X-rays by Compton Scattering and Sources Driven by SRF Linacs

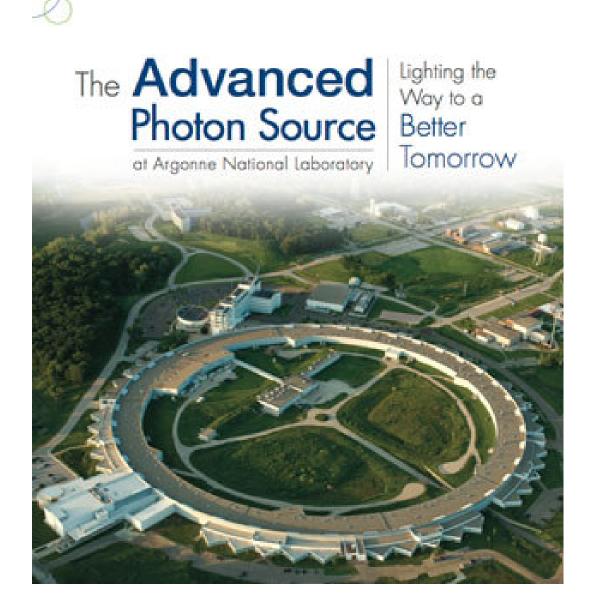
Geoffrey Krafft, Kirsten Deitrick, Jean Delayen, Randika Gamaga, Todd Satogata

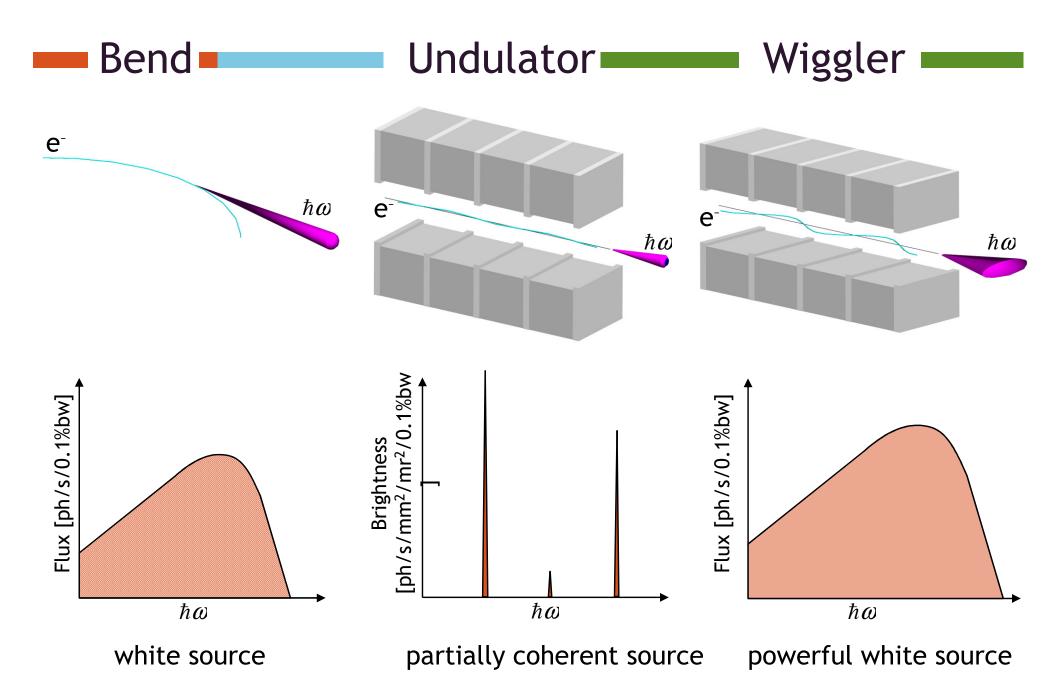
> Center for Accelerator Science Old Dominion University and Jefferson Lab

Outline

- Basic Physics
 - Wigglers, Undulators, and Insertion Devices
 - Compton Effect
 - Important Parameters
 - Line Broadening and Narrowing by Chirping
- Laser Performance
 - Self-Excited Arrangements
 - External High Power Optical Cavities
- SRF Compton Sources
 - New Ideas
 - Layout
 - Results

Argonne Advanced Photon Source







Compton Effect

TABLE I

Wave-length of Primary and Scattered y-rays

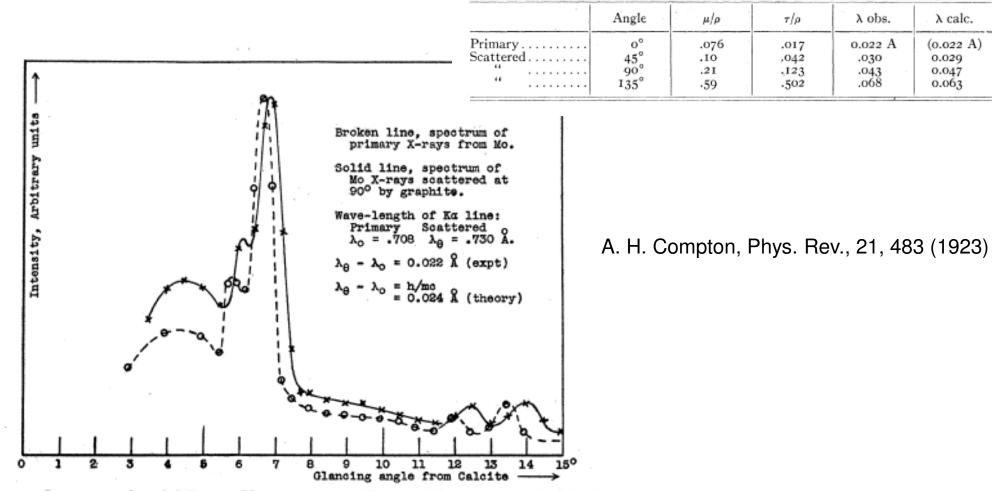


Fig. 4. Spectrum of molybdenum X-rays scattered by graphite, compared with the spectrum of the primary X-rays, showing an increase in wave-length on scattering.

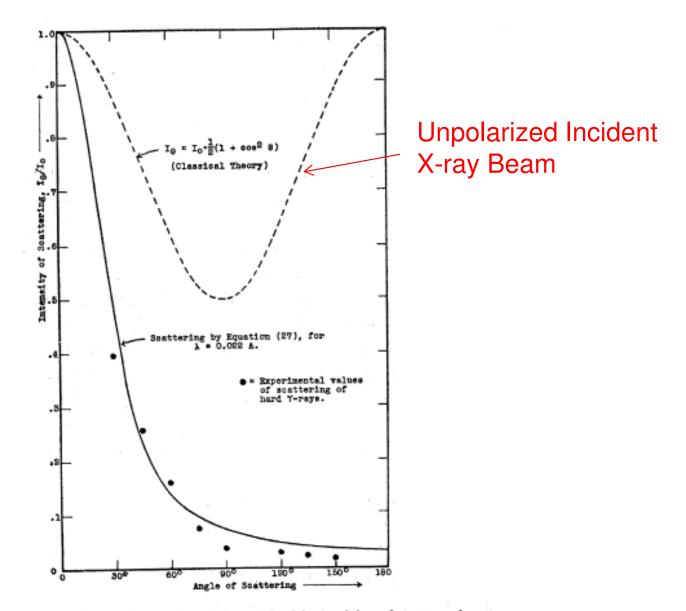
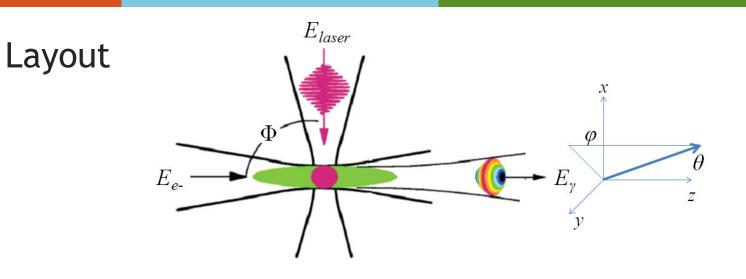


Fig. 7. Comparison of experimental and theoretical intensities of scattered γ-rays.

