

# Towards realising PRISM based muon to electron conversion experiment

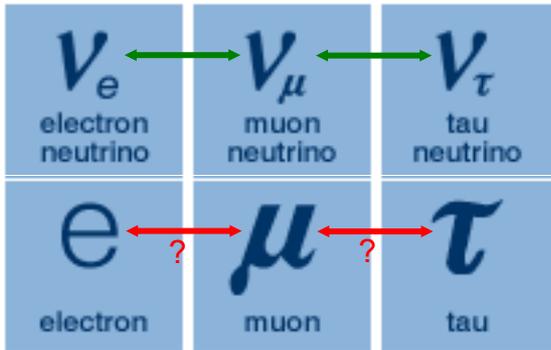
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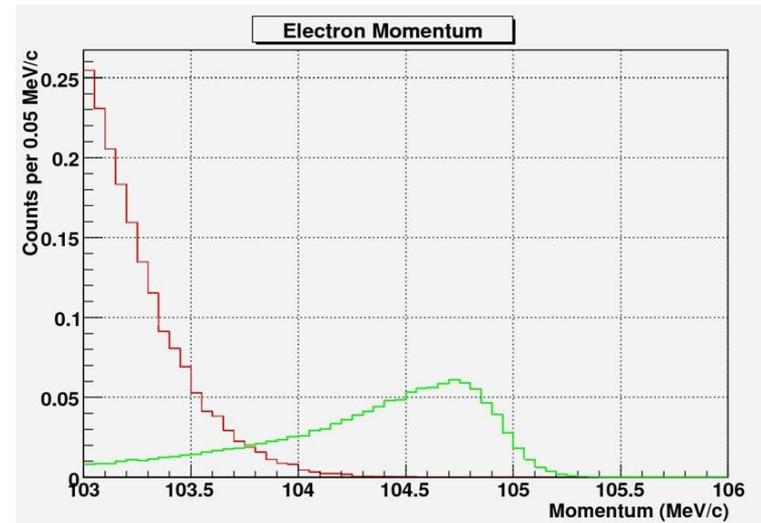
# Outline

- PRISM Parameters
- Challenges of PRISM
- PRISM Task Force initiative.
- Muon beam matching into FFAG ring.
- Injection/extraction hardware.
- Injection issues
- New ring design
- Way forward
- Conclusions

- Charge lepton flavor violation (cLFV) is strongly suppressed in the Standard Model, its detection would be a clear signal for **new physics!**
- Search for cLFV is **complementary** to LHC.
- The  $\mu^- + N(A,Z) \rightarrow e^- + N(A,Z)$  seems to be **the best laboratory** for cLFV.
- The background is dominated by beam, which can be **improved**.
- PRISM/PRIME is the next generation experiment (possible upgrade path to COMET).



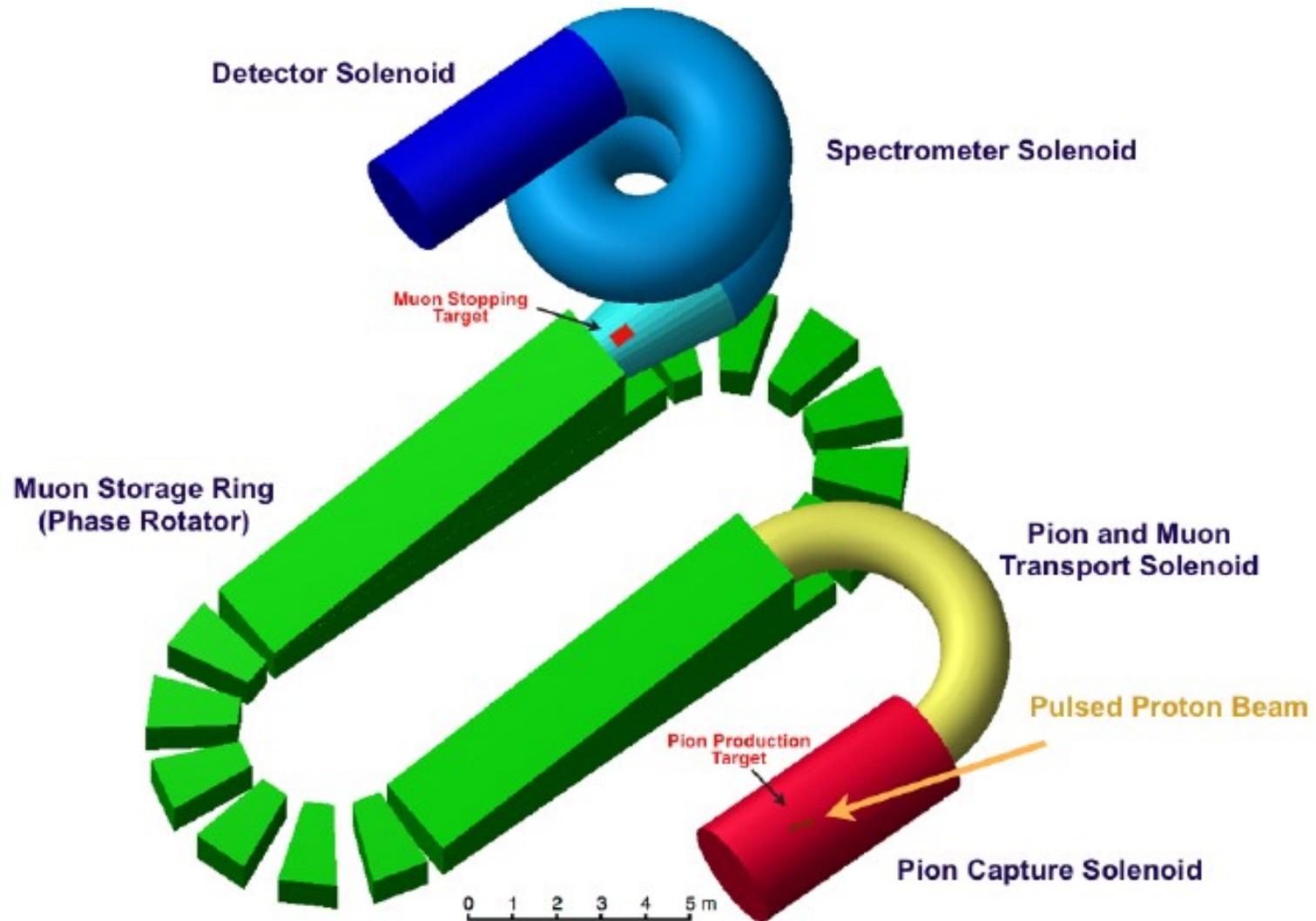
Does cLFV exist?



