#### X-rays by Compton Scattering and Sources Driven by SRF Linacs

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#### **Outline**

- ❖ Basic Physics
	- $\frac{1}{2}$ Wigglers, Undulators, and Insertion Devices
	- $\frac{1}{2}$ Compton Effect
	- $\frac{1}{2}$ Important Parameters
	- $\frac{1}{2}$ Line Broadening and Narrowing by Chirping
- **Example 2 Section 10 Section 10 Section 10 mm** 
	- $\frac{1}{2}$ Self-Excited Arrangements
	- $\frac{1}{2}$ External High Power Optical Cavities
- ❖ SRF Compton Sources
	- $\bullet$ New Ideas
	- $\bullet$ Layout
	- $\bullet$ Results

#### Argonne Advanced Photon Source







#### Compton Effect

#### TABLE I

Wave-length of Primary and Scattered y-rays







Fig. 7. Comparison of experimental and theoretical intensities of scattered  $\gamma$ -rays.

#### Scattered Photon Energy



Energy

 $\frac{1}{2}$ 

$$
E_{\gamma}(\theta,\varphi) = \frac{E_{\text{laser}}(1-\beta\cos\Phi)}{1-\beta\cos\theta + E_{\text{laser}}(1-\cos\Delta\Theta)/E_{e^{-}}}
$$

 $\frac{1}{2}$ Thomson limit

$$
E'_{\text{laser}} \ll mc^2
$$
,  $E_{\gamma}(\theta, \phi) \approx E_{\text{laser}} \frac{1 - \beta \cos \Phi}{1 - \beta \cos \theta}$ 

#### Field Strength Parameter

- $\mathcal{L}_{\mathcal{A}}$ Early 1960s: Laser Invented
- $\frac{1}{2}$  Brown and Kibble (1964): Earliest definition of the field strength parameters (normalized vector potential) *K* and/orparameters (normàlized vector potential) *K* and/or *a* in the literature<br>that I'm aware of

$$
a = \frac{eE_0\lambda_0}{2\pi mc^2} \quad \text{C}
$$

 $\frac{0.00000}{2}$  Compton/Thomson Sources  $K = \frac{0.000000000}{2\pi}$  $a = \frac{eE_0\lambda_0}{2\pi mc^2}$  Compton/Thomson Source

 Undulators $2\pi n c$  $\frac{0}{\sqrt{0}}$ *mceB* $K = 2\pi$  $\lambda_{\text{a}}$ 

Interpreted frequency shifts that occur at high fields as a "relativistic mass shift".

- $\frac{1}{2}$ Sarachik and Schappert (1970): Power into harmonics at high *K* and/or *a*. Full calculation for CW (monochromatic) laser. Later referenced, corrected, and extended by workers in fusion plasma diagnostics.
- $\mathcal{L}_{\mathcal{S}}$ Alferov, Bashmakov, and Bessonov (1974): Undulator/Insertion Device theories developed under the assumption of constant field strength. Numerical codes developed to calculate "real" fields in undulators.
- $\frac{1}{2}$ **Coisson (1979): Simplified undulator theory, which works at low K<br>4. and/or a. developed to understand the frequency distribution of "** and/or *a*, developed to understand the frequency distribution of "edge"<br>emission, or emission from "short" magnets, i.e., including pulse effects