Scattered Photon Energy



Energy ** $E_{\gamma}(\theta, \varphi) = \frac{E_{\text{laser}}(1 - \beta \cos \Phi)}{1 - \beta \cos \theta + E_{\text{laser}}(1 - \cos \Delta \Theta) / E_{\gamma}}$

- Thomson limit •

**

$$E'_{\text{laser}} \ll mc^2$$
, $E_{\gamma}(\theta, \phi) \approx E_{\text{laser}} \frac{1 - \beta \cos \Phi}{1 - \beta \cos \theta}$

Field Strength Parameter

- Early 1960s: Laser Invented
- Brown and Kibble (1964): Earliest definition of the field strength parameters (normalized vector potential) K and/or a in the literature that I'm aware of

$$a = \frac{eE_0\lambda_0}{2\pi mc^2}$$

Compton/Thomson Sources

 $K = \frac{eB_0\lambda_0}{2\pi mc}$ Undulators

Interpreted frequency shifts that occur at high fields as a "relativistic mass shift".

- Sarachik and Schappert (1970): Power into harmonics at high K and/or a. Full calculation for CW (monochromatic) laser. Later referenced, corrected, and extended by workers in fusion plasma diagnostics.
- Alferov, Bashmakov, and Bessonov (1974): Undulator/Insertion Device theories developed under the assumption of constant field strength. Numerical codes developed to calculate "real" fields in undulators.
- Coisson (1979): Simplified undulator theory, which works at low K and/or a, developed to understand the frequency distribution of "edge" emission, or emission from "short" magnets, i.e., including pulse effects

Emission From a "Short" Magnet

Coisson low-field strength undulator spectrum*

 $\frac{dU_{\gamma}}{dvd\Omega} = \frac{4r_e^2 c}{\mu_0} \gamma^2 \left(1 + \gamma^2 \theta^2\right)^2 f^2 \left|\tilde{B}\left(v\left(1 + \gamma^2 \theta^2\right)/2\gamma^2\right)\right|^2$ $f^2 = f_{\tau}^2 + f_{\tau}^2$ $f_{\sigma} = \frac{1}{\left(1 + \gamma^2 \theta^2\right)^2} \sin \phi$ $f_{\pi} = \frac{1}{\left(1 + \gamma^2 \theta^2\right)^2} \left(\frac{1 - \gamma^2 \theta^2}{1 + \gamma^2 \theta^2}\right) \cos \phi$

 $r_e^2 \equiv \frac{e^4}{16\pi^2 \varepsilon_0^2 m^2 c^4}$

*R. Coisson, Phys. Rev. A **20**, 524 (1979)

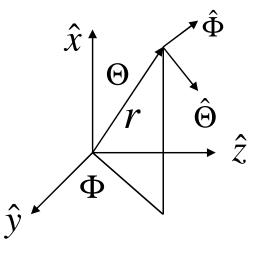
Dipole Radiation

$$\vec{B} = \frac{\mu_0 e\vec{d} (t - r / c)}{4\pi cr} \sin \Theta \hat{\Phi}$$

$$\vec{E} = \frac{\mu_0 e\vec{d} (t - r / c)}{4\pi r} \sin \Theta \hat{\Theta}$$

$$I = \frac{\vec{E} \times \vec{B}}{\mu_0} = \frac{\mu_0}{16\pi^2} \frac{e^2 \vec{d}^2 (t - r/c)}{cr^2} \sin^2 \Theta \hat{r}$$
$$\frac{dP}{d\Omega} = \frac{1}{16\pi^2 \varepsilon_0} \frac{e^2 \vec{d}^2 (t - r/c)}{c^3} \sin^2 \Theta$$

Polarized in the plane containing $\hat{r} = \vec{n}$ and \hat{x}



Define the Fourier Transform

$$\widetilde{d}(\omega) = \int d(t)e^{-i\omega t}dt \qquad \qquad d(t) = \frac{1}{2\pi}\int \widetilde{d}(\omega)e^{i\omega t}d\omega$$

With these conventions Parseval's Theorem is

$$\int d^{2}(t) dt = \frac{1}{2\pi} \int \left| \tilde{d} \right|^{2}(\omega) d\omega$$
$$\frac{dU_{\gamma}}{d\Omega} = \frac{e^{2}}{16\pi^{2}\varepsilon_{0}c^{3}} \int \ddot{d}^{2}(t-r/c) dt = \frac{e^{2}}{32\pi^{3}\varepsilon_{0}c^{3}} \int \omega^{4} \left| \tilde{d} \right|^{2}(\omega) d\omega$$
$$\frac{dU_{\gamma}}{d\omega d\Omega} = \frac{1}{32\pi^{3}\varepsilon_{0}} \frac{e^{2}\omega^{4} \left| \tilde{d}(\omega) \right|^{2}}{c^{3}} \sin^{2}\Theta \qquad \text{Blue Sky!}$$

This equation does not follow the typical (see Jackson) convention that combines both positive and negative frequencies together in a single positive frequency integral. The reason is that we would like to apply Parseval's Theorem easily. By symmetry, the difference is a factor of two.

Weak Field Undulator Emission

$$\begin{split} \tilde{\vec{d}}'(\omega') &= \tilde{d}'(\omega') \hat{x} = -\frac{ec}{mc} \frac{\tilde{B}(\omega'/c\beta_z\gamma)}{\omega'^2} \hat{x} \qquad \tilde{B}(k) = \int B(z) e^{-ikz} dz \\ \frac{dU_{\gamma,\sigma}}{d\omega d\Omega} &= \frac{1}{32\pi^3 \varepsilon_0} \frac{e^4}{m^2 c^3} \frac{\left| \tilde{B}(\omega(1-\beta_z\cos\theta)/c\beta_z) \right|^2}{\gamma^2 (1-\beta_z\cos\theta)^2} \sin^2 \phi \\ \frac{dU_{\gamma,\pi}}{d\omega d\Omega} &= \frac{1}{32\pi^3 \varepsilon_0} \frac{e^4}{m^2 c^3} \frac{\left| \tilde{B}(\omega(1-\beta_z\cos\theta)/c\beta_z) \right|^2}{\gamma^2 (1-\beta_z\cos\theta)^2} \left(\frac{\cos\theta-\beta_z}{1-\beta_z\cos\theta} \right)^2 \cos^2 \phi \\ \lambda &= \frac{\lambda_0}{2\gamma^2} \qquad (1-\beta_z\cos\theta)(1+\beta_z) \approx \frac{1}{\gamma^2} + \theta^2 + \dots \approx \frac{1+\gamma^2\theta^2}{\gamma^2} \end{split}$$

Generalizes Coisson results to arbitrary observation angles

Weak Field Thomson Backscatter

With $\Phi = \pi$ and $a \ll 1$ the result is identical to the weak field undulator result with the replacement of the magnetic field Fourier transform by the electric field Fourier transform

