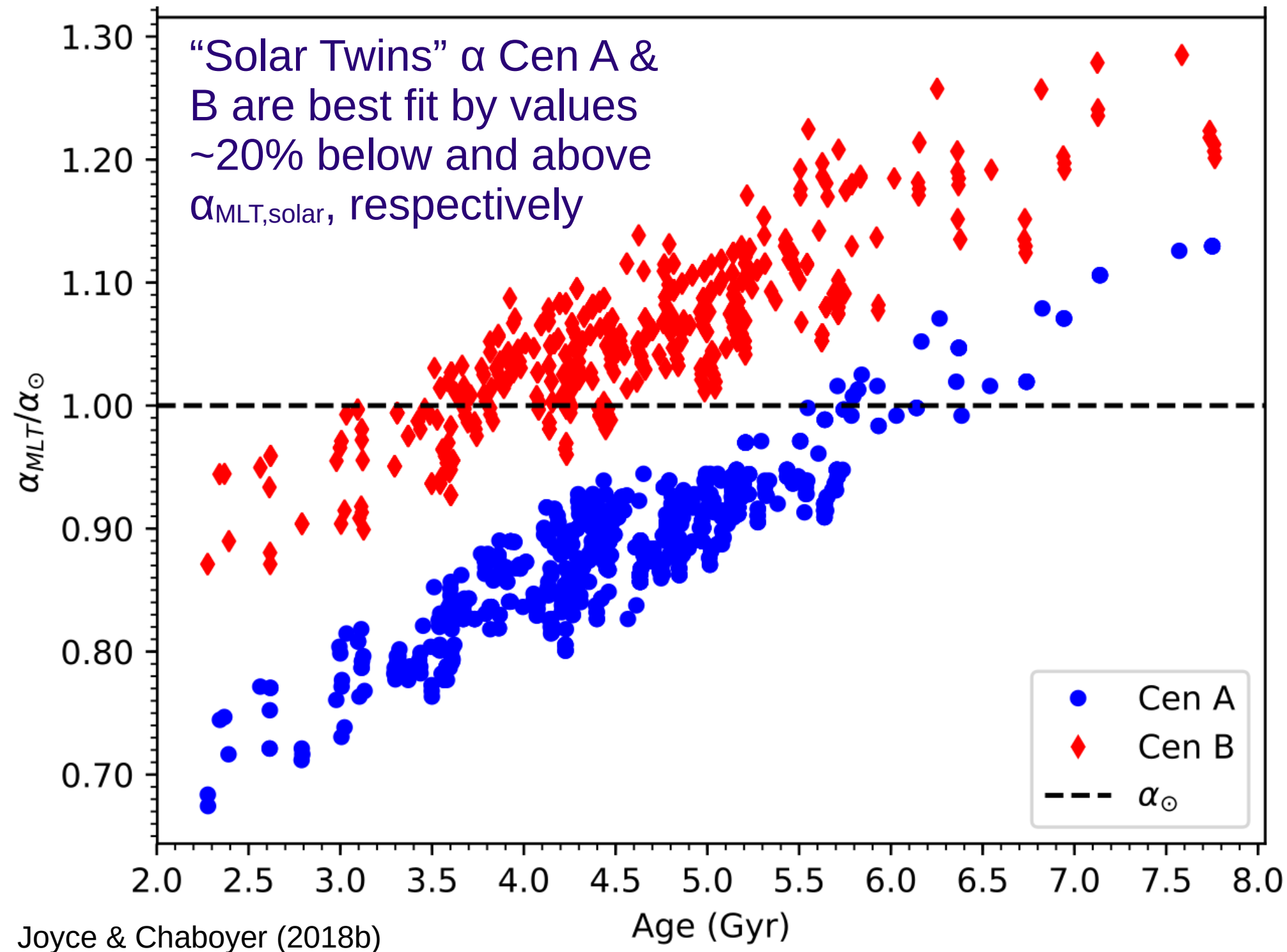
# Look at those RGBs!



# Point of demonstration: the convective mixing length, $\alpha_{\text{MLT}}$

## Why this parameter?

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- previous work has shown that even stars very similar to the Sun are better fit by mixing length values 10-20% different than the solar-calibrated value

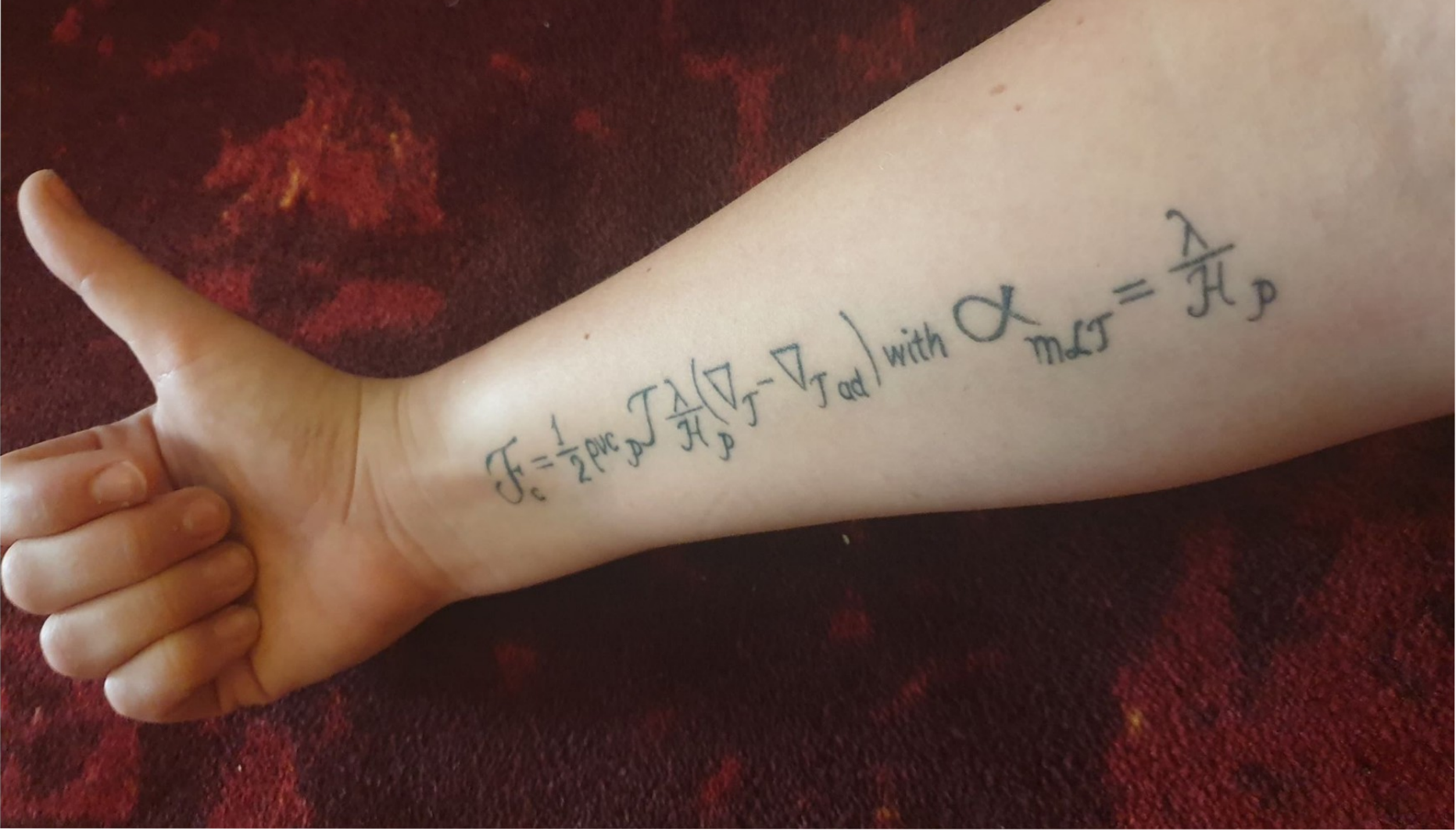


# Point of demonstration: the convective mixing length, $\alpha_{\text{MLT}}$

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- previous work has shown that even stars very similar to the Sun are better fit by mixing length values 10-20% different than the solar-calibrated value
- because it's my favorite parameter/because I can

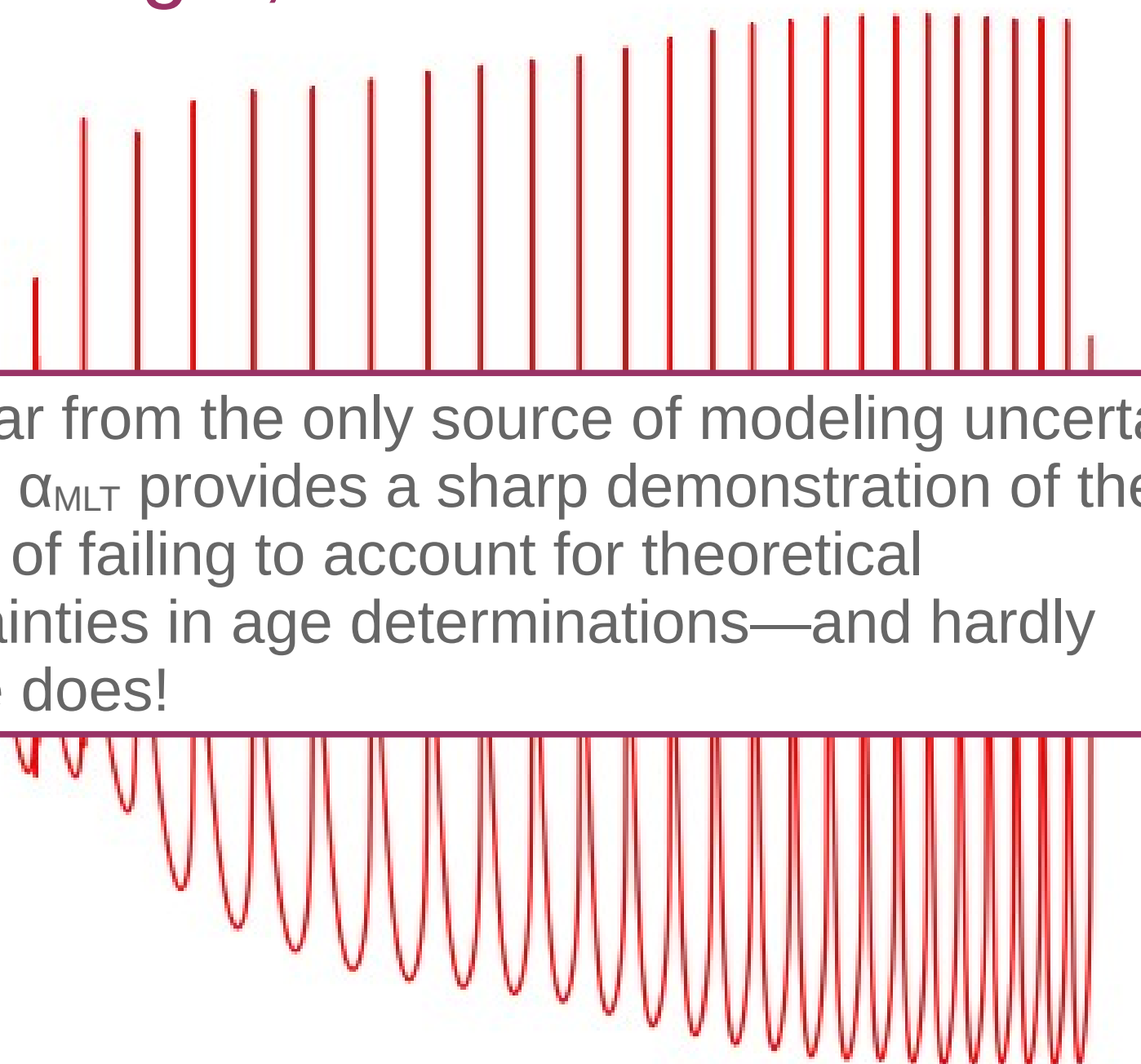




The image shows a person's forearm with a hand gesture (thumb up, fingers curled). A mathematical formula is written in black ink on the skin. The formula is:

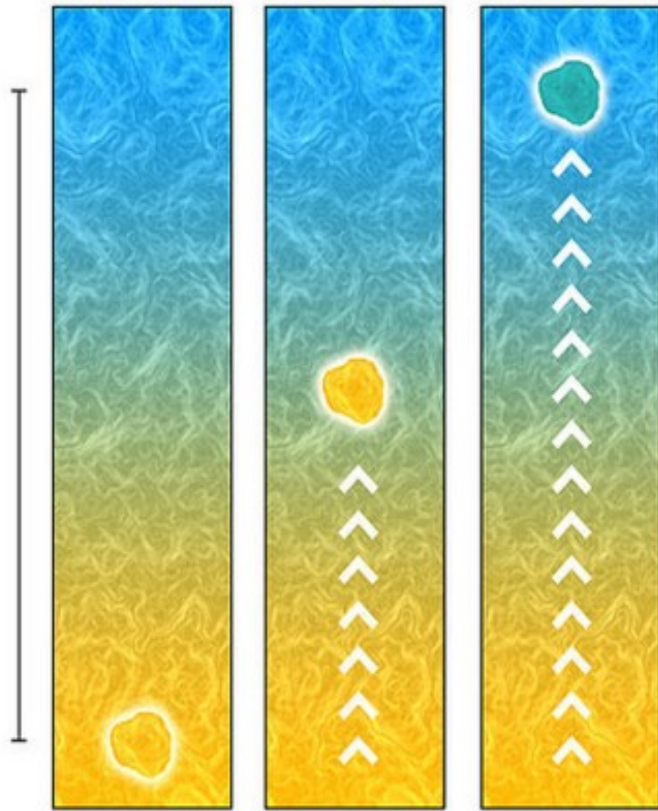
$$F_c = \frac{1}{2} \rho v c_p \int \frac{\lambda}{H_p} (\nabla_T - \nabla_{T_{ad}}) \text{ with } \alpha_{mLT} = \frac{\lambda}{H_p}$$

# Point of demonstration: the convective mixing length, $\alpha_{\text{MLT}}$



While far from the only source of modeling uncertainty, varying  $\alpha_{\text{MLT}}$  provides a sharp demonstration of the danger of failing to account for theoretical uncertainties in age determinations—and hardly anyone does!