#### Emission From a "Short" Magnet

Coisson low-field strength undulator spectrum\*

 $\left[\frac{c^2c}{\rho}\gamma^2\left(1+\gamma^2\theta^2\right)^2f^2\left|\tilde{B}\left(\nu\left(1+\gamma^2\theta^2\right)/2\gamma^2\right)\right|^2\right]$  $\frac{dU_{\gamma}}{d\Omega} = \frac{4r_e^2c}{\mu}\gamma^2\left(1+\gamma^2\theta^2\right)^2f^2\left[\tilde{B}\left(\nu\left(1+\gamma^2\theta^2\right)/2\gamma^2\right)\right]$  $\frac{\partial^2 \mathbf{v}}{\partial \mathbf{v} d\Omega} = \frac{4\mathbf{v}_e}{\mu_0} \gamma^2 \left(1 + \gamma^2 \theta^2\right)^2 f^2 \left[\tilde{B}\left(\mathbf{v}\left(1 + \gamma^2 \theta^2\right)/2\gamma^2\right)\right]$  $2 = f^2 + f^2$ σ $f^2 = f^2_{\sigma} + f^2_{\pi}$  $\left( 1+\gamma ^{2}\theta ^{2}\right) ^{2}$ ( )2 2 2  $^{2}$  $\theta^{2}$  $^{2}$  $\boldsymbol{\theta}^{2}$ 1 $\frac{1}{\sqrt{2}}$ sin  $1+\gamma^2\theta^2$  $\frac{1}{\sqrt{1-\gamma^2\theta^2}}\Big|_{\text{COS}}$  $\left(1+\gamma^2\theta^2\right)^2\left(1+\gamma^2\theta^2\right)$ *f* σ $f_\pi$  $(1 + \gamma^2 \theta^2)$  $(1+\gamma)$  $\ \ \gamma^{\scriptscriptstyle\angle} \theta^{\scriptscriptstyle\angle}$ θ $\phi$  $\phi$  $\gamma^2 \theta^2$  ) = $+$  $\left(\frac{1-\gamma^2\theta^2}{c}\right)_C$  $=\frac{1}{(1+\gamma^2\theta^2)^2}\left(\frac{1+\gamma^2\theta^2}{1+\gamma^2\theta^2}\right)$ c 4*e*

2 c  $e^{-}$  16 $\pi^2 \varepsilon_0^2 m^2 c^4$ 0 $r =$   $\frac{r}{r}$  $16\pi$ <sup>2</sup> $\varepsilon$ <sup>2</sup> $m$ <sup>2</sup> $c$ <sup>2</sup> ≡

\*R. Coisson, Phys. Rev. A **20**, 524 (1979)

#### Dipole Radiation

$$
\vec{B} = \frac{\mu_0 e \ddot{d} (t - r/c)}{4\pi c r} \sin \Theta \hat{\Phi}
$$

$$
\vec{E} = \frac{\mu_0 e \ddot{d} (t - r/c)}{4\pi r} \sin \Theta \hat{\Theta}
$$

$$
I = \frac{\vec{E} \times \vec{B}}{\mu_0} = \frac{\mu_0}{16\pi^2} \frac{e^2 \vec{d}^2 (t - r/c)}{cr^2} \sin^2 \Theta \hat{r}
$$

$$
\frac{dP}{d\Omega} = \frac{1}{16\pi^2 \varepsilon_0} \frac{e^2 \vec{d}^2 (t - r/c)}{c^3} \sin^2 \Theta
$$

Polarized in the plane containing  $\hat{r} = \vec{n}$  and  $\hat{r} = \vec{n}$  and  $\hat{x}$ ˆ



Define the Fourier Transform

$$
\tilde{d}(\omega) = \int d(t)e^{-i\omega t}dt \qquad d(t) = \frac{1}{2\pi} \int \tilde{d}(\omega)e^{i\omega t}d\omega
$$

With these conventions Parseval's Theorem is

$$
\int d^{2}(t) dt = \frac{1}{2\pi} \int |\tilde{d}|^{2}(\omega) d\omega
$$
  
\n
$$
\frac{dU_{\gamma}}{d\Omega} = \frac{e^{2}}{16\pi^{2} \varepsilon_{0} c^{3}} \int \tilde{d}^{2}(t - r/c) dt = \frac{e^{2}}{32\pi^{3} \varepsilon_{0} c^{3}} \int \omega^{4} |\tilde{d}|^{2}(\omega) d\omega
$$
  
\n
$$
\frac{dU_{\gamma}}{d\omega d\Omega} = \frac{1}{32\pi^{3} \varepsilon_{0}} \frac{e^{2} \omega^{4} |\tilde{d}(\omega)|^{2}}{c^{3}} \sin^{2} \Theta
$$
Blue Sky!