Undulator

Thomson Backscatter

Driving Field
$$c\tilde{B}_{y}(\omega(1-\beta_{z}\cos\theta)/c\beta_{z}) = \tilde{E}_{x}(\omega(1-\beta_{z}\cos\theta)/(c(1+\beta_{z})))$$

Forward Frequency

$$\lambda \approx \frac{\lambda_0}{2\gamma^2}$$

 $\lambda \approx \frac{\lambda_0}{4\nu^2}$

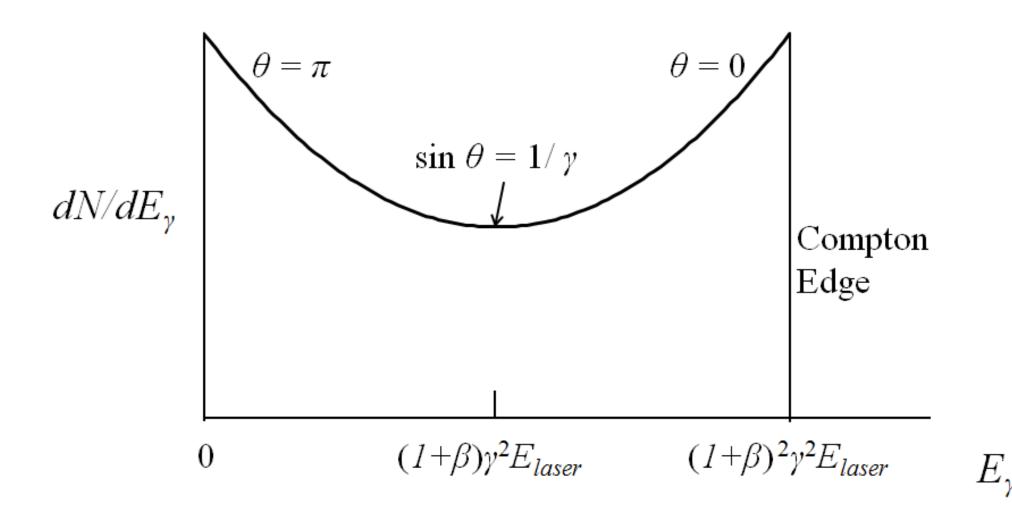
Lorentz contract + Doppler

Double Doppler

Handy Formulas

$$\frac{d^{2}U_{\gamma}}{d\omega d\Omega} = \frac{r_{e}^{2}\varepsilon_{0}}{2\pi c} \left| \tilde{E} \left[\frac{\omega \left(1 - \beta \cos \theta \right)}{c \left(1 + \beta \right)} \right] \right|^{2} \times \frac{\sin^{2} \phi \left(1 - \beta \cos \theta \right)^{2} + \cos^{2} \phi \left(\cos \theta - \beta \right)^{2}}{\gamma^{2} \left(1 - \beta \cos \theta \right)^{2/2}} U_{\gamma} = \gamma^{2} \left(1 + \beta \right) \frac{N_{e} \sigma_{T}}{\left(\sigma_{e}^{2} + \sigma_{laser}^{2} \right)} U_{laser} N_{\gamma} = \sigma_{T} \frac{N_{e} N_{laser}}{2\pi \left(\sigma_{e}^{2} + \sigma_{laser}^{2} \right)} N_{\gamma, \text{per } e} = \frac{2\pi \alpha N_{\lambda} a^{2}}{3}$$

Number Distribution of Photons





• Percentage in 0.1% bandwidth ($\theta = 0$)

$$N_{0.1\%} = 1.5 \times 10^{-3} N_{\gamma}$$

Flux into 0.1% bandwidth

$$F = 1.5 \times 10^{-3} \dot{N}_{\gamma}$$

Flux for high rep rate source

 $F = 1.5 \times 10^{-3} f N_{\gamma}$

Scattered Photon Energy Spread

Source Term	Estimate	Comment
Beam energy spread	$2 \sigma_{_{\!E_{e^-}}}$ / $E_{_{\!e^-}}$	From FEL resonance
Laser pulse width	$\sigma_{_{\! \omega}}$ / ω	Doppler Freq Independent
Finite θ acceptance (full width)	$\gamma^2 \Delta heta^2$	$\theta = 0$ for experiments
Finite beam emittance	$2\gamma^2 arepsilon$ / eta_{e^-}	Beta-function

Spectral Brilliance

In general

$$B = \frac{F}{4\pi^{2}\sigma_{x}\sigma_{x'}\sigma_{y}\sigma_{y'}}$$

$$\approx \frac{F}{4\pi^{2}\sqrt{\beta_{x}\varepsilon_{x}}\sqrt{\varepsilon_{x}/\beta_{x}+\lambda/2L}}\sqrt{\beta_{y}\varepsilon_{y}}\sqrt{\varepsilon_{y}/\beta_{y}+\lambda/2L}}$$

For Compton scattering from a low energy beam

$$\mathsf{B} = \frac{\mathsf{F}}{4\pi^2 \varepsilon_x \varepsilon_y}$$

High a/K

"Figure Eight" Orbits "Figure Eight" Orbits 0.01 -0.00001 -0.000005 0.000005 0.000005 0.00001 -0.01 0.02 -0.03 -0.03 -0.05X

 $\gamma = 100$, distances are normalized by $\lambda_0 / 2\pi$

"Effective" Dipoles

$$D_{t}(\omega;\theta,\varphi) = \frac{1}{\gamma(1-\beta\cos\Phi)} \int \frac{eA(\xi)}{mc} e^{i\phi(\omega,\xi;\theta,\varphi)} d\xi$$
$$D_{p}(\omega;\theta,\varphi) = \frac{1}{\gamma(1-\beta\cos\Phi)} \int \frac{e^{2}A^{2}(\xi)}{2m^{2}c^{2}} e^{i\phi(\omega,\xi;\theta,\varphi)} d\xi$$

And the (Lorentz invariant!) phase is

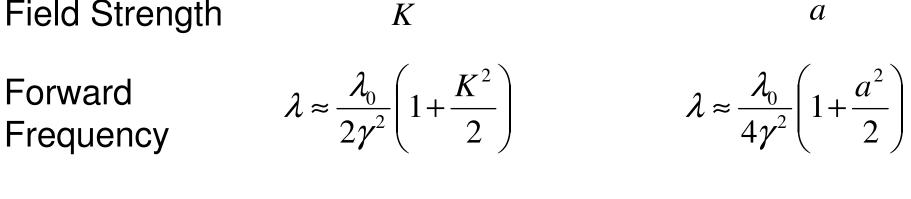
$$\varphi(\omega,\xi;\theta,\phi) = \frac{\omega}{c} \left(\frac{\xi \frac{(1-\beta\cos\theta)}{(1-\beta\cos\Phi)} - \frac{\sin\theta\cos\phi}{\gamma(1-\beta\cos\Phi)} \int_{-\infty}^{\xi} \frac{eA(\xi')}{mc} d\xi'}{\frac{1-\sin\theta\sin\phi\sin\Phi - \cos\theta\cos\Phi}{\gamma^2(1-\beta\cos\Phi)^2} \int_{-\infty}^{\xi} \frac{e^2A^2(\xi')}{2m^2c^2} d\xi'} \right)$$

High Field Backscatter

For a flat incident laser pulse the main results are very similar to those from undulaters with the following correspondences