Simulations of the expected electron signal (green).



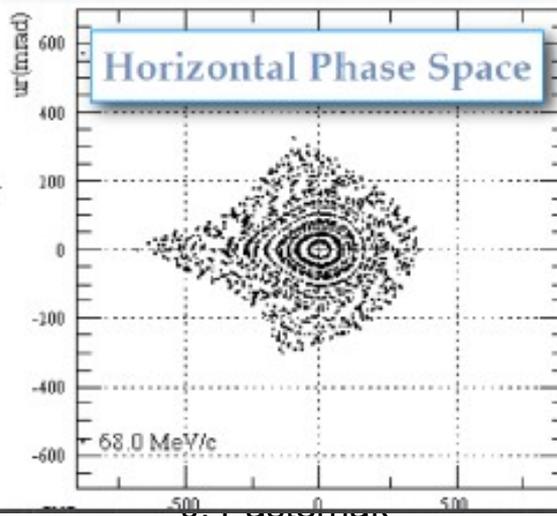
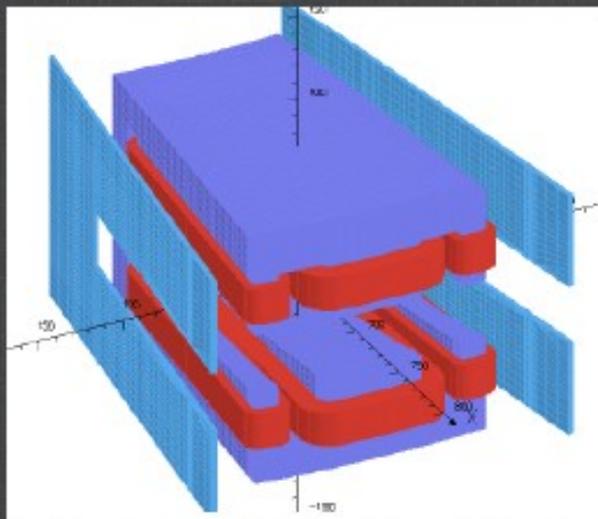
# PRISM overview





# Phase rotator (1)

- 10-cell DFD FFAG ring designed at RCNP, Osaka University.
- FFAG magnet designed, manufactured and tested.
- Phase rotation principle demonstrated with  $\alpha$  particles.
- Problems of injection/extraction.