# The convective mixing length: The most important neglected parameter in stellar modeling!



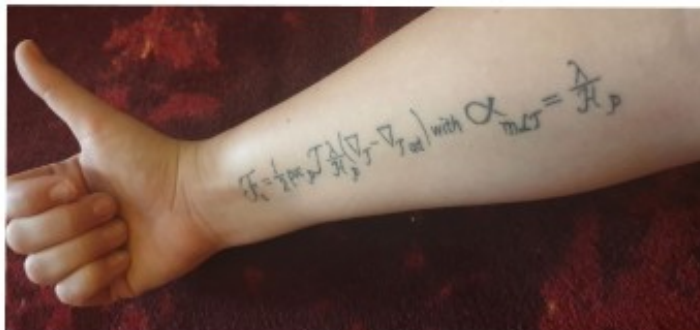
$$F_{\text{conv}} = \frac{1}{2} \rho v c_p T \frac{\lambda}{H_P} (\nabla_T - \nabla_{\text{ad}}).$$

$$\alpha_{\text{MLT}} = \frac{\lambda}{H_P}, \quad \nabla_T = \left( \frac{d \ln T}{d \ln P} \right)$$

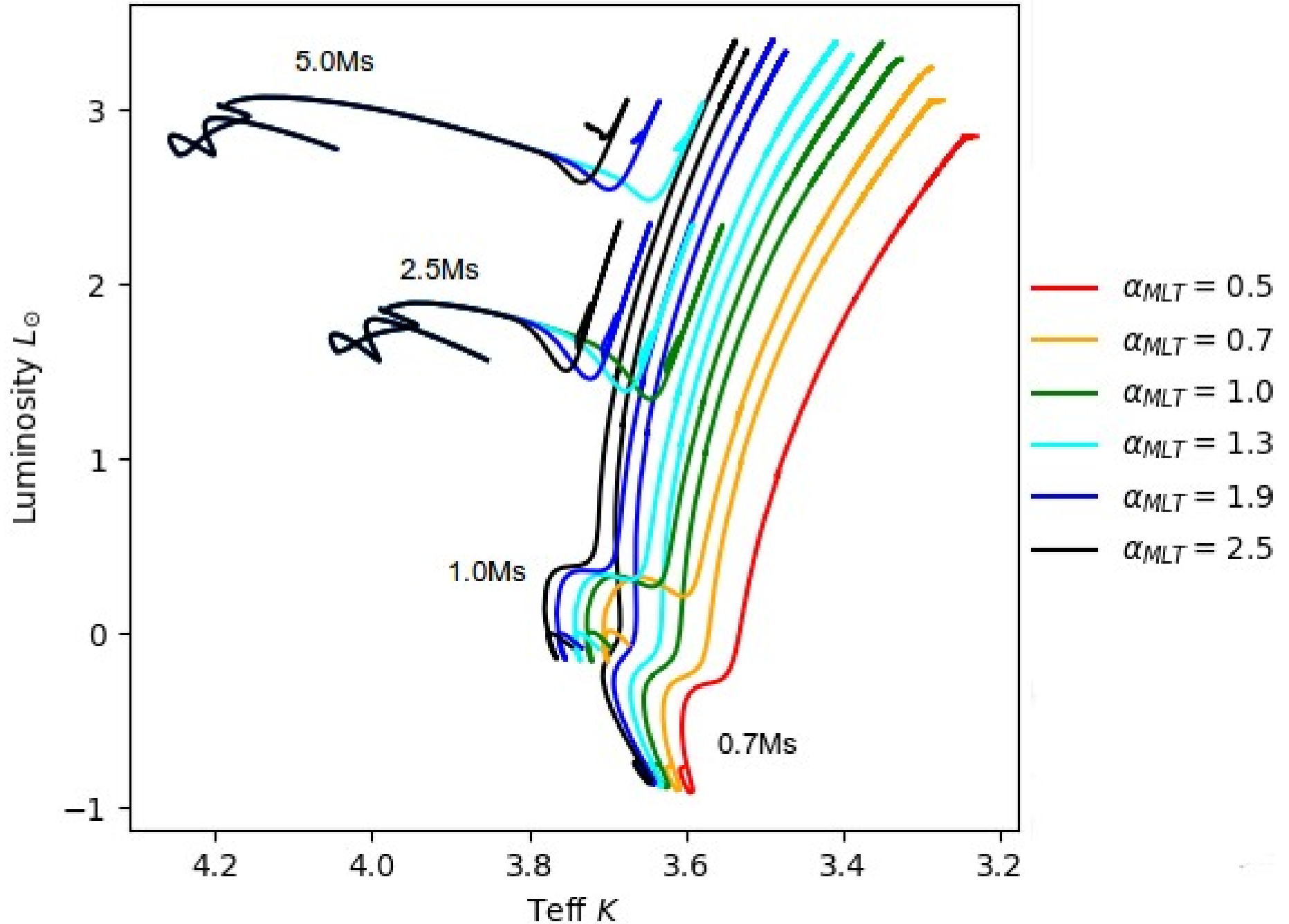
- “mixing length:” average vertical distance over which parcels in pressure, but not thermal, equilibrium can travel before denaturing

-  $\alpha_{\text{MLT}}$  represents mean free path measured in pressure scale heights,  $H_P = d \ln(P)/d \ln(T)$

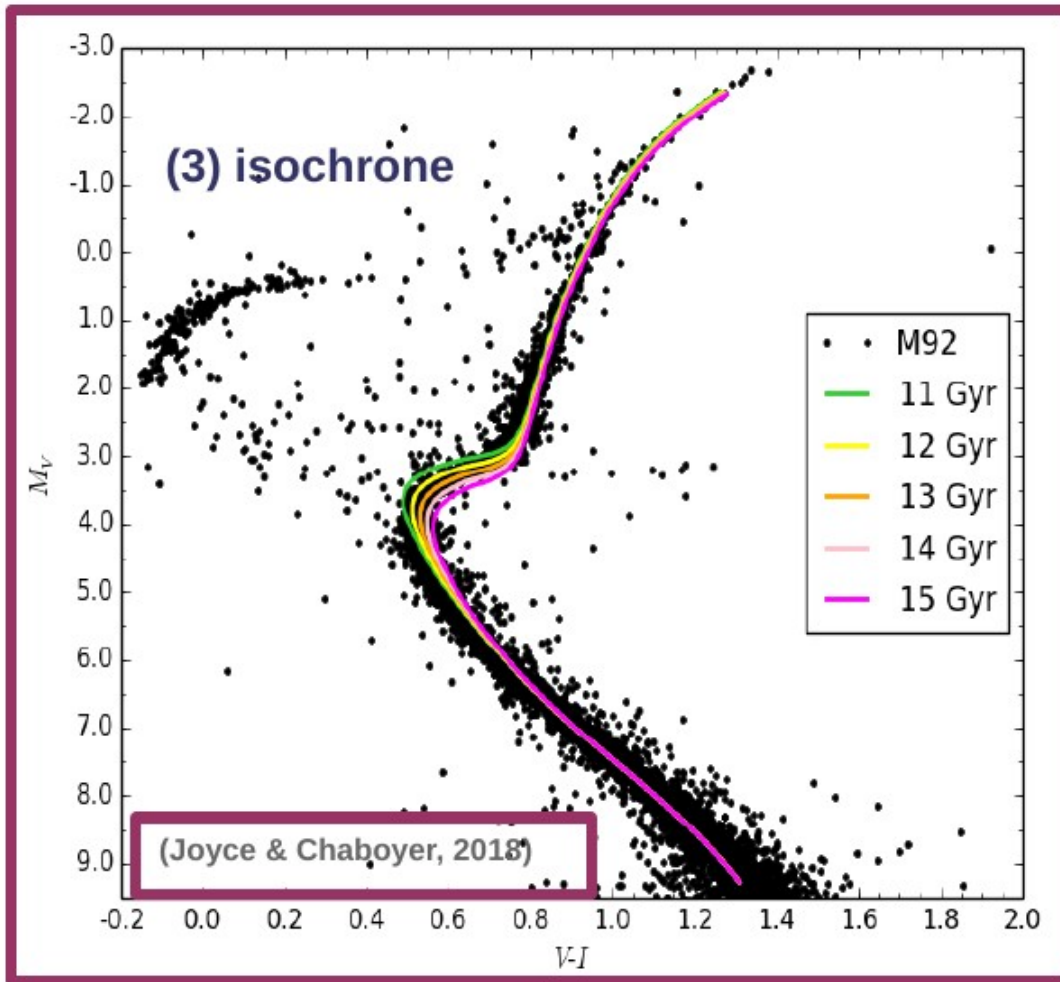
- a measure of “efficiency” of convection