This equation does not follow the typical (see Jackson) convention that combines both positive and negative frequencies together in a single positive frequency integral. The reason is that we would like to apply Parseval's Theorem easily. By symmetry, the difference is a factor of two.

## Weak Field Undulator Emission

$$
\tilde{d} \cdot (\omega') = \tilde{d} \cdot (\omega') \hat{x} = -\frac{ec}{mc} \frac{\tilde{B} (\omega' / c \beta_z \gamma)}{\omega'^2} \hat{x} \qquad \tilde{B}(k) = \int B(z) e^{-ikz} dz
$$
\n
$$
\frac{dU_{\gamma,\sigma}}{d\omega d\Omega} = \frac{1}{32\pi^3 \epsilon_0} \frac{e^4}{m^2 c^3} \frac{\left| \tilde{B} (\omega (1 - \beta_z \cos \theta) / c \beta_z) \right|^2}{\gamma^2 (1 - \beta_z \cos \theta)^2} \sin^2 \phi
$$
\n
$$
\frac{dU_{\gamma,\pi}}{d\omega d\Omega} = \frac{1}{32\pi^3 \epsilon_0} \frac{e^4}{m^2 c^3} \frac{\left| \tilde{B} (\omega (1 - \beta_z \cos \theta) / c \beta_z) \right|^2}{\gamma^2 (1 - \beta_z \cos \theta)^2} \left( \frac{\cos \theta - \beta_z}{1 - \beta_z \cos \theta} \right)^2 \cos^2 \phi
$$
\n
$$
\lambda = \frac{\lambda_0}{2\gamma^2} \qquad (1 - \beta_z \cos \theta)(1 + \beta_z) \approx \frac{1}{\gamma^2} + \theta^2 + \dots \approx \frac{1 + \gamma^2 \theta^2}{\gamma^2}
$$

Generalizes Coisson results to arbitrary observation angles

#### Weak Field Thomson Backscatter

With  $\Phi = \pi$  and  $a \ll 1$  the result is identical to the weak field undulator result with the replacement of the magnetic field Fourier transform by the electric field Fourier transform

Undulator Thomson Backscatter

Driving Field

\n
$$
c\tilde{B}_y\left(\omega\left(1-\beta_z\cos\theta\right)/c\beta_z\right) = \tilde{E}_x\left(\omega\left(1-\beta_z\cos\theta\right)/\left(c\left(1+\beta_z\right)\right)\right)
$$

ForwardFrequency

$$
\lambda \approx \frac{\lambda_0}{2\gamma^2} \qquad \lambda \approx \frac{\lambda_0}{4\gamma^2}
$$

Lorentz contract + Doppler Double Doppler

#### Handy Formulas

$$
\frac{d^2U_{\gamma}}{d\omega d\Omega} = \frac{r_e^2 \mathcal{E}_0}{2\pi c} \left| \tilde{E} \left[ \frac{\omega (1 - \beta \cos \theta)}{c (1 + \beta)} \right] \right|^2 \times
$$
\n
$$
\frac{\sin^2 \phi (1 - \beta \cos \theta)^2 + \cos^2 \phi (\cos \theta - \beta)^2}{\gamma^2 (1 - \beta \cos \theta)^{2/2}}
$$
\n
$$
U_{\gamma} = \gamma^2 (1 + \beta) \frac{N_e \sigma_r}{(\sigma_e^2 + \sigma_{laser}^2)} U_{laser}
$$
\n
$$
N_{\gamma} = \sigma_r \frac{N_e N_{laser}}{2\pi (\sigma_e^2 + \sigma_{laser}^2)}
$$
\n
$$
N_{\gamma, \text{per } e} = \frac{2\pi \alpha N_{\lambda} a^2}{3}
$$