Undulator

Thomson Backscatter



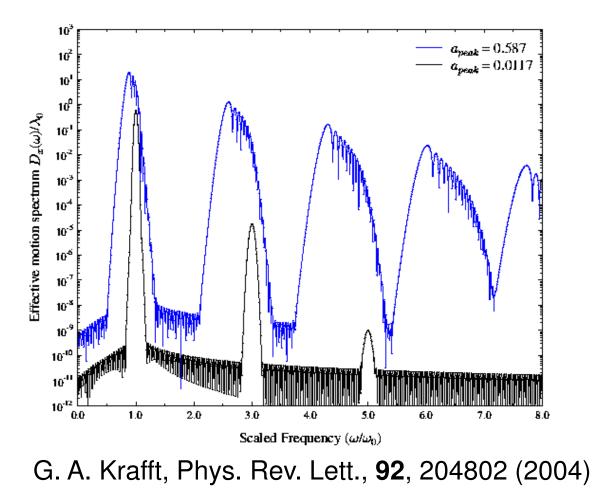
 $1 + \cos \theta'$ Transverse Pattern $\beta *_{z} + \cos \theta'$

NB, be careful with the radiation pattern, it is the same at small angles, but quite a bit different at large angles

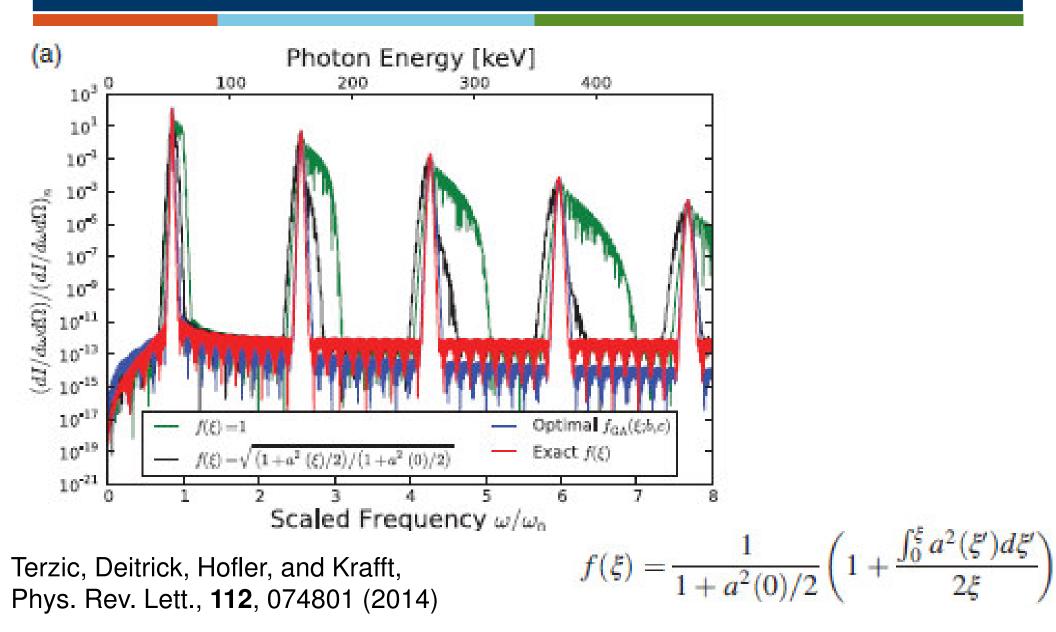
Ponderomotive Broadening

$$A_{x}(\xi) = A_{peak} \exp(-z^{2}/2(8.156\lambda_{0})^{2})\cos(2\pi\xi/\lambda_{0})$$





Compensation By "Chirping"



Beam Illumination Methods

- Direct illumination by laser
 - Earliest method
 - Deployed on storage rings
- Optical cavities
 - Self-excited
 - Externally excited
 - Deployed on rings, linacs, and energy recovered linacs

Early Gamma Ray Source

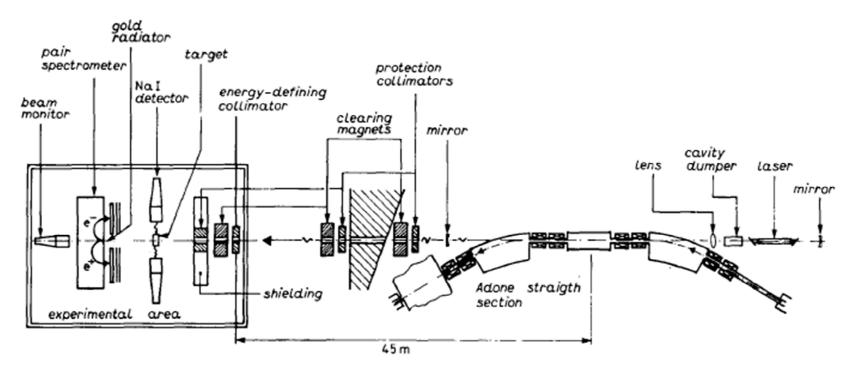
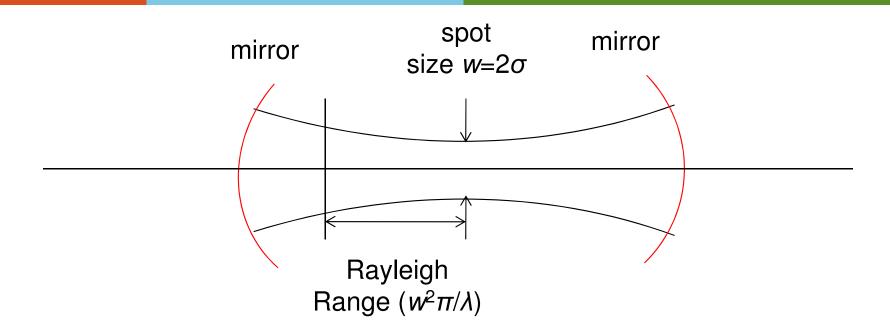


Fig. 1. - Overall view of the experimental set-up.

Compton Edge 78 MeV Federici, *et al.* Nouvo. Cim. B 59, 247 (1980)

Optical Cavities



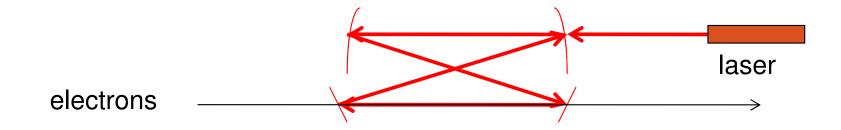
Quantity	Dimensions	
Wavelength	200 nm-10 microns	
Circulating Power	0.1-200 kW	
Spot Size	50-500 microns	
Rayleigh Range	40 cm-5 m	

Self Excited



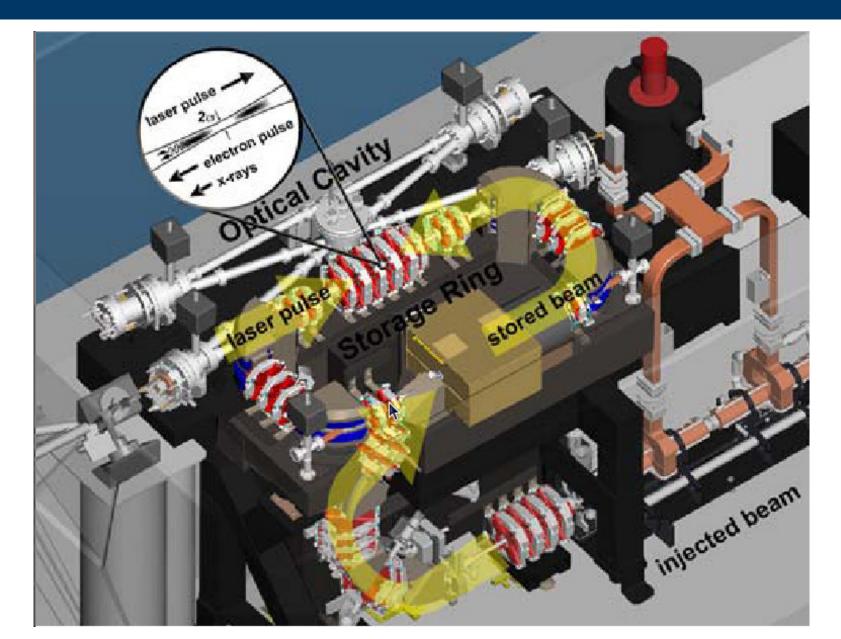
Location	Wavelength	Circulating Power	Spot Size	Rayleigh Range
Orsay	5 microns	100 W	mm	0.7 m
UVSOR	466 nm	20 W	250 microns	0.4 m
Duke Univ.	545 nm	1.6 kW	930 microns	5 m
Super-ACO	300 nm	190 W	440 microns	2 m
Jefferson Lab FEL	1 micron	100 kW	150 microns	1 m