# Effect of $\alpha_{MLT}$ on a stellar track



# Isochrone review



Derive fundamental parameters for both individual stars and stellar populations

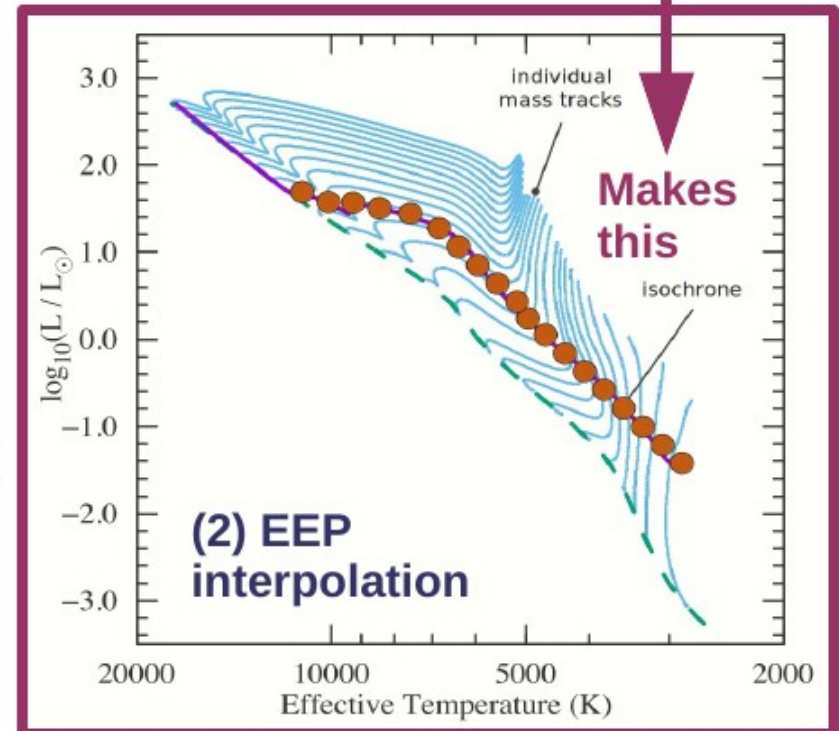
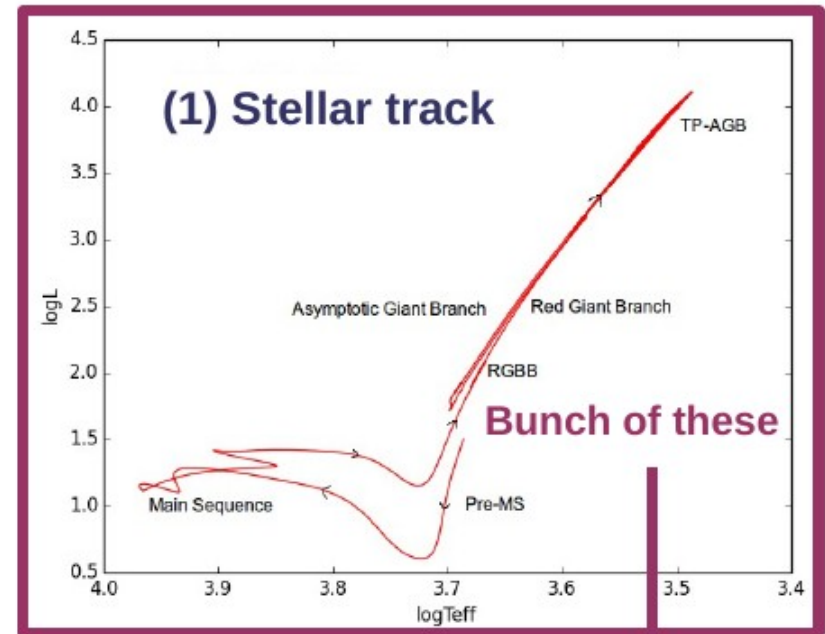
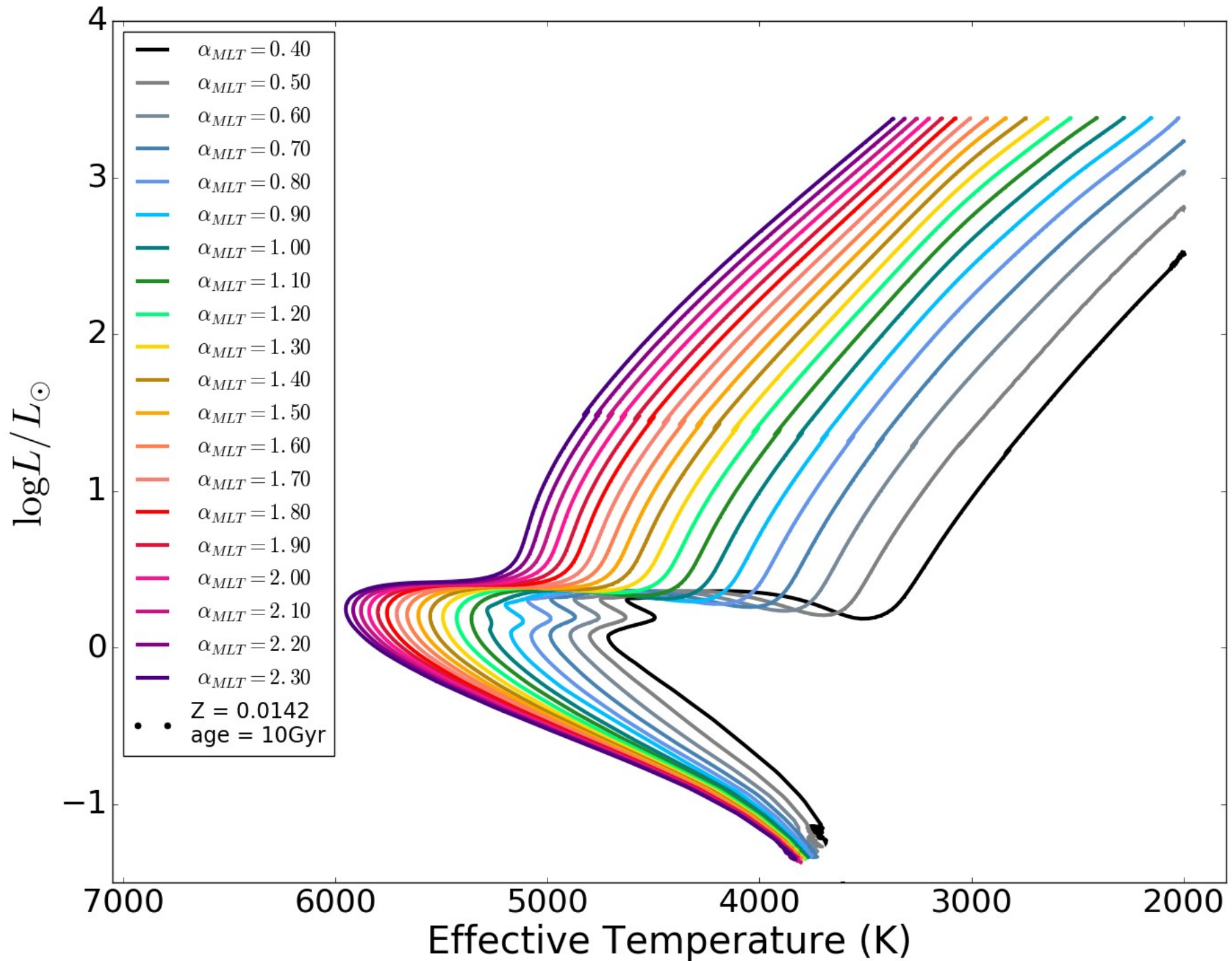
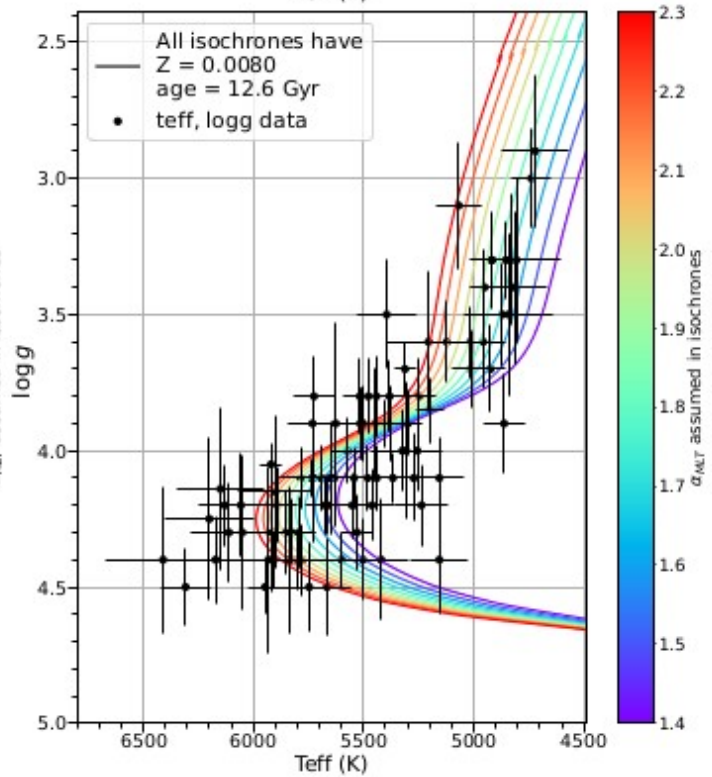
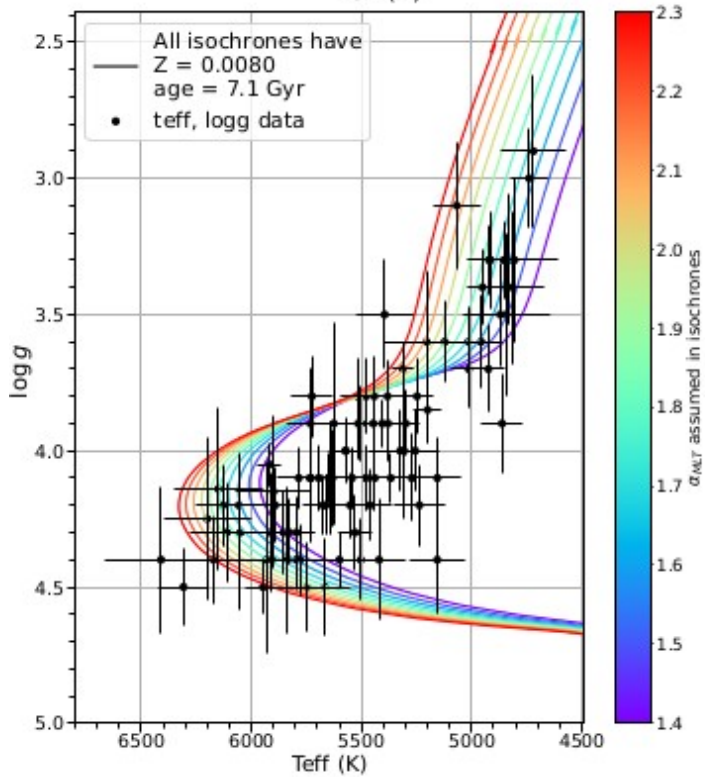
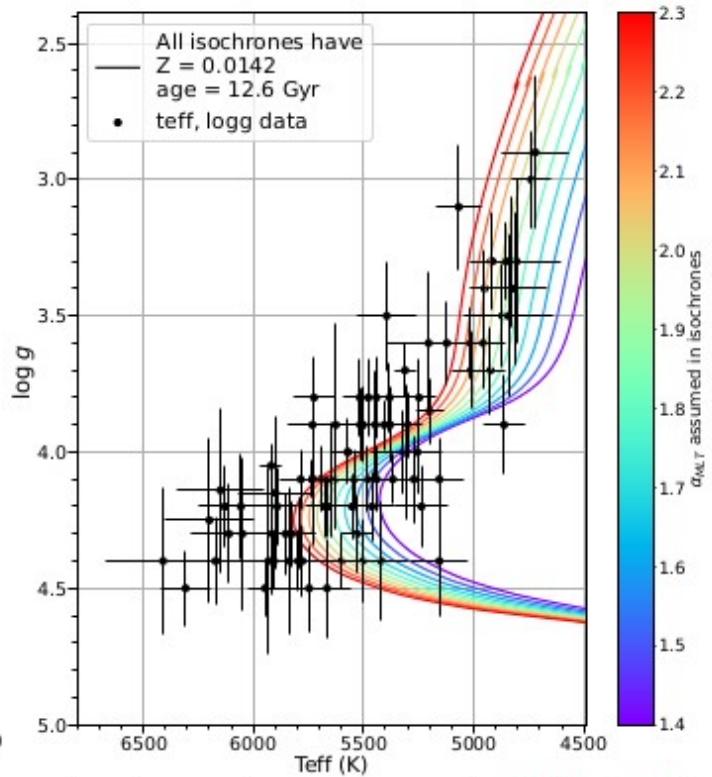
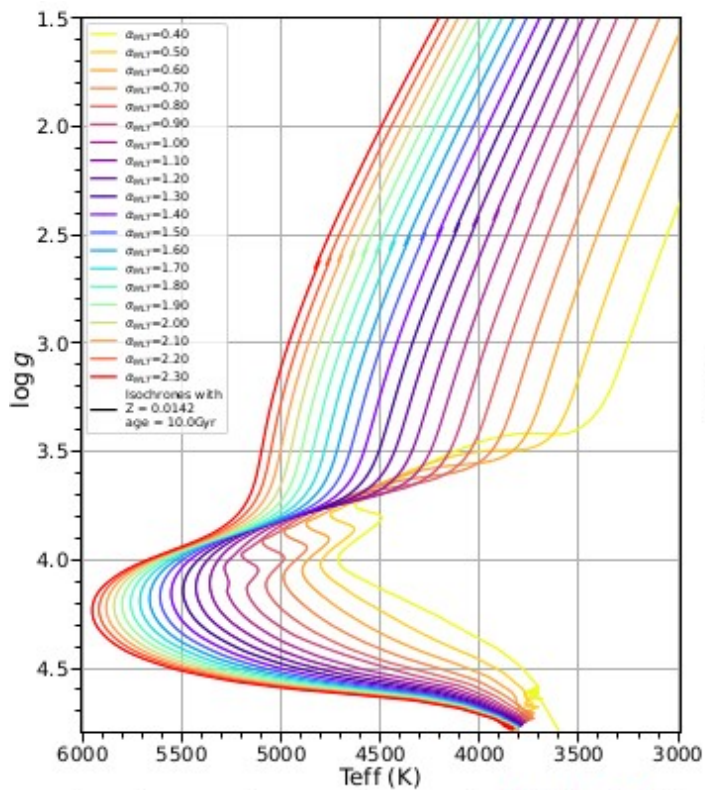


Figure 1: a set of isochrones, each having the same assumption for metallicity but computed with different mixing length values, as indicated on the legend.



# The impact of $\alpha$ MLT



# How do we incorporate the isochrones' “shift” in our error simulations?

Figure 11. In a new set of Monte Carlo simulations, we adopt the same definitions for  $\chi^2$  and  $t_S$  given in Equations 2 and 3 and sample from the same distributions in observational parameters given in Equation 4, but we introduce an additional term accounting for variation in the isochrones. In each Monte Carlo simulation, we sample normal distributions given by

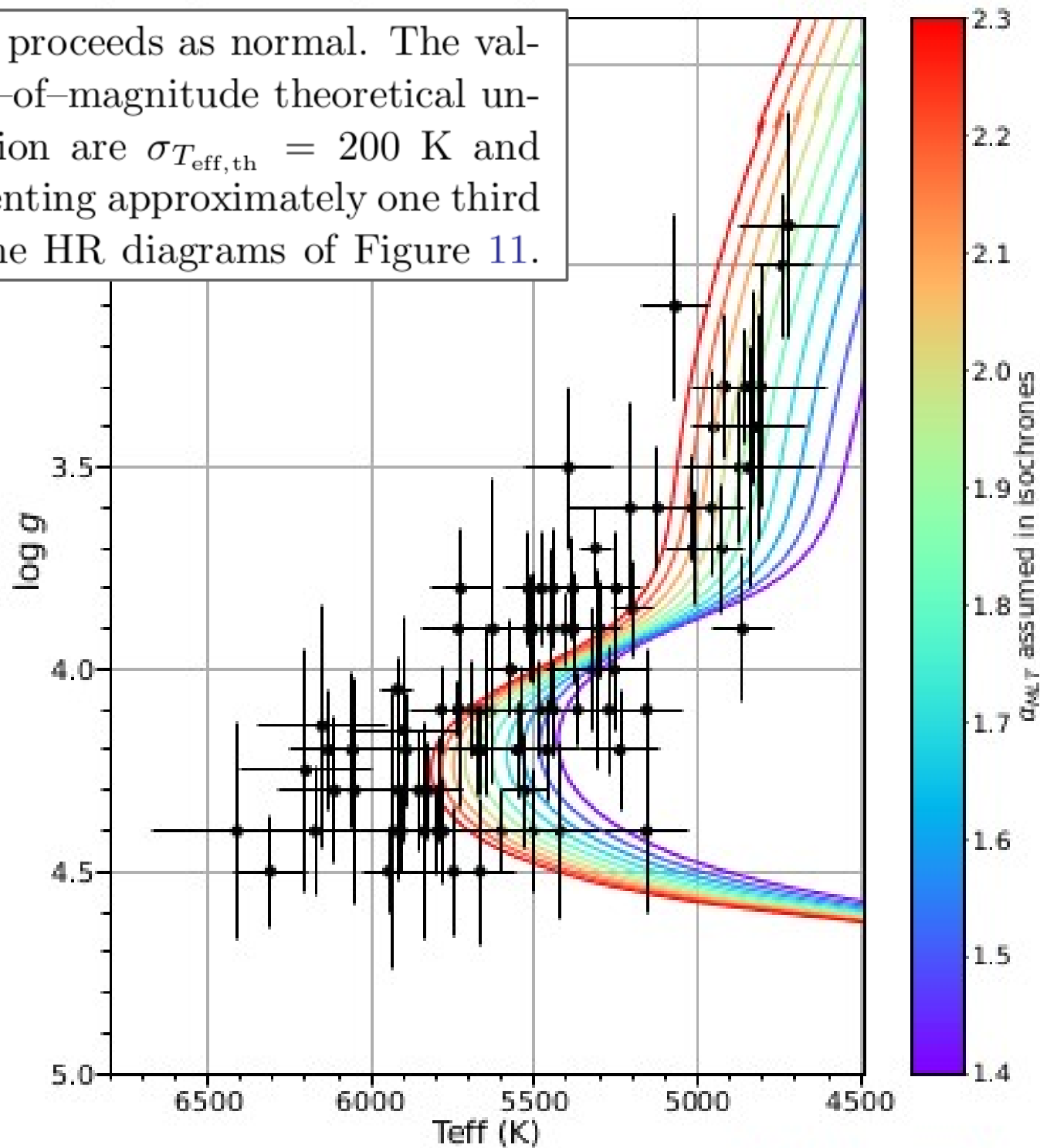
$$\mu = 0, \quad \sigma = \sigma_{T_{\text{eff,th}}} \quad (5a)$$

$$\mu = 0, \quad \sigma = \sigma_{\log g_{\text{th}}}, \quad (5b)$$

uniformly shifting the entire basis of isochrones horizontally by a random sample of **Equation 5a** and vertically by a random sample from **Equation 5b**.



The rest of the algorithm proceeds as normal. The values adopted for the order-of-magnitude theoretical uncertainties in each direction are  $\sigma_{T_{\text{eff,th}}} = 200$  K and  $\sigma_{\log g_{\text{th}}} = 0.17$  dex, representing approximately one third of the spans<sup>6</sup> shown in the HR diagrams of Figure 11.



# What happens when we incorporate variation in the isochrones' position in $\log g$ - $T_{\text{eff}}$ in the MC simulations?