#### Number Distribution of Photons



 $E,$ 



#### Percentage in 0.1% bandwidth (*<sup>θ</sup>* = 0)

$$
N_{0.1\%} = 1.5 \times 10^{-3} N_{\gamma}
$$

#### $\div$  Flux into 0.1% bandwidth

$$
F = 1.5 \times 10^{-3} \dot{N}_\gamma
$$

Flux for high rep rate source

 $F = 1.5 \times 10^{-3} fN_{\gamma}$ 

#### Scattered Photon Energy Spread



#### Spectral Brilliance

In general

$$
B = \frac{F}{4\pi^2 \sigma_x \sigma_x \sigma_y \sigma_y}
$$
  

$$
\approx \frac{F}{4\pi^2 \sqrt{\beta_x \varepsilon_x} \sqrt{\varepsilon_x / \beta_x + \lambda / 2L} \sqrt{\beta_y \varepsilon_y} \sqrt{\varepsilon_y / \beta_y + \lambda / 2L}}
$$

For Compton scattering from a low energy beam

$$
\mathbf{B} = \frac{\mathbf{F}}{4\pi^2 \varepsilon_x \varepsilon_y}
$$

#### High a/K



*γ* = 100, distances are normalized by  $λ<sub>0</sub> / 2π$ 

#### "Effective" Dipoles

$$
D_{t}(\omega;\theta,\varphi) = \frac{1}{\gamma(1-\beta\cos\Phi)}\int \frac{eA(\xi)}{mc}e^{i\phi(\omega,\xi;\theta,\varphi)}d\xi
$$

$$
D_{p}(\omega;\theta,\varphi) = \frac{1}{\gamma(1-\beta\cos\Phi)}\int \frac{e^{2}A^{2}(\xi)}{2m^{2}c^{2}}e^{i\phi(\omega,\xi;\theta,\varphi)}d\xi
$$

And the (Lorentz invariant!) phase is

$$
\varphi(\omega,\xi;\theta,\phi) = \frac{\omega}{c} \left( \frac{\xi \frac{(1-\beta\cos\theta)}{(1-\beta\cos\Phi)} - \frac{\sin\theta\cos\phi}{\gamma(1-\beta\cos\Phi)} \int\limits_{-\infty}^{\xi} \frac{eA(\xi')}{mc} d\xi'}{\gamma^2 (1-\beta\cos\Phi)^2 \left(\frac{\xi}{c^2} - \frac{\xi^2A^2(\xi')}{2m^2c^2} d\xi'\right)} \right)
$$

#### High Field Backscatter

Undulator Thomson Backscatter

For a flat incident laser pulse the main results are very similar to those from undulaters with the following correspondences

Field Strength

*K*

*a*

ForwardFrequency

 $\int$  $\bigg)$  $\setminus$  $\bigg($  $\approx$  —————— + 21 $2\nu^2$  ( 220*K* $2\gamma^2$  (  $\lambda_{\text{a}}$  $\lambda \approx \frac{N_0}{2v^2} \left| 1 + \frac{N_0}{2} \right|$   $\lambda \approx \frac{N_0}{4v^2} \left| 1 + \frac{N_0}{2} \right|$ 

 $\int$  $\bigg)$  $\setminus$  $\bigg($  $\approx$  —————— + 21 $4\nu^2$  ( 220*a* $\cdot \gamma$  $\lambda_{\text{a}}$  $\lambda$   $\approx$   $-$ 

Transverse Pattern  $\beta^*{}_{z}+\cos\theta^*$ 

 $1+\cos\theta$ 

NB, be careful with the radiation pattern, it is the same at small angles, but quite a bit different at large angles