Externally Excited



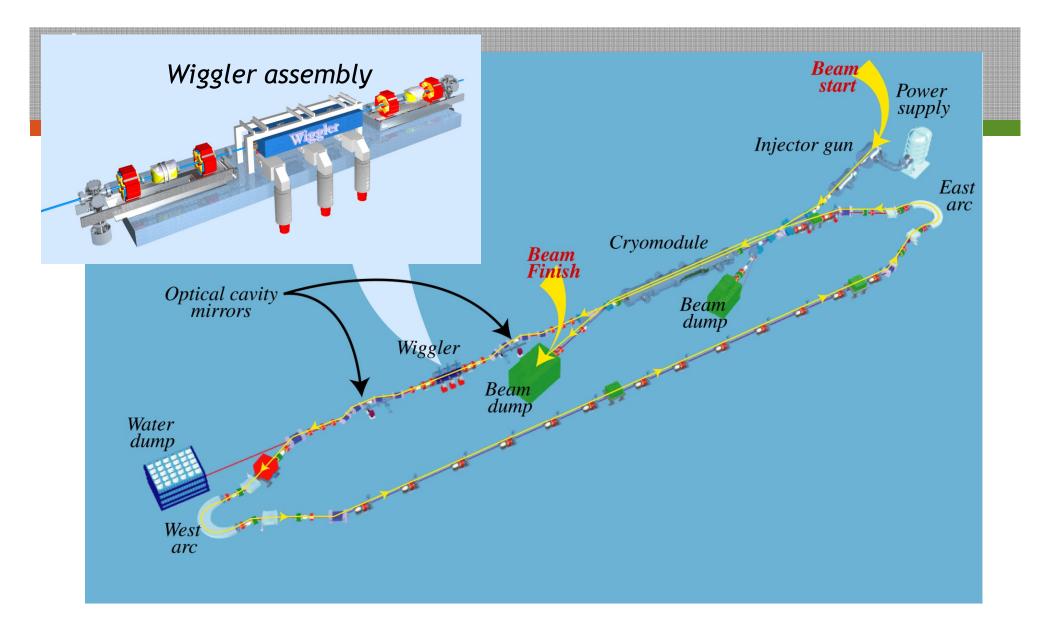
Location	Wavelength	Input Power	Circulating Power	Spot Size (rms)
Jefferson Lab Polarimeter	1064 nm	0.3 W	1.5 kW	120 microns
TERAS	1064 nm	0.5 W	7.5 W	900 microns
Lyncean	1064 nm	7 W	25 kW	60 microns
HERA Polarimeter	1064 nm	0.7 W	2 kW	200 microns
LAL	532 nm	1.0 W	10 kW	40 microns

Lyncean Compact X-ray Source

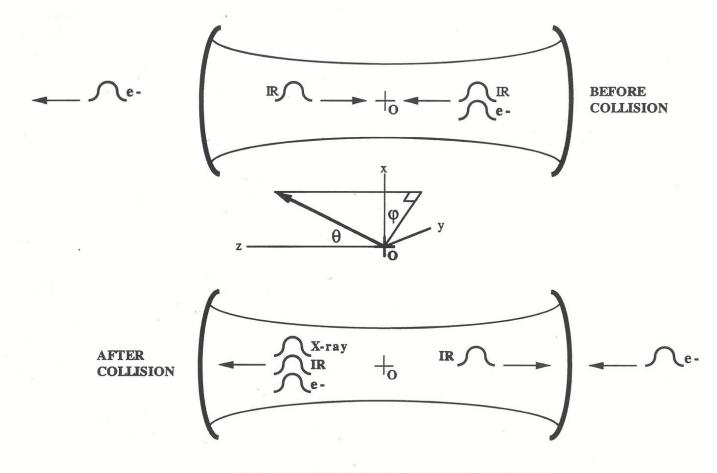


Lyncean Source Performance

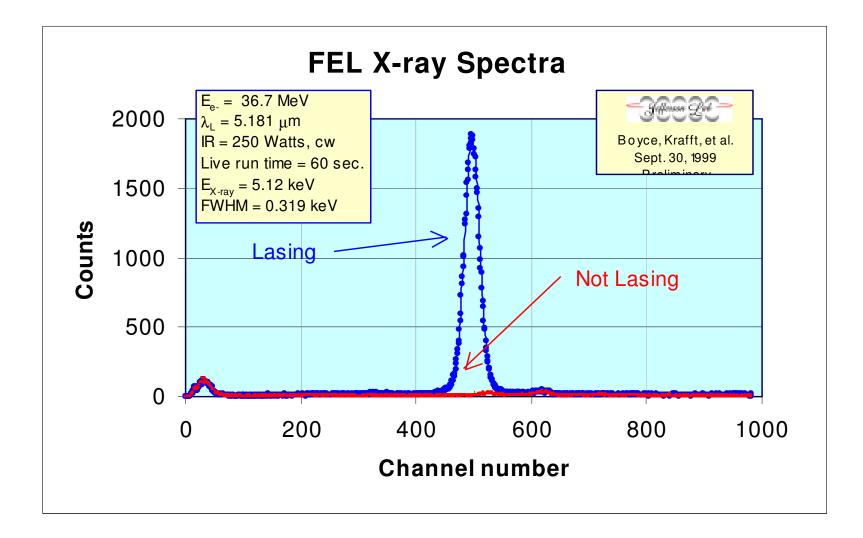
Parmeter	Value	Unit
Photon Energy	10-20	keV
Production Rate	1011	photons/sec
Laser Wavelength	1064	nm
Circulating Power	25	kW
Polarization	100%	
Ultimate Brilliance	5×10 ¹¹	p/(sec mm ² mrad ² 0.1%)



Neil, G. R., et. al, Physical Review Letters, 84, 622 (2000)

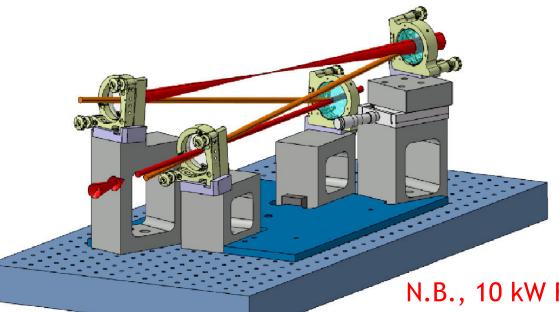


SCATTERING GEOMETRY



Boyce, et al., 17th Int. Conf. Appl. Accel., 325 (2002)