	Name	.. $\alpha$ -enhanced	...model err
1	MOA-2009-BLG-174S	$9.3 \pm 2.0$	$9.3 \pm 4.0$
2	MOA-2009-BLG-259S	$7.8 \pm 2.4$	$7.8 \pm 3.8$
3	MOA-2010-BLG-167S ★	$15.4 \pm 1.7$	$15.4 \pm 3.8$
4	MOA-2010-BLG-311S	$7.7 \pm 2.7$	$7.7 \pm 3.3$
5	MOA-2010-BLG-446S	$4.9 \pm 1.2$	$4.9 \pm 2.0$
6	MOA-2010-BLG-523S ★	$7.5 \pm 2.5$	$7.5 \pm 3.8$
7	OGLE-2011-BLG-0950S ★ †	$3.3 \pm 1.1$	$3.3 \pm 1.6$
8	OGLE-2011-BLG-0969S ★	$13.4 \pm 1.1$	$13.4 \pm 1.5$
9	MOA-2011-BLG-034S	$14.6 \pm 1.9$	$14.6 \pm 2.8$
10	MOA-2011-BLG-058S	$13.8 \pm 1.9$	$13.8 \pm 2.8$
11	OGLE-2011-BLG-1072S	$8.2 \pm 2.3$	$8.2 \pm 3.4$
12	MOA-2011-BLG-090S	$17.4 \pm 1.1$	$17.4 \pm 2.7$
13	MOA-2011-BLG-104S	$13.3 \pm 1.2$	$13.3 \pm 1.8$
14	OGLE-2011-BLG-1105S	$9.9 \pm 1.9$	$9.9 \pm 2.9$
15	MOA-2011-BLG-174S	$5.0 \pm 1.0$	$5.0 \pm 2.5$
16	MOA-2011-BLG-191S	$8.1 \pm 3.1$	$8.1 \pm 4.1$
17	MOA-2011-BLG-234S †	$8.3 \pm 1.8$	$8.3 \pm 3.0$
18	MOA-2011-BLG-278S	$12.7 \pm 1.5$	$12.7 \pm 1.8$
19	OGLE-2011-BLG-1410S	$10.8 \pm 1.6$	$10.8 \pm 2.4$
20	MOA-2011-BLG-445S	$11.1 \pm 1.8$	$11.1 \pm 2.8$
21	MOA-2012-BLG-022S	$5.0 \pm 1.3$	$5.0 \pm 2.2$
22	OGLE-2012-BLG-0026S	$11.1 \pm 1.5$	$11.1 \pm 2.5$

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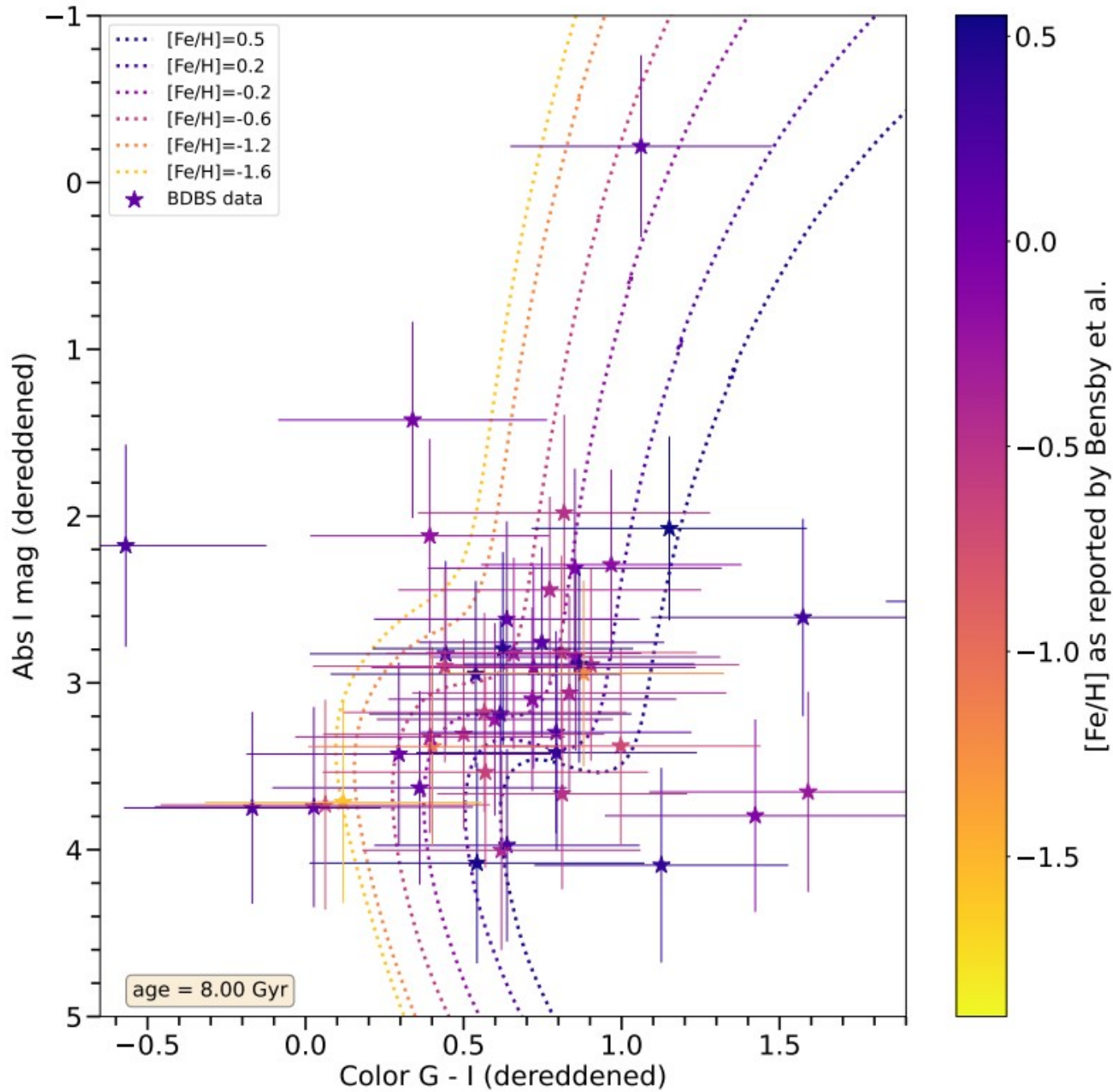
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9	MOA-2011-BLG-001S	$9.8 \pm 1.8$	$9.8 \pm 3.8$
10	MOA-2011-BLG-002S	$8.2 \pm 1.5$	$8.2 \pm 3.4$
11	MOA-2011-BLG-003S	$17.4 \pm 1.1$	$17.4 \pm 2.7$
12	MOA-2011-BLG-004S	$13.3 \pm 1.2$	$13.3 \pm 1.8$
13	MOA-2011-BLG-005S	$9.9 \pm 1.9$	$9.9 \pm 2.9$
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uncertainties increase by a factor of 1.5 - 2x

Tension between  
inference methods?

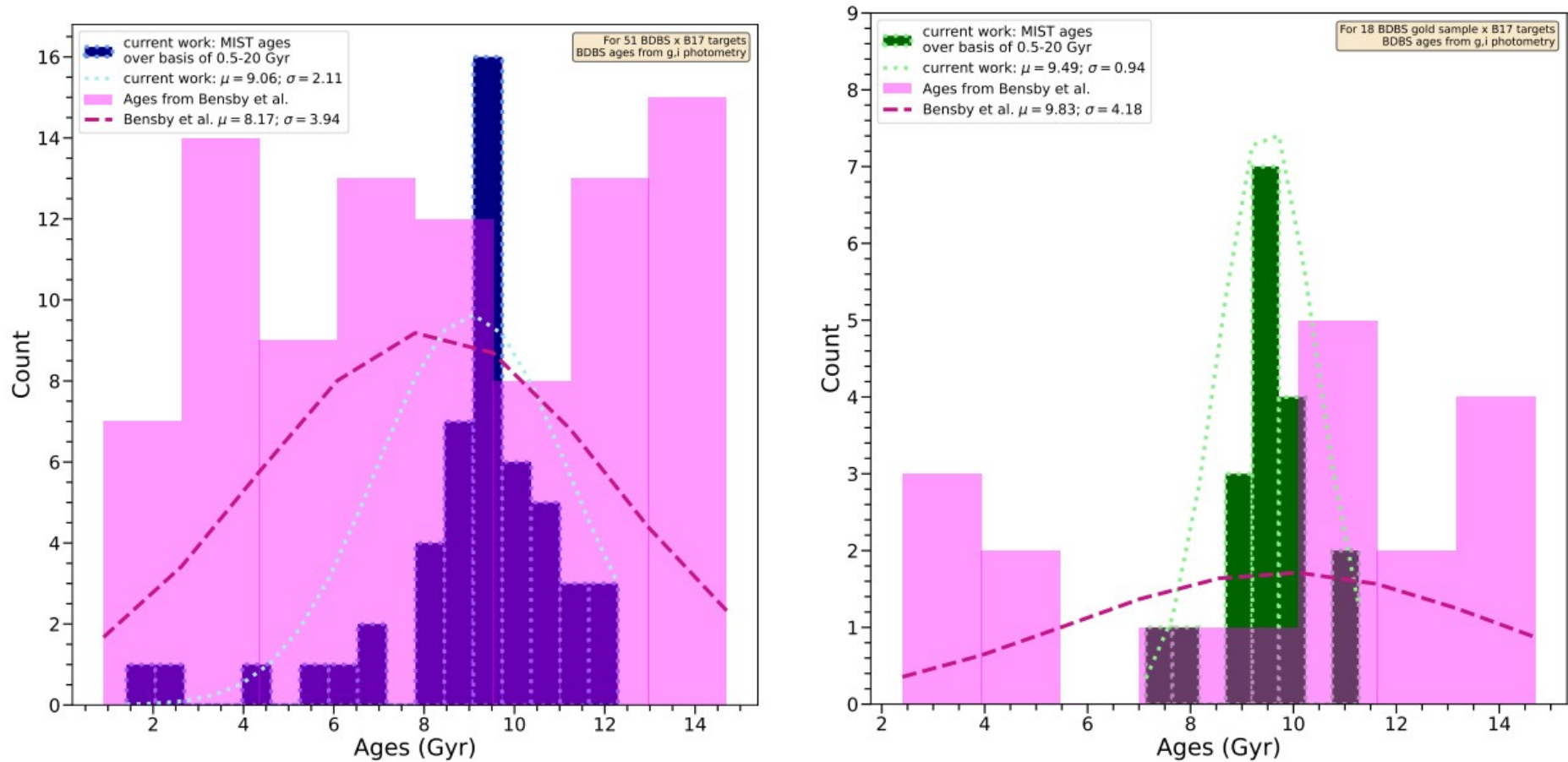
# Attempt to fit BDBS photometry



# Insufficient data resolution?

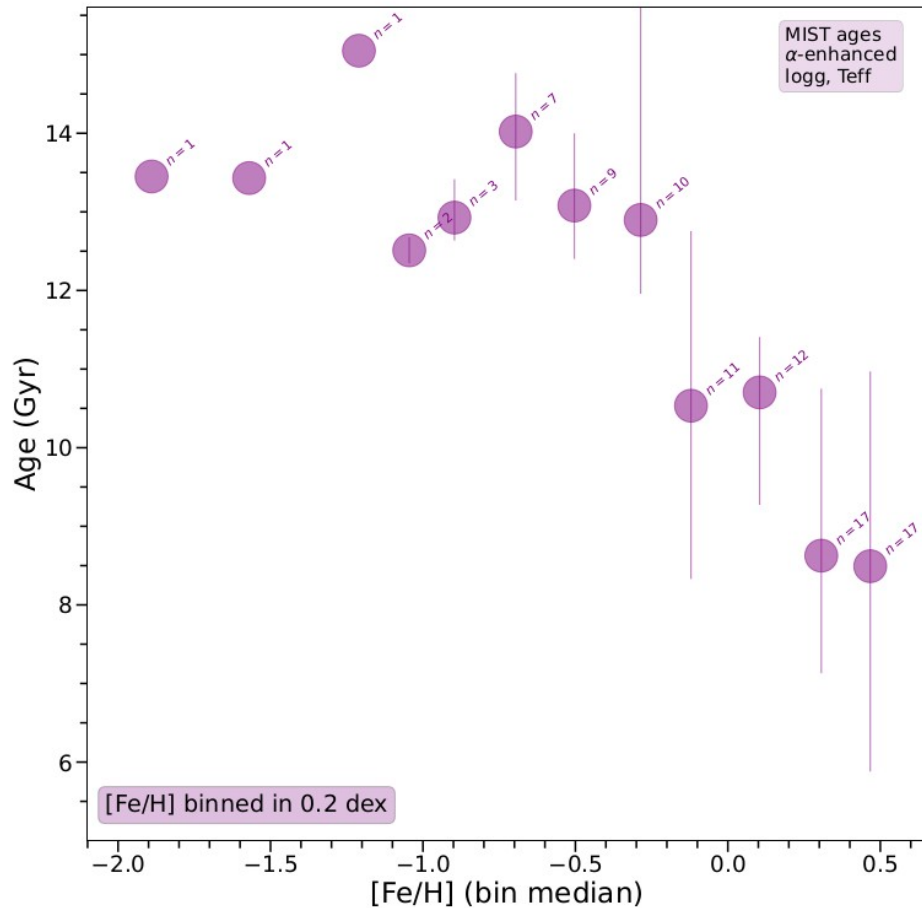
## REALISTIC AGES IN THE BULGE

27

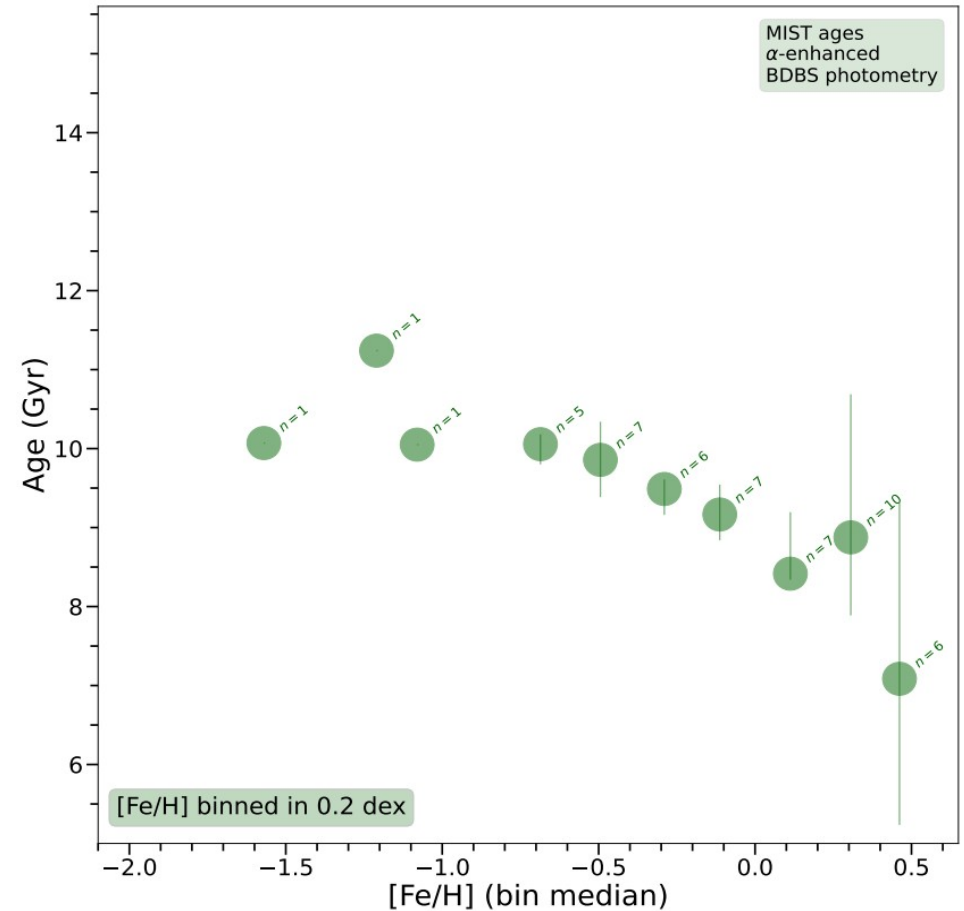


**Figure 14.** Age histograms in the style of Figures 5 and 7 but with ages derived from BDBS photometry. **LEFT:** The full intersection of the B17 and BDBS target lists for which complete photometric and distance information was available, totalling 51. The age distribution according to Bensby et al. (2017) for the same subset of stars is overlaid in pink. **RIGHT:** Same as left panel, but for the gold sample containing 18 members. The ages for the same 18 stars according to B17 is overlaid in pink.