# Ponderomotive Broadening

$$
A_x(\xi) = A_{peak} \exp(-z^2/2(8.156\lambda_0)^2) \cos(2\pi\xi/\lambda_0)
$$
  $a_{peak} = eA_{peak}/mc$ 

$$
a_{\scriptscriptstyle peak} = eA_{\scriptscriptstyle peak} \; / \; mc
$$



#### Compensation By "Chirping"



#### Beam Illumination Methods

- ❖ Direct illumination by laser
	- **❖** Earliest method
	- Deployed on storage rings
- ❖ Optical cavities
	- $\frac{1}{2}$ Self-excited
	- $\frac{1}{2}$ Externally excited
	- Deployed on rings, linacs, and energy recovered linacs

#### Early Gamma Ray Source



Fig. 1.  $-$  Overall view of the experimental set-up.

Federici, et al.Compton Edge Federici, *et al.*<br>78 MeV Mouvo. Cim. B 59, 247 (1980)

#### Optical Cavities





#### Self Excited





#### Externally Excited





# Lyncean Compact X-ray Source



# Lyncean Source Performance





Neil, G. R., et. al, Physical Review Letters, **84,** 622 (2000)



**SCATTERING GEOMETRY** 



Boyce, et al., 17th Int. Conf. Appl. Accel., 325 (2002)

#### High Power Optical Cavities



V. Brisson, et al., NIM A, **608**, S75 (2009)

N.B., 10 kW FEL there, sans spot!

In this paper we described our first results on the locking of a Ti:sapph oscillator to a high finesse FPC. For the first time, to our knowledge, we demonstrate the possibility of stacking picosecond pulses inside an FPC at a very high repetition rate with a gain of the level of 10000. By studying thestability of four-mirrors resonators, we developed a new promising nonplanar geometry that we have just started to study experimentally. Finally, we mentioned that we shall next use the recent and powerful laser fiber amplification scheme to reach the megawatt average power inside FPC as required by the applications of the Compton X and gamma ray sources.

#### LAL/Thales THomX



BES Workshop on Compact Light Sources (2010)

### Hajima, et al.

#### Uranium Detection



Fig. 3. Layout of the 350-MeV ERL designed for a high-flux y-ray source. An electron beam generated by the 7-MeV injector is accelerated up to 350MeV by the main linac and transported to the recirculation loop. The collision point for LCS y-ray generation is located in the middle of the straight section.