High Power Optical Cavities

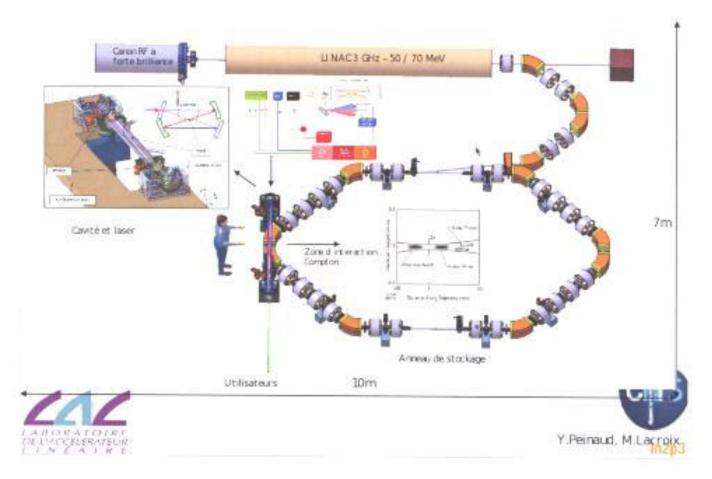


V. Brisson, *et al., NIM A*, **608**, S75 (2009)

N.B., 10 kW FEL there, sans spot!

In this paper we described our first results on the locking of a Ti:sapph oscillator to a high finesse FPC. For the first time, to our knowledge, we demonstrate the possibility of stacking picosecond pulses inside an FPC at a very high repetition rate with a gain of the level of 10000. By studying the stability of four-mirrors resonators, we developed a new promising nonplanar geometry that we have just started to study experimentally. Finally, we mentioned that we shall next use the recent and powerful laser fiber amplification scheme to reach the megawatt average power inside FPC as required by the applications of the Compton X and gamma ray sources.

LAL/Thales THomX



BES Workshop on Compact Light Sources (2010)

Hajima, et al.

Uranium Detection

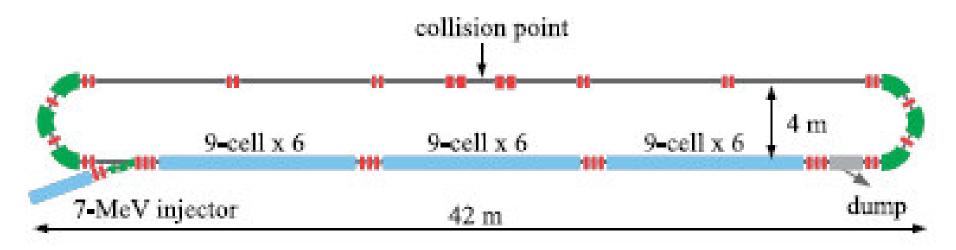
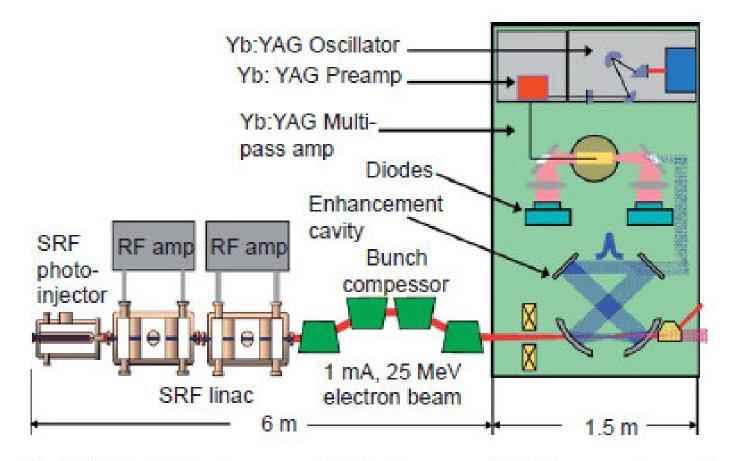
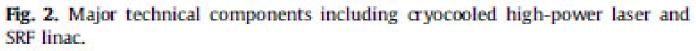


Fig. 3. Layout of the 350-MeV ERL designed for a high-flux γ -ray source. An electron beam generated by the 7-MeV injector is accelerated up to 350 MeV by the main linac and transported to the recirculation loop. The collision point for LCS γ -ray generation is located in the middle of the straight section.

Hajima, *et al., NIM A*, **608**, S57 (2009) TRIUMF Moly Source?

MIT CUBiX





Graves, et al., NIM A, 608, S103 (2009)

Table 1 X-ray parameters.

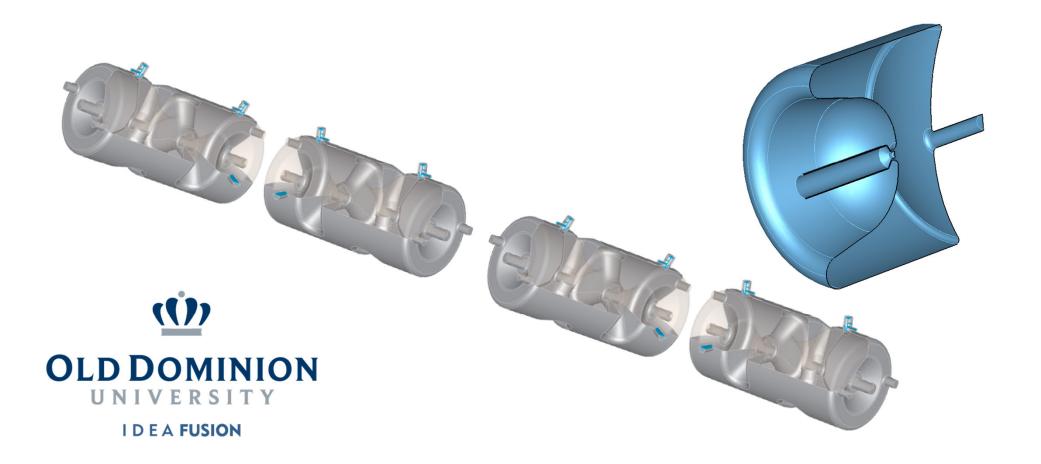
Parameter	Single shot	High flux
Tunable photon energy (keV)	3-30	
Pulse length (ps)	2	0.1
Flux per shot (photons)	1×10^{10}	3×10^{6}
Repetition rate (Hz)	10	10 ⁸
Average flux (photons/s)	1×10^{11}	3×10^{14}
On-axis bandwidth (%)	2	1
RMS divergence (mrad)	5	1
Source RMS size (mm)	0.006	0.002
Peak brilliance (photons/(smm ² mrad ² 0.1%bw))	6×10^{22}	6×10^{19}
Average brilliance (photons/(s mm ² mrad ² 0.1%bw))	6×10^{11}	2×10^{15}

numerical simulation results assuming parameters of E = 25 MeV, $\varepsilon_{nx} = 0.1 \,\mu\text{m}, \ x_e = 2 \,\mu\text{m}, \ \Delta t_L = 0.3 \text{ ps}, \ \lambda = 1 \,\mu\text{m}, \ Q_e = 10 \text{ pc}, \text{ and} W_{\gamma} = 10 \text{ mJ}.$ Note that no nonlinear effects were included in this



ODU Compton Light Source

01 June 2015





Parameters

Parameter	Quantity	Units
Energy	25	MeV
Bunch charge	10	рС
Repetition rate	100	MHz
Average current	1	mA
Trans. norm. emittance	0.1	mm-mrad
B _{x,y}	5	mm
FWHM bunch length	3.0 (0.9)	psec (mm)
RMS energy spread	7.5	keV

Electron beam parameters at collision point.