# Spectroscopic vs (poor) photometric



Age-metallicity relation based on re-fitting Bensby et al. spectroscopic data

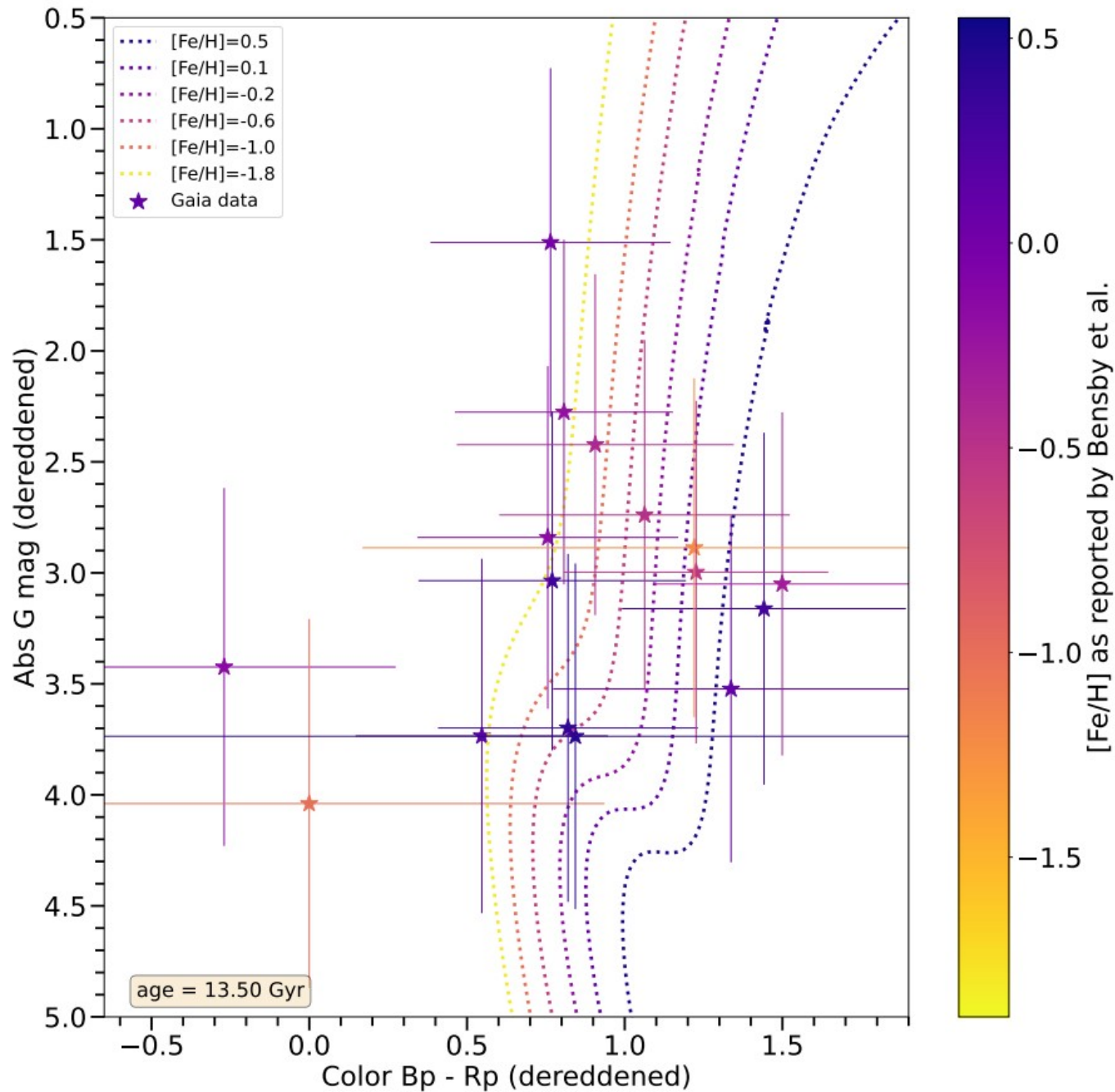


Age-metallicity relation based on subsample with BDBS photometry, using same algorithm

\*Note that BDBS measurements are not precise enough to avoid sensitivity to the set of hypotheses



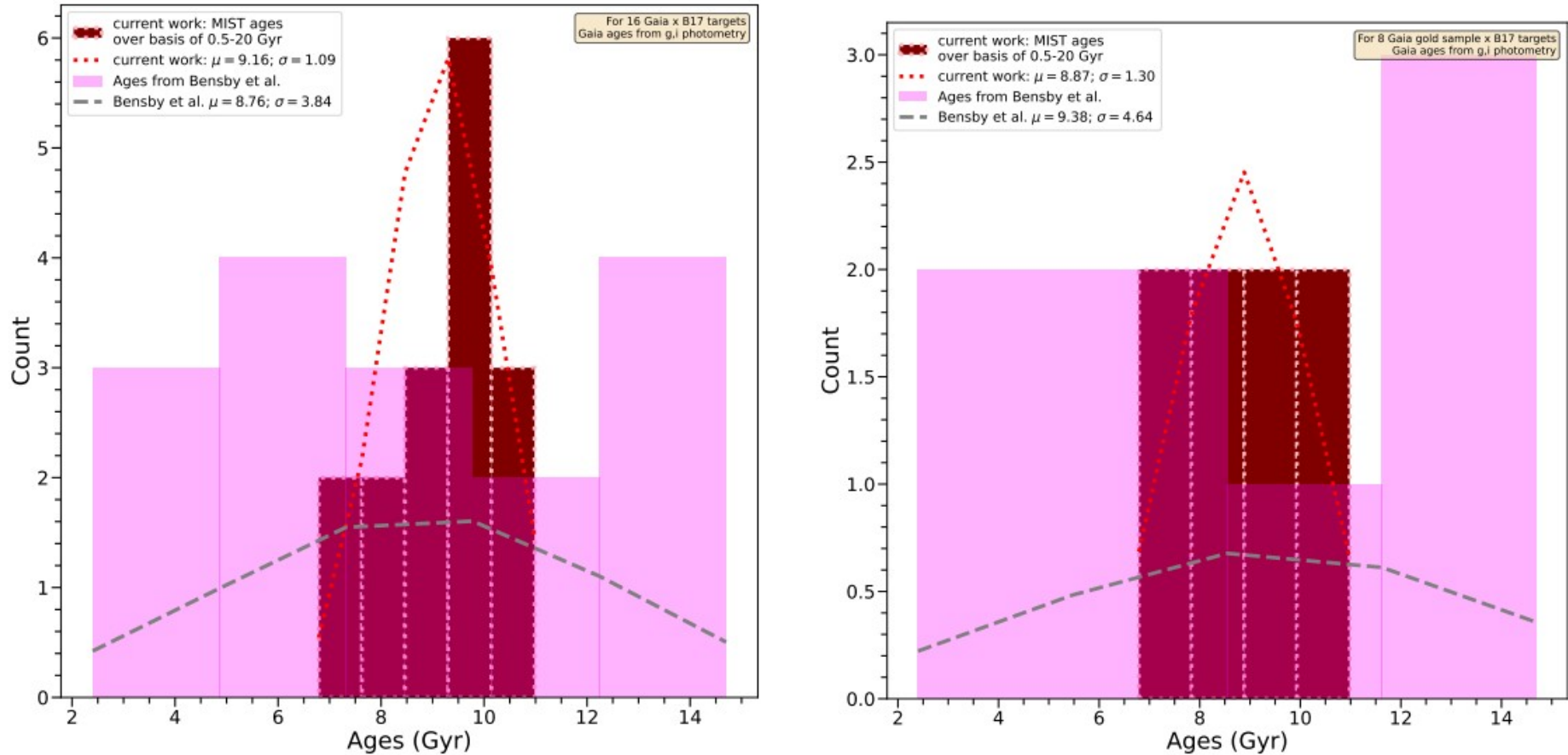
# Attempt to fit *Gaia* photometry



# Clear case of insufficient data resolution

30

JOYCE ET AL.



**Figure 17.** **LEFT:** Same as Figure 14, but for the intersection of the B17 and *Gaia* target lists examining only those stars selected according to the description in Section A.2. This is the “*Gaia* gold sample.” **RIGHT:** Same as left panel, but for the entire intersection of the B17 and *Gaia* target lists. This totals 16 stars after the removal of *Gaia* stars with either (1) bad photometry or (2) for which two independent distance determinations with uncertainties were not available.

# Conclusions

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Bensby+ 2017 (Yale isochrones) find a large population of metal-rich, young stars in the bulge, suggesting prolonged star formation in the region, which is in conflict with previous/other understanding of the formation history of the Galaxy

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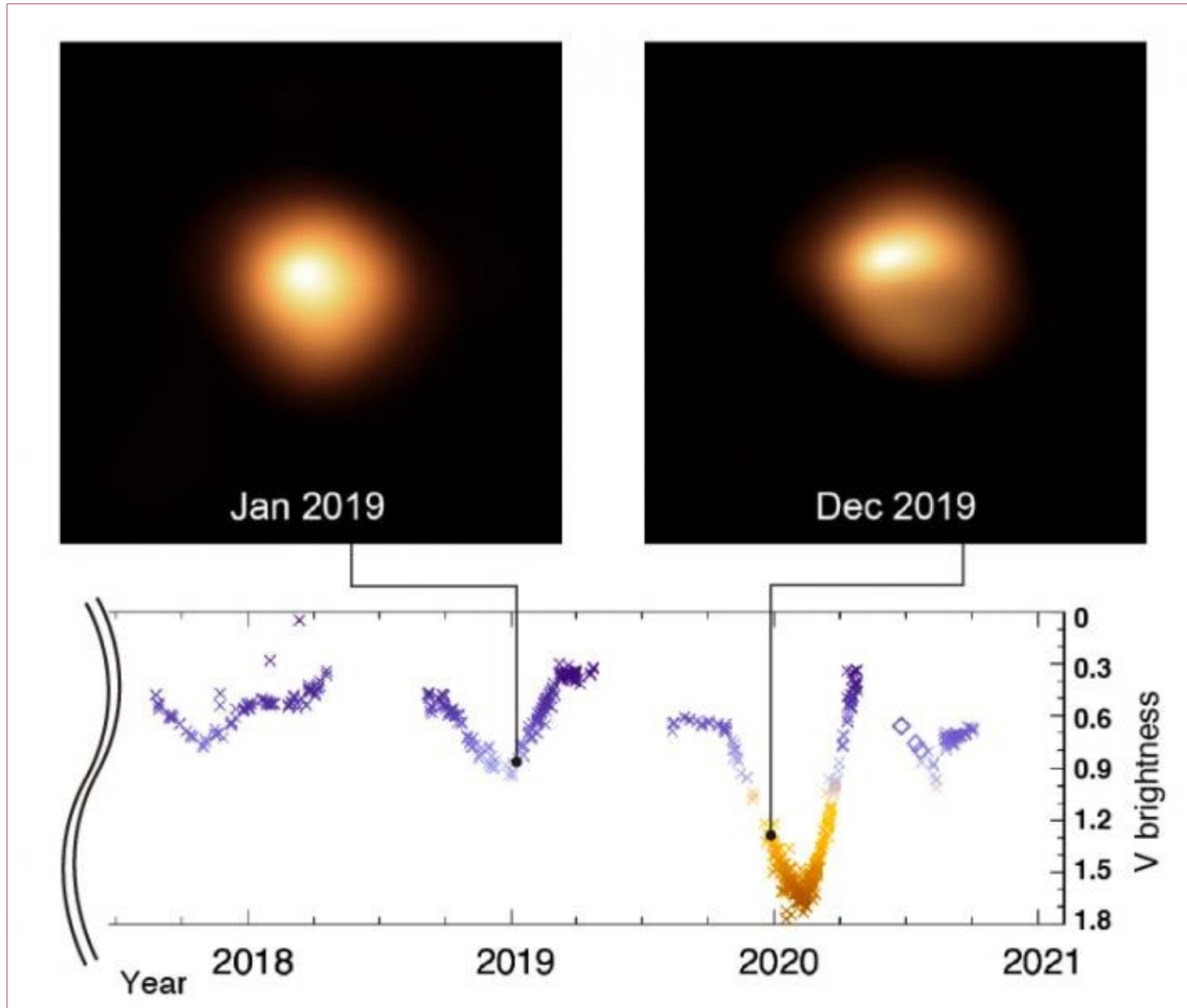
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**Have we resolved the spectroscopic/photometric tension?** Not entirely, but careful application of statistics puts the picture in better focus

Ages are hard! Be careful with math.