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Hajima, et al., NIM A, 608, S57 (2009)TRIUMF Moly Source?
```
#### MIT CUBiX





Graves, et al., NIM A, **608**, S103 (2009)

#### **Table 1** X-ray parameters.



numerical simulation results assuming parameters of  $E = 25$  MeV,  $\varepsilon_{nx} = 0.1 \,\mu\text{m}$ ,  $x_e = 2 \,\mu\text{m}$ ,  $\Delta t_L = 0.3 \,\text{ps}$ ,  $\lambda = 1 \,\mu\text{m}$ ,  $Q_e = 10 \,\text{pc}$ , and  $W<sub>y</sub> = 10$  mJ. Note that no nonlinear effects were included in this



### ODU Compton Light Source

01 June 2015





#### **Parameters**



Electron beam parametersat collision point.



#### **Parameters**



Optical cavity parameters.

Compton source parameters.



## Electron gun



- $\frac{1}{2}$  Originally based on quarter-wave SRF electron gun developed by Harris *et al.*
- $\frac{1}{2}$  Highly reentrant to mitigate growth of normalized emittance due to space charge.



RF Properties at  $\mathsf{E}_{\mathsf{acc}}$  = 1 MV/m

#### Electron gun

- † EM fields calculated by<br>SUPEREISH SUPERFISH
- **\*** Particle tracking simulated<br>by ASTRA by ASTRA
- ❖ Diameter/length 30 cm<br>❖ Beam travels 15 cm
- ❖ Beam travels 15 cm



- Top: Transverse phase space and spot. Bottom: Electron beam
	- properties at gun exit.









- ❖ Consists of 4 high-velocity,<br>double-spoke cavities double-spoke cavities.
- Alternating orientation to produce<br>roundest beam at exit roundest beam at exit.
- $\div$  500 MHz<br> $\div$  Diamete
- ❖ Diameter of 41.6 cm<br>❖ Longth of 80.5 cm
- ❖ Length of 80.5 cm
- **EM fields calculated by CST**<br>Microwayo Studio Microwave Studio.
- \* Particle tracking simulated<br>by ASTRA by ASTRA.
- ❖ Entire accelerating section has<br>
<u>F</u> m x 1 m footprint 5 m x 1 m footprint







❖ Transverse phase spaces are bowties,<br>not ellinses not ellipses.

Top: Electron beam properties at linac exit. Bottom: Transverse phase spaces and beam spot.



 $y$  (mm)

 $-1 - 0.5$  0 0.5 1

 $x$  (mm)

0.08 0.06 0.04  $0.02$  $\overline{0}$ 





## Matching



- Solenoid transforms bowties into phase spaces.<br>A Normalized PMS s : 0.16, 0.15, 0.19, 0.18 m
- $\clubsuit$  Normalized RMS  $\varepsilon_{x,y}$ : 0.16, 0.15  $\rightarrow$  0.19, 0.18 mm-mrad.<br> $\clubsuit$  As solenoid strength increases, so does emittance growt
- ❖ As solenoid strength increases, so does emittance growth.<br>❖ Eollowed by a quadrupole and skew quadrupole, to get q
- Followed by a quadrupole and skew quadrupole, to get  $\alpha_x = \alpha_y$  and to remove<br>x'w' coupling respectively *x'y'* coupling, respectively.
- ❖ ~1 m in length.<br>❖ Modeled by ele
- ❖ Modeled by elegant.



# Bunch Compressor

- ❖ Consists of four dipole s-chicane.
- ❖ Two designs:
	- $\frac{1}{2}$ 3π phase advance (symmetric dispersion)
	- 4π phase advance (antisymmetric dispersion)
- ◆  $M_{56}$  is tunable by adjusting bend angle of inner dipole pair.
- $\frac{1}{2}$ Sextupoles to remove longitudinal curvature.
- $\frac{1}{2}$ Followed by uncoupling and final focusing sections.
- $\frac{1}{2}$ Modeled by elegant.



# Tunable M<sub>56</sub>



## 3π Design





## 4π Design





#### Beam spot and phase spaces





#### Results vs Goals





- ❖ Compton sources of high energy photons have existed<br>for about thirty vears for about thirty years
- **↑ The have followed the usual progression: [1] borrow an**<br>existing mashine (1st generation), and [2] make it existing machine (1<sup>st</sup> generation), and [2] make it better by technological innovation (2<sup>nd</sup> generation?)
- $\div$  We are perhaps approaching 3<sup>rd</sup> generation devices, i.e., electron accelerators specifically designed for Compton/Thomson sources. ODU or Uppsala design?
- Our design ideas are having "convergence" with high<br>conserves lider design ideas energy collider design ideas
- $\frac{1}{2}$ Lots of ideas, but still looking for the "killer ap".

#### **Summary**

- A "new" calculation scheme for high intensity pulsed<br>lases Themsen Scattering has been developed. This laser Thomson Scattering has been developed. This same scheme can be applied to calculate spectral properties of "short", high-*K* wigglers, and to compute optimal incident laser chirping.
- ❖ Due to ponderomotive broadening, it is simply wrong<br>to use single frequency estimates of flux in many. to use single-frequency estimates of flux in many situations
- The new theory is needed for Thomson scattering of<br>Table Ten TeraWatt lasers, which have exceedingly Table Top TeraWatt lasers, which have exceedingly high field and short pulses. Proper laser chirping is important in this regime.