Parameters

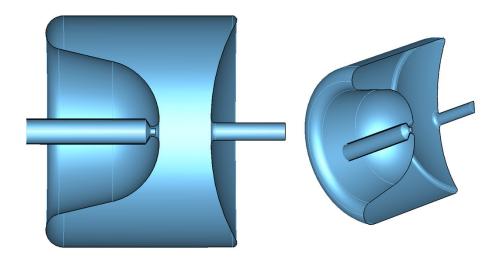
Parameter	Quantity	Units
Wavelength	1 (1.24)	µm (eV)
Circulating power	1	MW
Number of photons/bunch	5 x 10 ¹⁶	
Spot size	3.2	μm
Peak strength	0.026	
X-ray energy	Up to 12	keV
Photons/bunch	1.6 x 10 ⁶	
Flux	1.6 x 10 ¹⁴	photon/sec
Avg. brilliance	1.6 x 10 ¹⁵	photon/(sec-mm ² - mrad ² -0.1%BW)

Optical cavity parameters.

Compton source parameters.



Electron gun



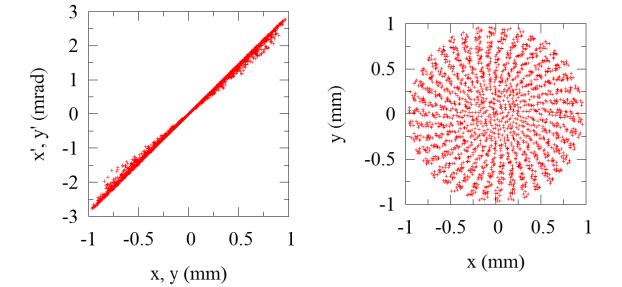
- Originally based on quarter-wave
 SRF electron gun developed by
 Harris *et al*.
- Highly reentrant to mitigate growth of normalized emittance due to space charge.

Parameter	Quantity	Units
Freq. of accele- rating mode	499.3	MHz
λ/4	150	mm
Design B	0.95	
Stored energy	44	mJ
QR _S	83.5	Ω
R/Q	154	Ω
Peak electric surface field (E_P)	3.67	MV/m
Peak magnetic surface field (<i>B_P</i>)	6.64	mT
E_P/B_P	1.81	mT/(MV/m)

RF Properties at $E_{acc} = 1 \text{ MV/m}$

Electron gun

- EM fields calculated by SUPERFISH
- Particle tracking simulated by ASTRA
- Diameter/length 30 cm
- ✤ Beam travels 15 cm



- Top: Transverse phase space and spot. Bottom: Electron beam
 - properties at gun exit.

Parameter	Quantity	Units
E _{kin}	1.55	MeV
RMS Energy spread	0.526	keV
σ _{x,y}	0.477	mm
Normalized RMS $\boldsymbol{\epsilon}_{x,y}$	0.12	mm-mrad







- Consists of 4 high-velocity, double-spoke cavities.
- Alternating orientation to produce roundest beam at exit.
- ✤ 500 MHz
- Diameter of 41.6 cm
- ✤ Length of 80.5 cm

- EM fields calculated by CST Microwave Studio.
- Particle tracking simulated by ASTRA.
- Entire accelerating section has
 5 m x 1 m footprint

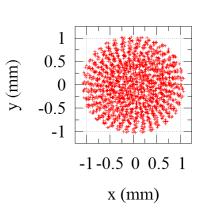




Parameter	Quantity	Units	0.08 0.06 - 0.04
Energy	25.02	MeV	
RMS Energy spread	31.09	keV	-∞ -0.02 -0.04
σ _z	2.1 (7.0)	mm (psec)	-0.06
σ _{x,y}	0.511, 0.482	mm	
Norm. RMS $\epsilon_{x,y}$	0.16, 0.15	mm-mrad	
a _{x,y}	2.34, -0.591		
B _{x,y}	82.7, 75.5	m	

Transverse phase spaces are bowties, not ellipses.

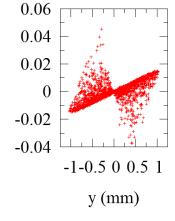
Top: Electron beam properties at linac exit. Bottom: Transverse phase spaces and beam spot.



-1-0.5 0 0.5 1

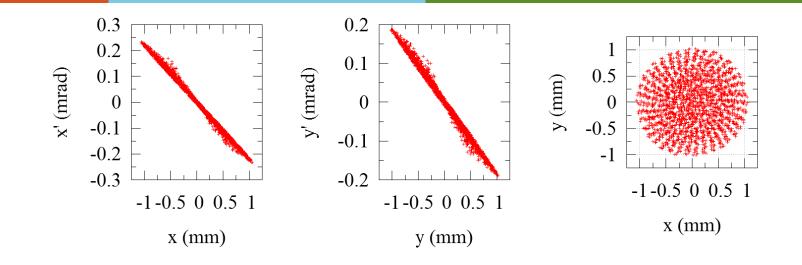
x (mm)

y' (mrad)





Matching



- Solenoid transforms bowties into phase spaces.
- ↔ Normalized RMS $\epsilon_{x,y}$: 0.16, 0.15 → 0.19, 0.18 mm-mrad.
- ✤ As solenoid strength increases, so does emittance growth.
- Followed by a quadrupole and skew quadrupole, to get α_x = α_y and to remove x'y' coupling, respectively.
- ✤ ~1 m in length.
- ✤ Modeled by elegant.

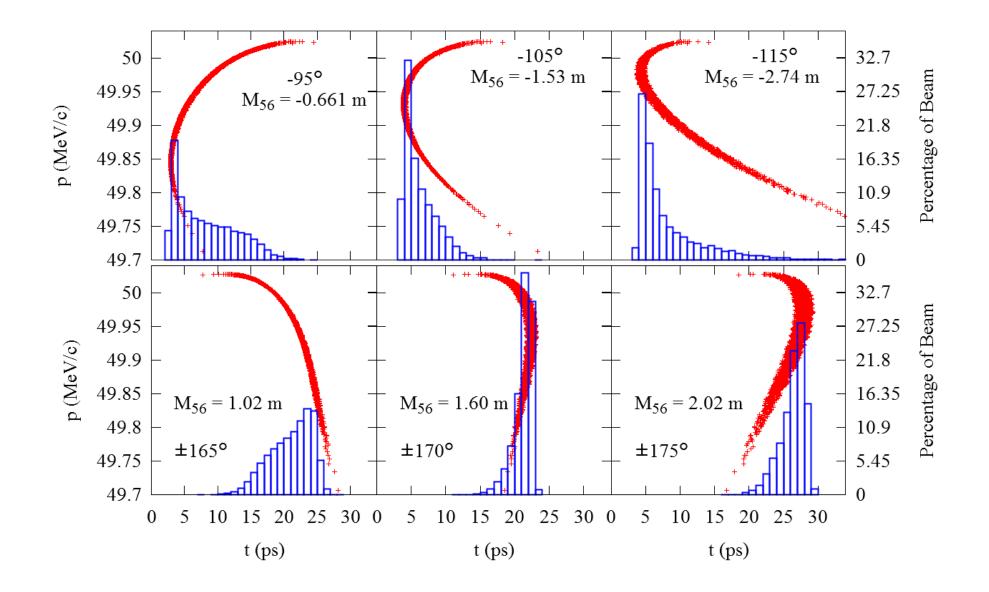


Bunch Compressor

- Consists of four dipole s-chicane.
- Two designs:
 - 3π phase advance (symmetric dispersion)
 - 4π phase advance (antisymmetric dispersion)
- *M*₅₆ is tunable by adjusting bend angle of inner dipole pair.
- Sextupoles to remove longitudinal curvature.
- Followed by uncoupling and final focusing sections.
- Modeled by elegant.