**BONUS: Betelgeuse MLT content**

# Late 2019: unprecedented brightness drop



# **Our Approach (one of many):**

**Reproduce this lightcurve via simulation to understand why Betelgeuse became dim or rule out causes**

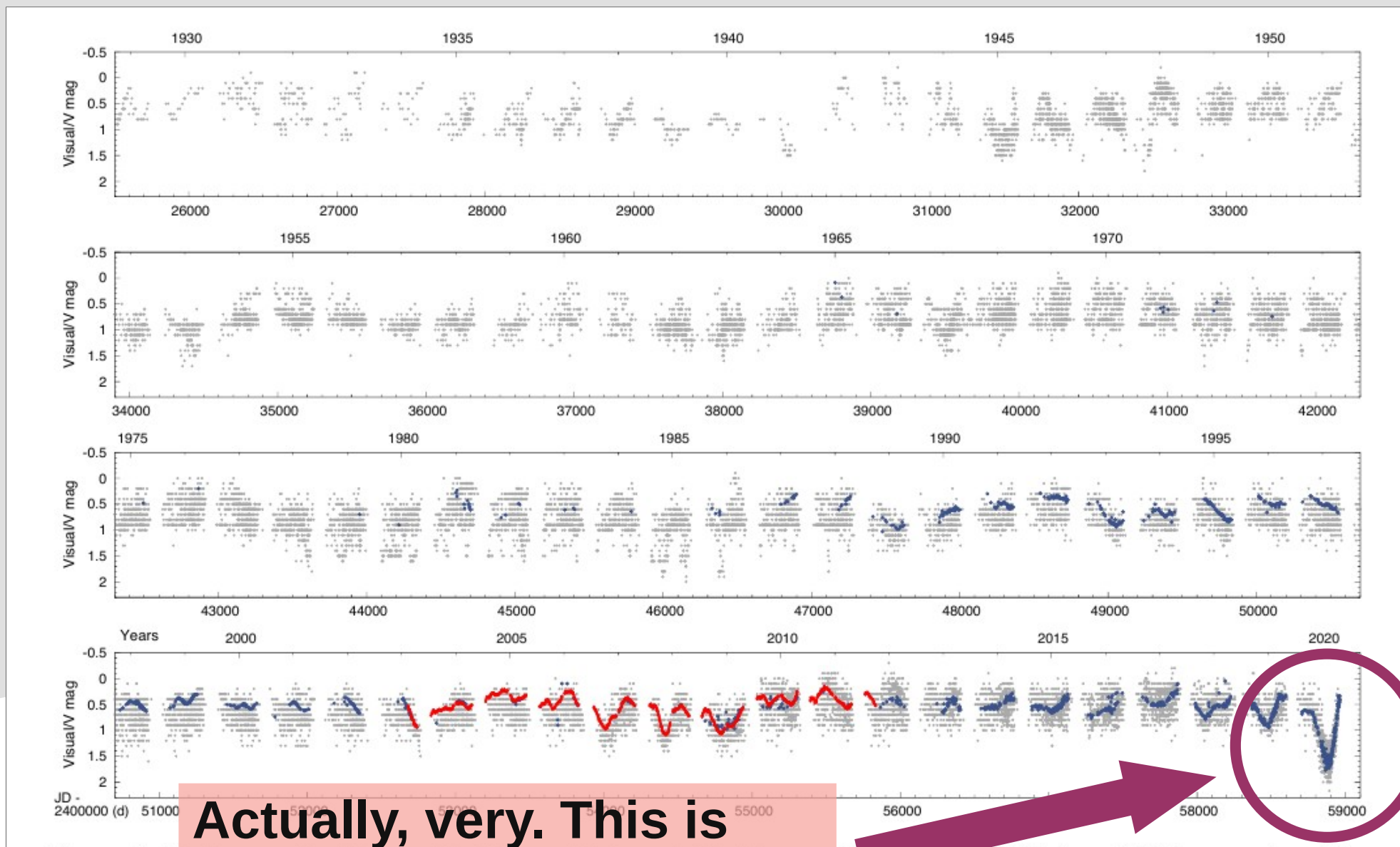
# **Our Approach (one of many):**

**Reproduce this lightcurve via simulation to understand why Betelgeuse became dim or rule out causes**

**...but in order to understand why this dimming event was “unprecedented,” we must first understand Betelgeuse’s normal periodic variations**

# The 'unprecedented' dimming of Betelgeuse

## -First question: How unprecedented, *really*?



**Actually, very. This is the dimmest it's been in nearly 100 years**

# What patterns do we detect in the frequencies?

From new and archival photometry we find periodicities (variabilities):

- 416 days
- 185 days
- 5.6 years

## Determining the drivers of different frequencies tells us about the structure of the star

What we want to know...

Is the 416-day periodicity the fundamental mode?

Is the 185-day periodicity the first overtone?

Is the 416-day period driven by the kappa mechanism?

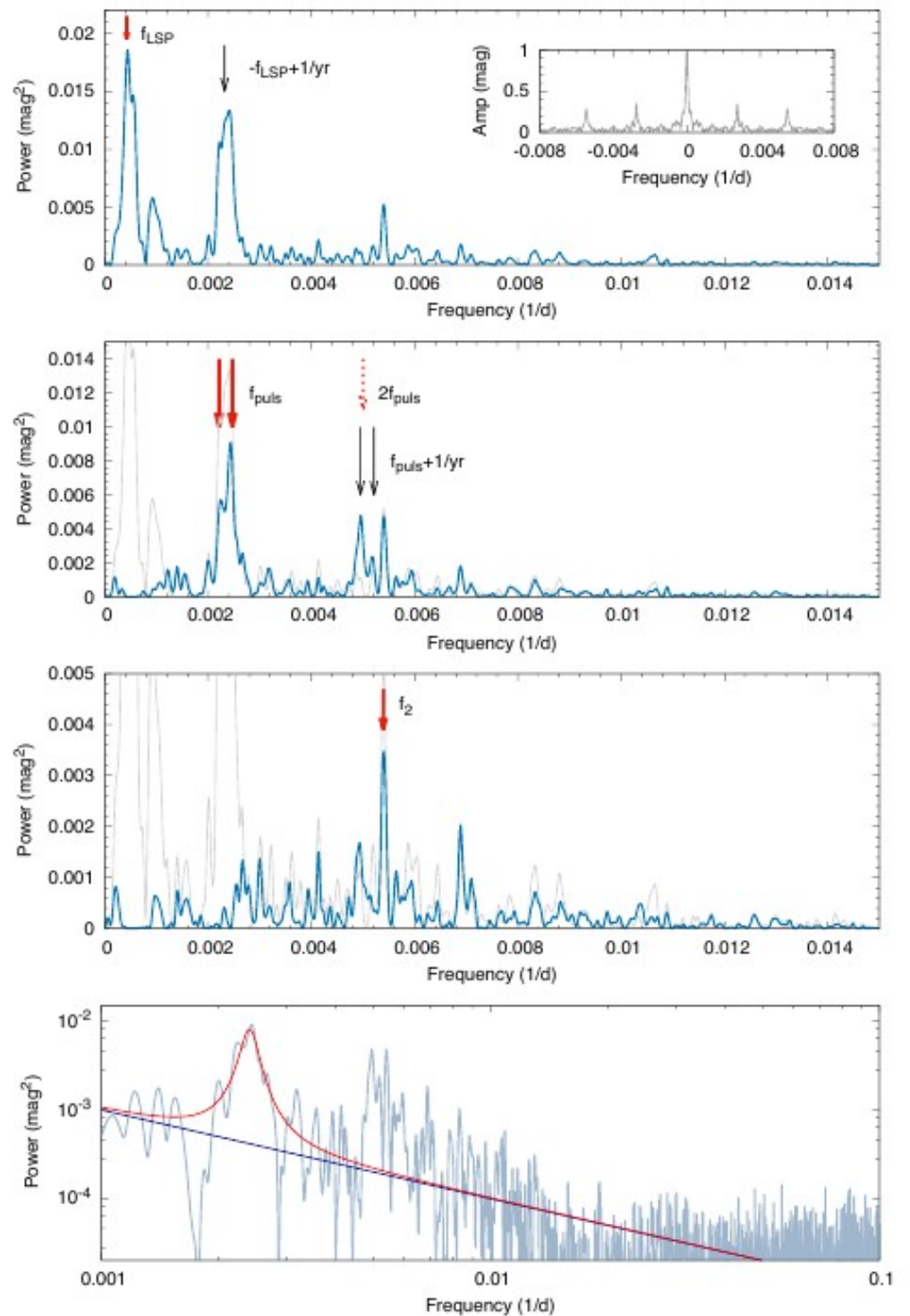
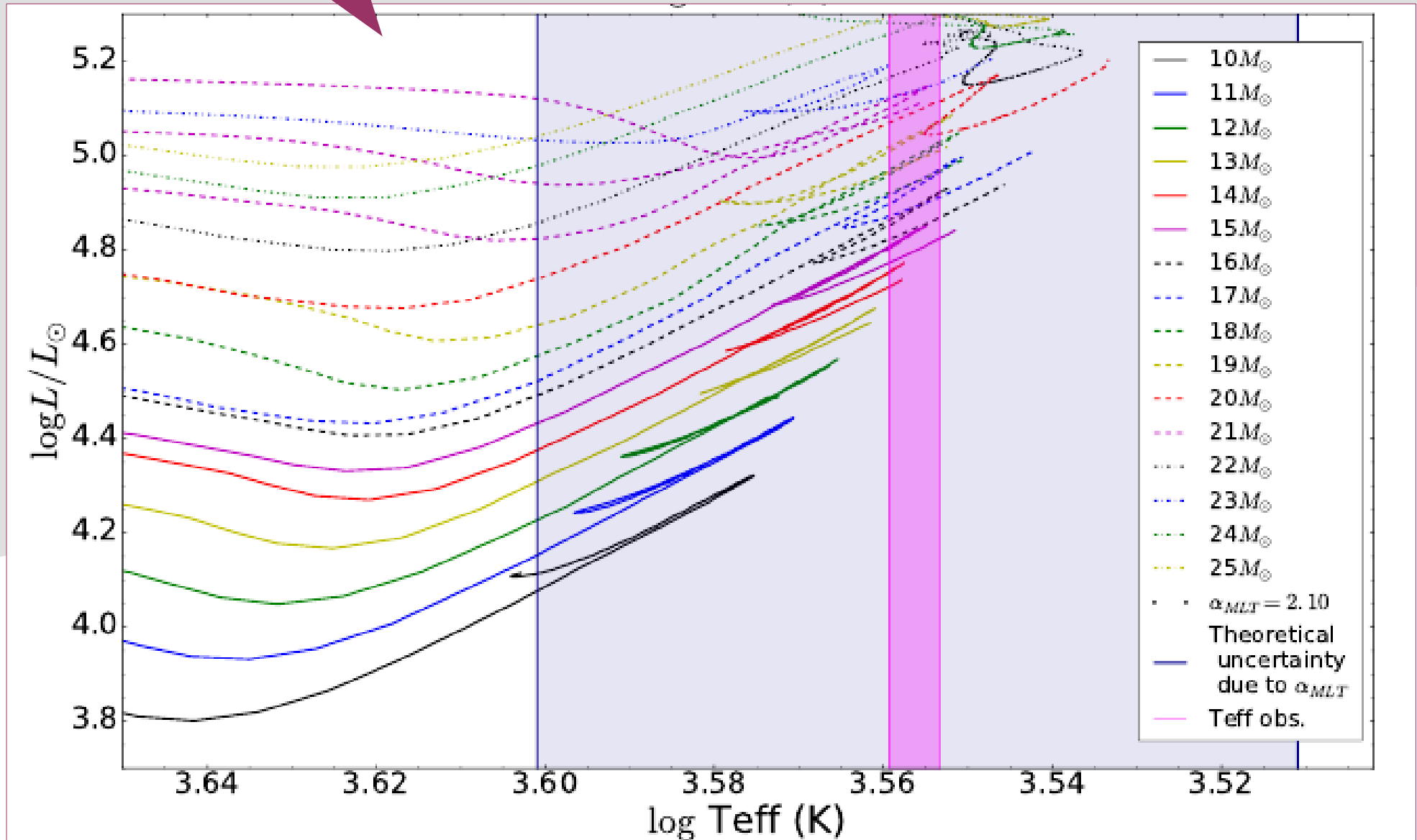
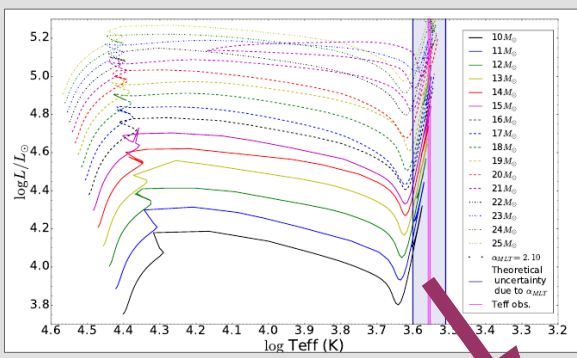
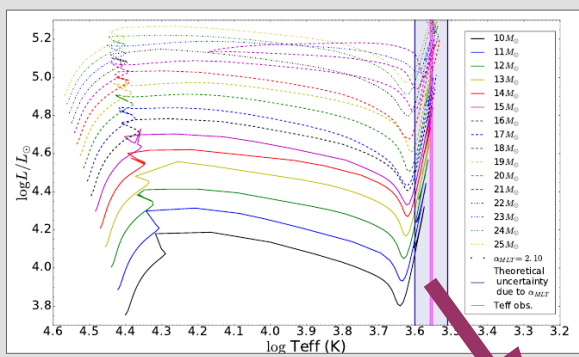