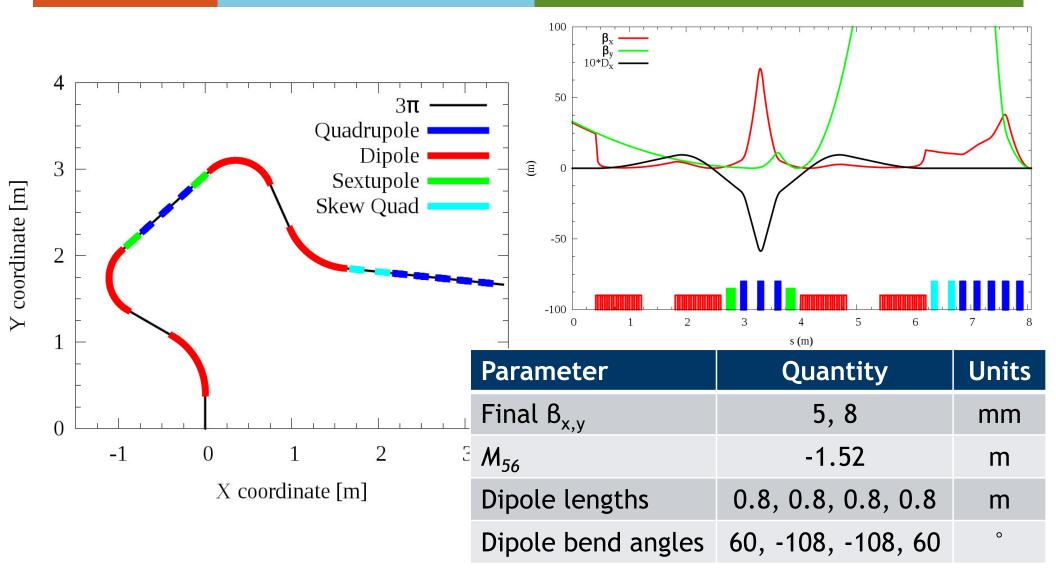


Tunable M₅₆



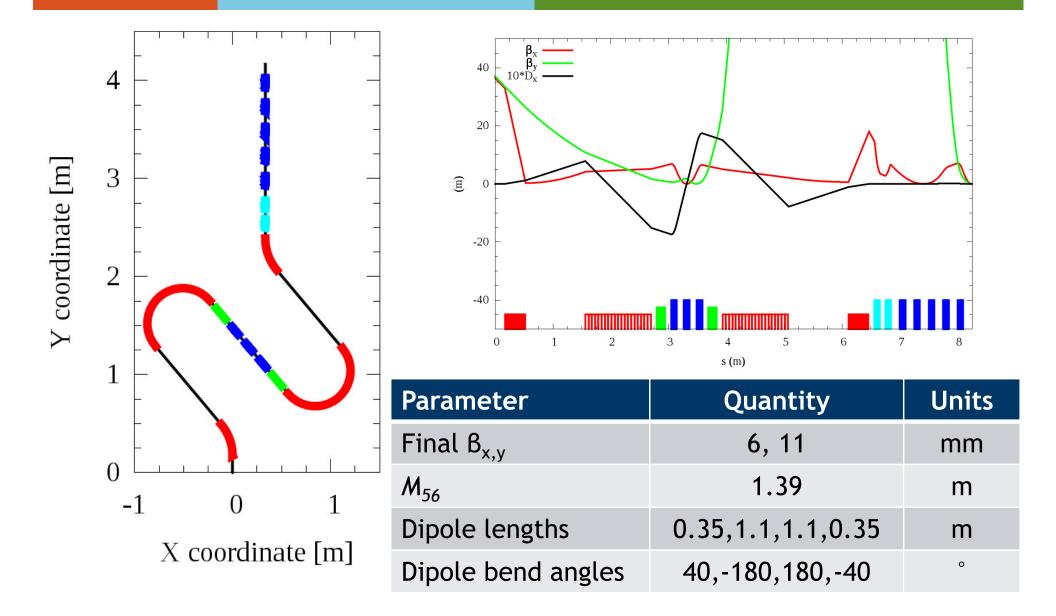
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3π Design



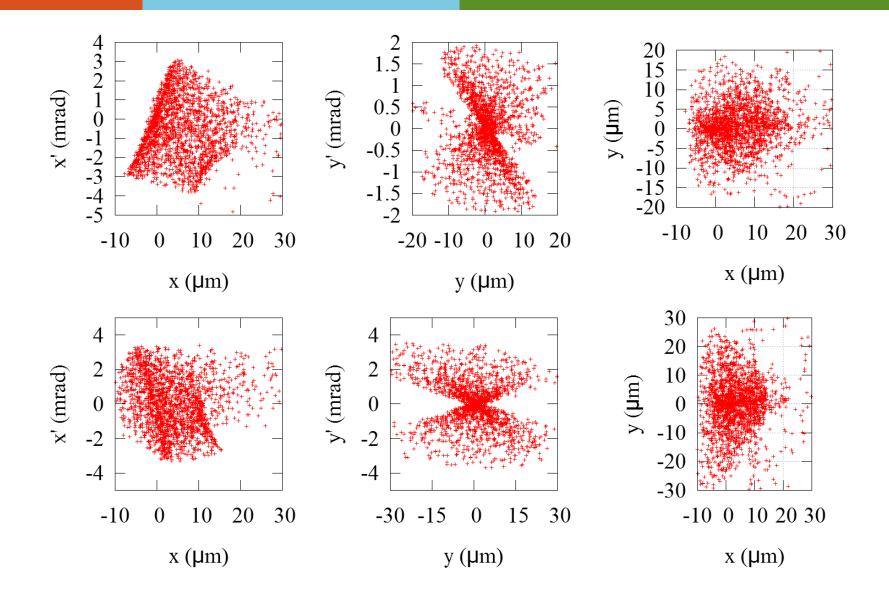


4π Design





Beam spot and phase spaces





Results vs Goals

Parameter	Goal	3π Design	4π Design	Units
Energy	25	25.02		MeV
RMS energy spread	7.5	31.09		keV
FWHM bunch length	3.0 (0.9)	2	2	psec (mm)
Normalized RMS $\epsilon_{x,y}$	0.1	0.6,0.3	0.6,1.4	mm-mrad
B _{x,y}	5	5,8	6, 11	mm
σ _{x,y}	3.2	7, 8	9, 18	μm

Summary

- Compton sources of high energy photons have existed for about thirty years
- The have followed the usual progression: [1] borrow an existing machine (1st generation), and [2] make it better by technological innovation (2nd generation?)
- We are perhaps approaching 3rd generation devices,
 i.e., electron accelerators specifically designed for
 Compton/Thomson sources. ODU or Uppsala design?
- Our design ideas are having "convergence" with high energy collider design ideas
- Lots of ideas, but still looking for the "killer ap".

Summary

- A "new" calculation scheme for high intensity pulsed laser Thomson Scattering has been developed. This same scheme can be applied to calculate spectral properties of "short", high-K wigglers, and to compute optimal incident laser chirping.
- Due to ponderomotive broadening, it is simply wrong to use single-frequency estimates of flux in many situations
- The new theory is needed for Thomson scattering of Table Top TeraWatt lasers, which have exceedingly high field and short pulses. Proper laser chirping is important in this regime.