Fig by László Molnár



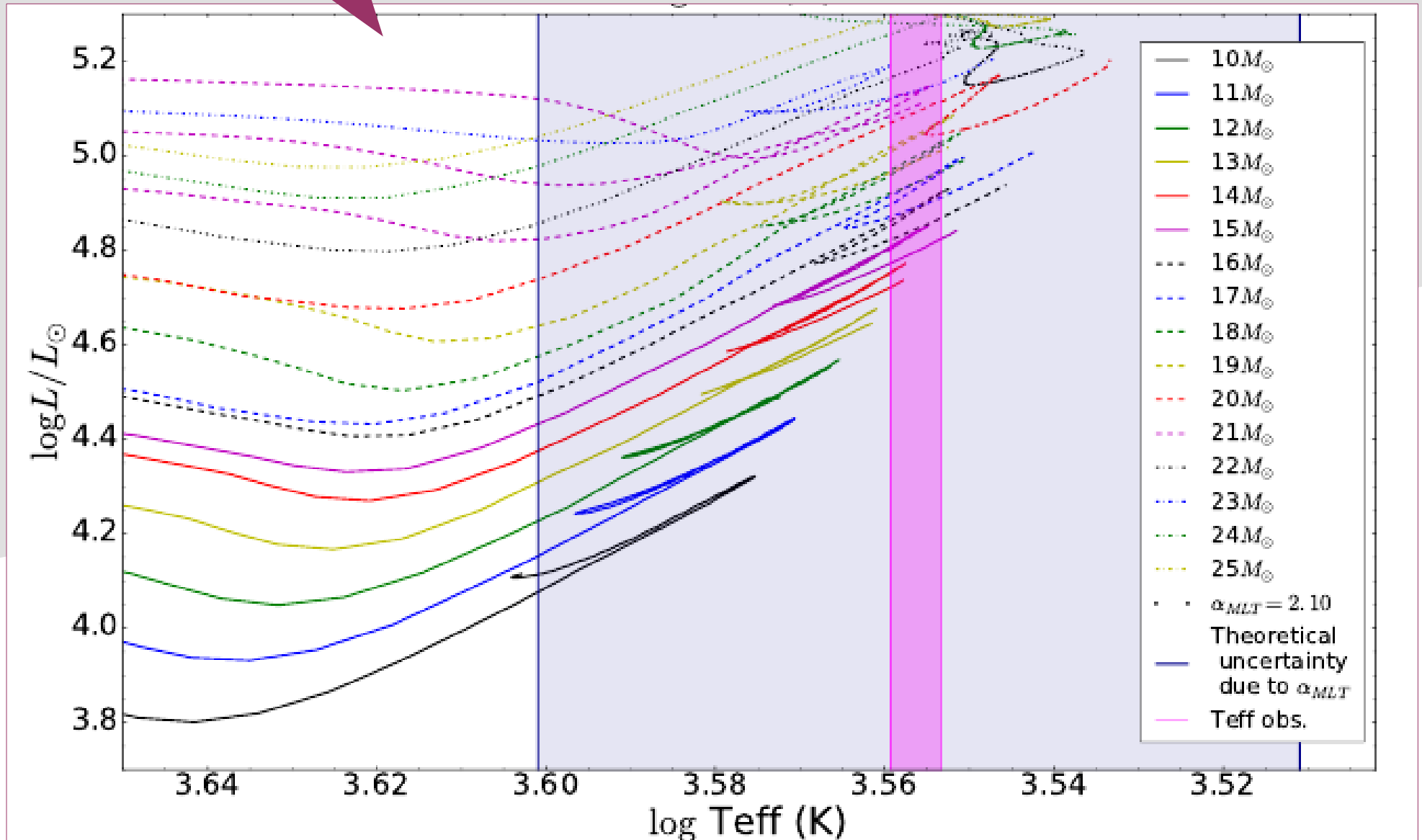
Observations state  $3600 \pm 25$  K, yet we can move an evolutionary track by  $\sim 350$  K just by changing the convective mixing length from  $1.8x$  to  $2.5x$  the pressure scale height



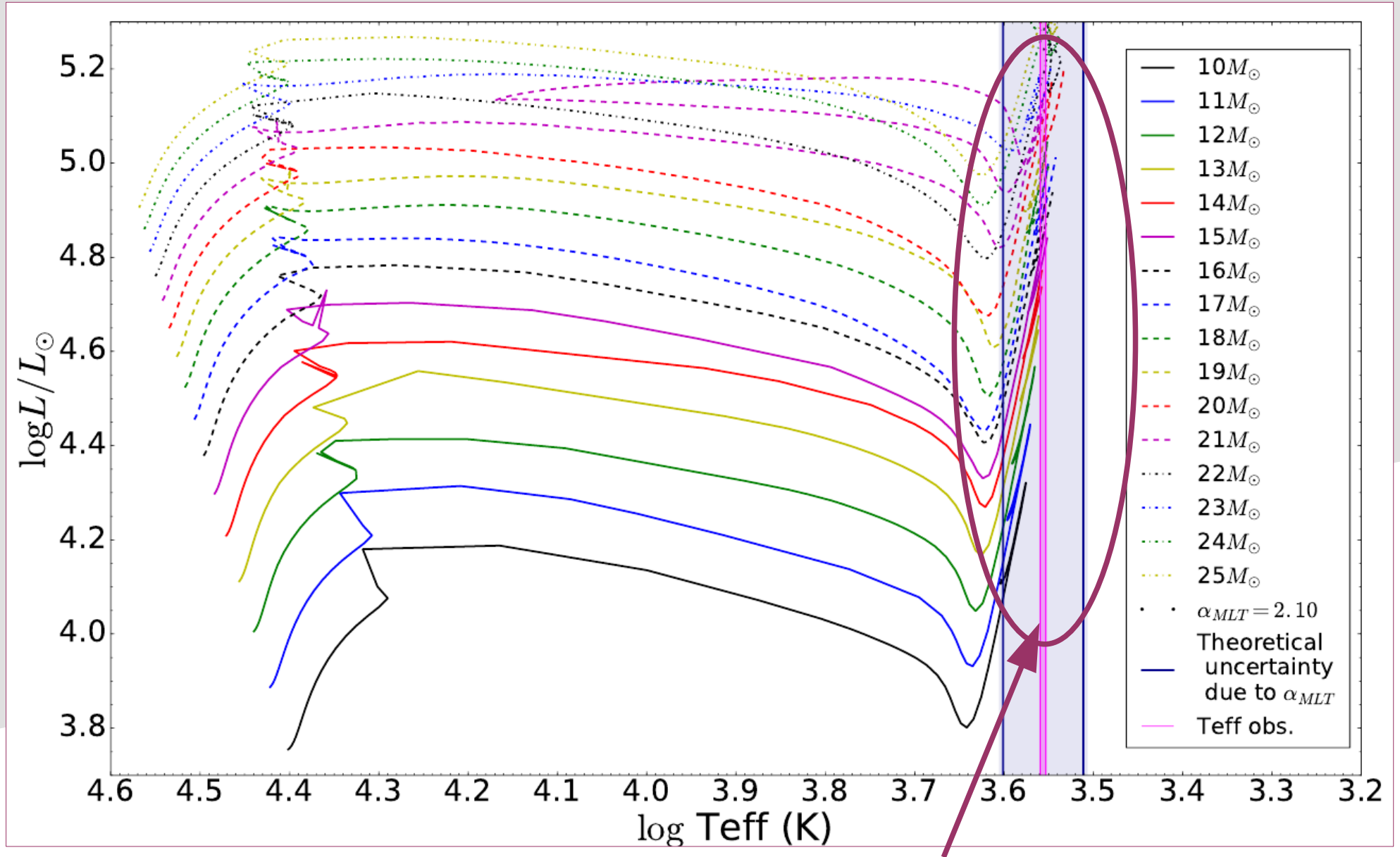


Observations state  $3600 \pm 25$  K, yet we can move an evolutionary track by  $\sim 350$  K just by changing the **convective mixing length** from  $1.8x$  to  $2.5x$  the pressure scale height

→ need to introduce new interpretation of temperature constraints that account for *ad hoc* modeling choices: region in blue

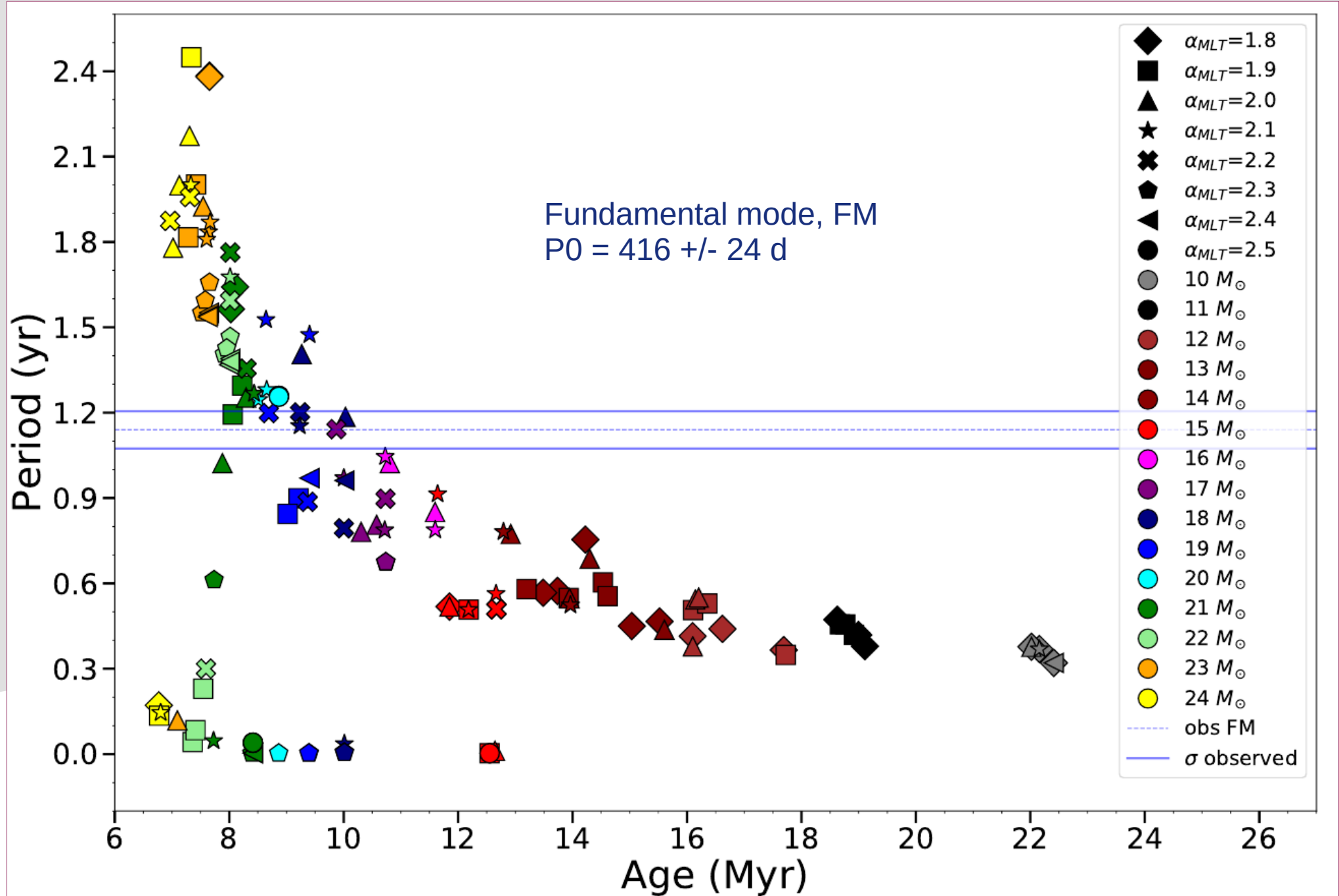


# Add in asteroseismology

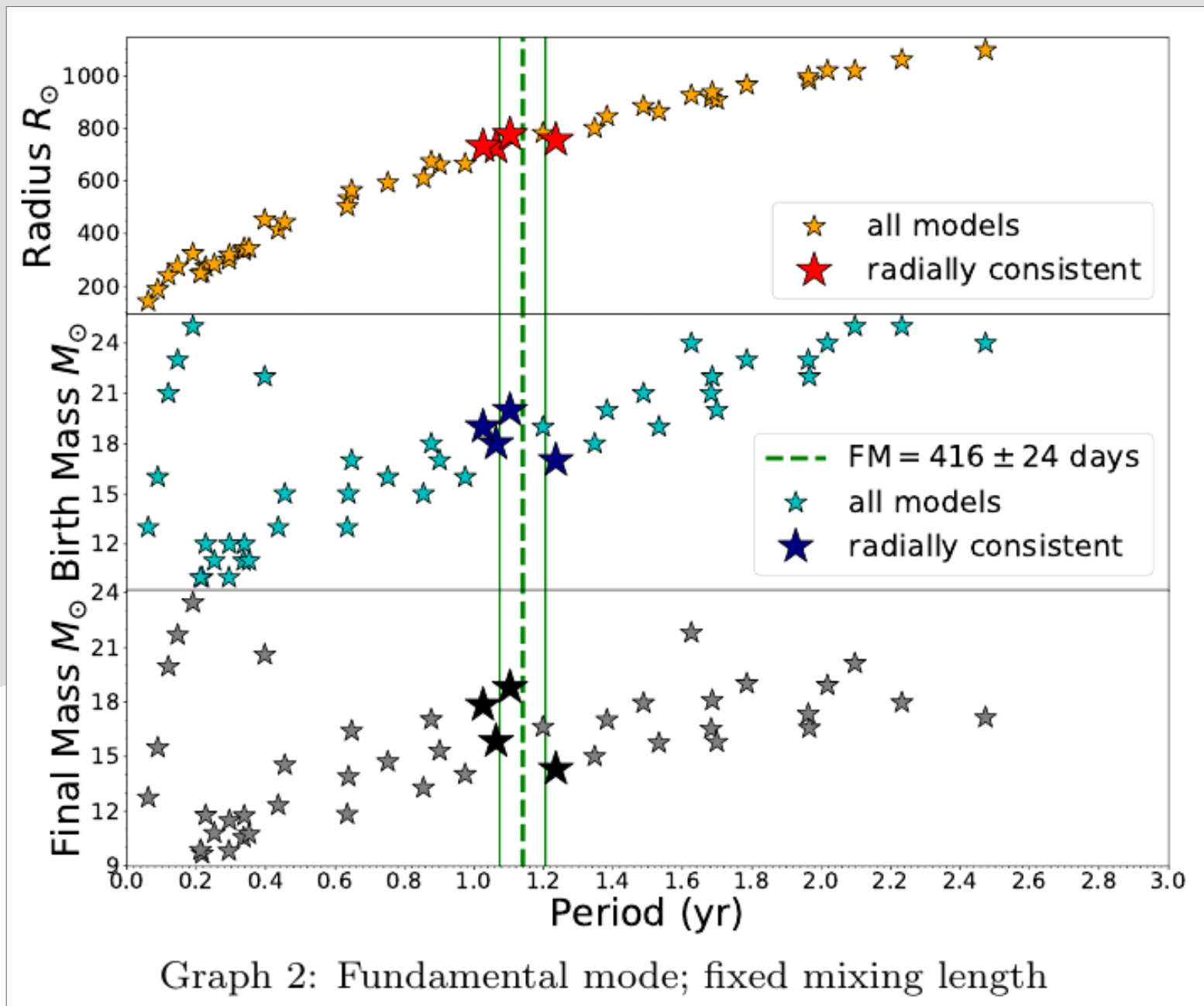


Use GYRE to perform linear seismic analysis on observationally consistent tracks (those which intersect the uncertainty-adjusted Teff constraints)

# Determining which models are seismically compatible



# This method constrains Betelgeuse's physical radius ...even more tightly than the traditional interferometry + parallax method



# Classical & Seismic results:

**General finding:** on the (initial) mass of Betelgeuse, our results are consistent with other modeling efforts; not particularly more precise: 18-24 Msolar

...but our models permit only a **very small range** for the physical radius: a  $3\sigma$  band of 150 Rsolar

In fact, this range is considerably smaller than predictions for the physical radius provided by traditional observational methods (interferometry + parallax)!

## Unanticipated Bonus:

precision modelled radius + measured angular diameter  
= **new parallax distance estimate**



Seismic parallax!!

# Revised distance from seismic parallax

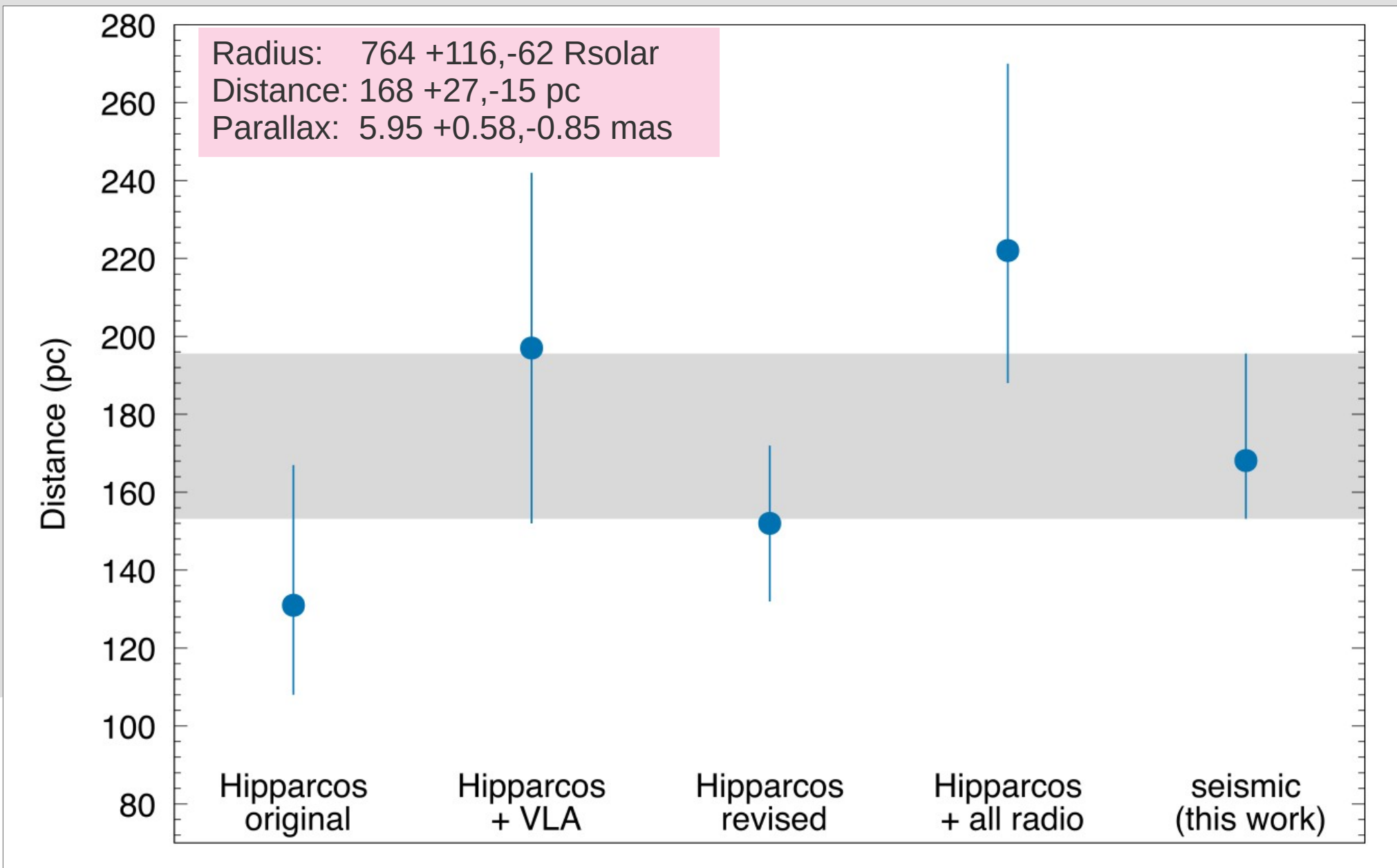


Fig by László Molnár

# Ultra bonus content: you can do statistics for sociology of science, too

## Gender Disparity in Publishing Six Months after the KITP Workshop *Probes of Transport in Stars*

MERIDITH JOYCE <sup>1,2</sup> JAMIE TAYAR <sup>3,2</sup> AND DANIEL LECOANET <sup>4,5,2</sup>

<sup>1</sup>*Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA*

<sup>2</sup>*Kavli Institute for Theoretical Physics, University of California, Santa Barbara, CA 93106, USA\**

<sup>3</sup>*Department of Astronomy, University of Florida, Bryant Space Science Center, Stadium Road, Gainesville, FL 32611, USA*

<sup>4</sup>*Department of Engineering Sciences and Applied Mathematics, Northwestern University, Evanston IL 60208, USA*

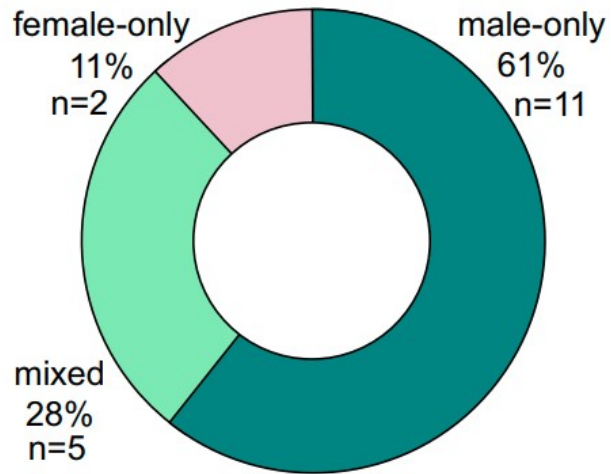
<sup>5</sup>*CIERA, Northwestern University, Evanston IL 60201, USA*

### ABSTRACT

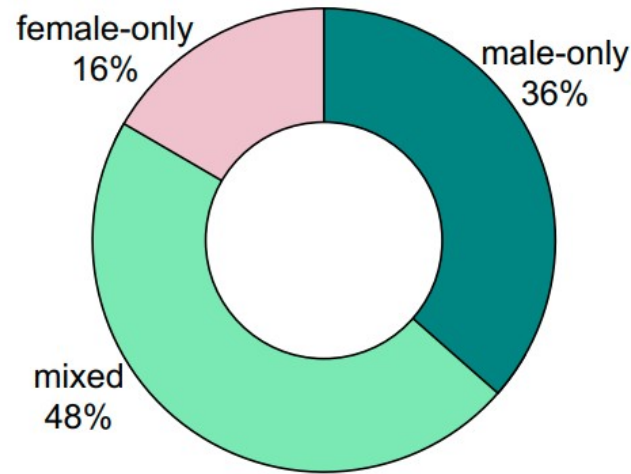
Conferences and workshops shape scientific discourse. The Kavli Institute for Theoretical Physics (KITP) hosts long-term workshops to stimulate scientific collaboration that would not otherwise have taken place. One goal of KITP programs is to increase diversity in the next generation of scientists.



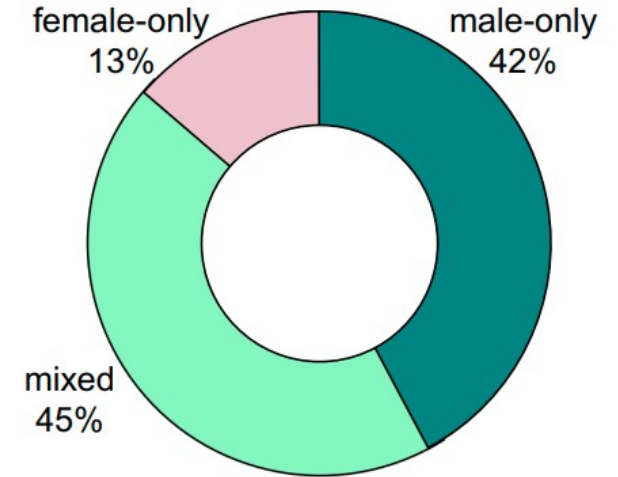
# Ultra bonus content: you can do statistics for sociology of science, too



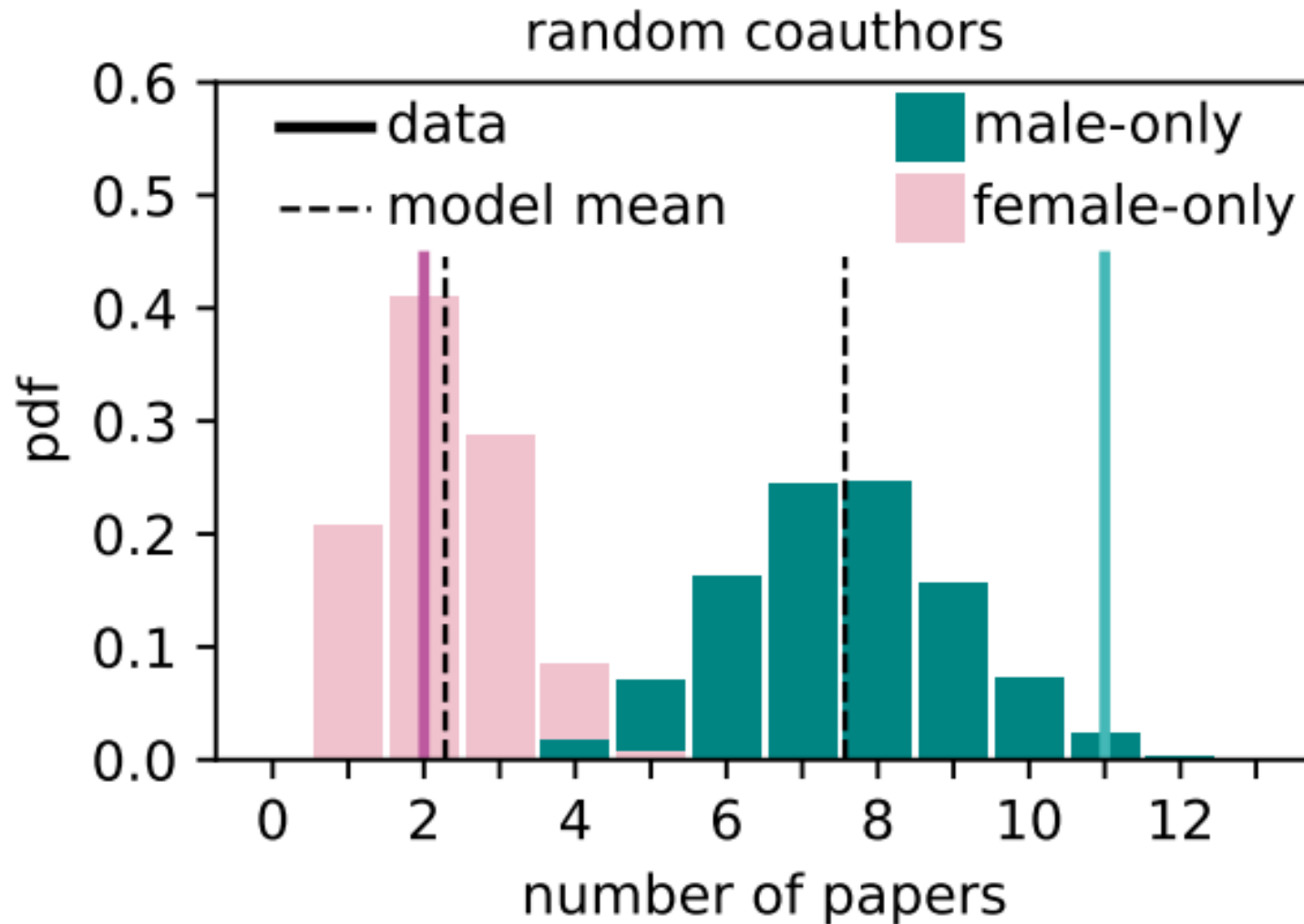
Observed outcome



Predicted by "Random Authors" Model



Predicted by "Random Coauthors" Model



The number of observed all-female\* papers is about the same as predicted by our (most generous) model, whereas the number of observed all-male\* papers is highly outlying ( $p < 0.05$ )

(see paper for detailed discussion of assumptions)

\*genders as reported by participants; “non-binary” and “another not included” options were available

# Fin Tack

$$F_c = \frac{1}{2} \rho v c_D J \frac{\lambda}{H_p} (\nabla_{T^*} - \nabla_{T_{ad}}) \text{ with } \alpha_{mLJ} = \frac{\lambda}{H_p}$$

# Bulge Age Conclusions: reprise

Bensby+ 2017 (Yale isochrones) find a large population of metal-rich, young stars in the bulge, suggesting prolonged star formation in the region, which is in conflict with previous/other understanding of the formation history of the Galaxy

Joyce (me)+ 2022 (MIST isochrones) do not find a large constituency of metal-rich young stars in this region, despite using Bensby+2017's parameters verbatim

There is no significant discrepancy between the physical assumptions adopted between both isochrone databases, nor can differences in alpha-abundance scale explain the striking difference in derived age distributions

Bensby+2017's age distribution is statistically consistent with a uniform distribution across 1 to 15 Gyr, whereas Joyce+2022 finds a clear peak at 13 Gyr and a median of 10.8 Gyr.

While still showing some slight age spread, Joyce+2022 results are **more consistent with photometric analyses of this region** despite being **based on the same spectroscopic, microlensed sample** analyzed in Bensby+2017

**Have we resolved the spectroscopic/photometric tension?** Not entirely, but careful application of statistics puts the picture in better focus

Ages are hard! Be careful with math.