Parameter	Value
Target type	solid or <b>liquid (powder)</b>
Proton beam power	1-4 MW
Proton beam energy	multi-GeV
<b>Proton bunch duration</b>	<b>~10 ns total (in synergy with the NF)</b>
Pion capture field	4-10 T
Momentum acceptance	$\pm 20\%$
Reference $\mu^-$ momentum	40-68 MeV/c
Harmonic number	1
Minimal acceptance (H/V)	3.8/0.5 $\pi$ cm rad
RF voltage per turn	3-5.5 MV
RF frequency	3-6 MHz
Final momentum spread	$\pm 2\%$
Repetition rate	100 Hz-1 kHz

- **The need for the compressed proton bunch:**
  - is in full synergy with the Neutrino Factory and a Muon Collider.
  - puts PRISM in a position to be one of the incremental steps of the muon programme.
- **Target and capture system:**
  - is in full synergy with the Neutrino Factory and a Muon Collider studies.
  - requires a detailed study of the effect of the energy deposition induced by the beam
- **Design of the muon beam matching from the solenoidal capture to the PRISM FFAG ring.**
  - very different beam dynamics conditions.
  - very large beam emittances and the momentum spread.
- **Muon beam injection/extraction into/from the FFAG ring.**
  - very large beam emittances and the momentum spread.
  - affects the ring design in order to provide the space and the aperture.
- **RF system**
  - large gradient at the relatively low frequency and multiple harmonics (the “sawtooth” in shape).

## The aim of the PRISM Task Force:

- Address the technological challenges in realising an FFAG based muon-to-electron conversion experiment,
- Strengthen the R&D for muon accelerators in the context of the Neutrino Factory and future muon physics experiments.

## The Task Force areas of activity:

- the physics of muon to electron conversion,
- proton source,
- pion capture,
- muon beam transport,
- injection and extraction for PRISM-FFAG ring,
- FFAG ring design including the search for a new improved version,
- FFAG hardware systems R&D.

## Members:

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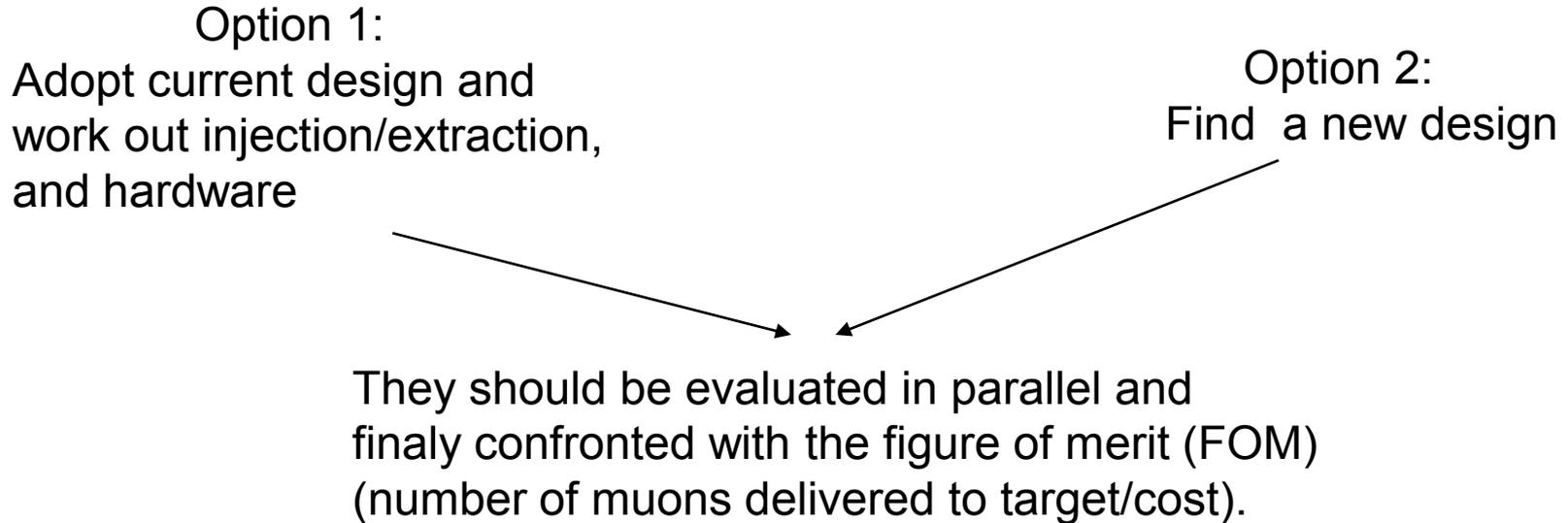
Y. Mori, Kyoto University, KURRI, Osaka, Japan

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J. Pasternak **You are welcome to join us!**



### Requirements for a new design:

- High transverse acceptance (at least  $38h/5.7v$  [ $\text{Pi mm}$ ] or more).
- High momentum acceptance (at least  $\pm 20\%$  or more).
- Small orbit excursion.
- Compact ring size (this needs to be discussed).
- Relaxed or at least conserved the level of technical difficulties. for hardware (kickers, RF) with respect to the current design.

## Option 1:

Adopt current design and work out injection/extraction, and hardware



We should think how to efficiently use existing PRISM magnets:

- demonstration of the concept (?)
- longitudinal cooling experiment (?)

## Option 2:

Find a new design



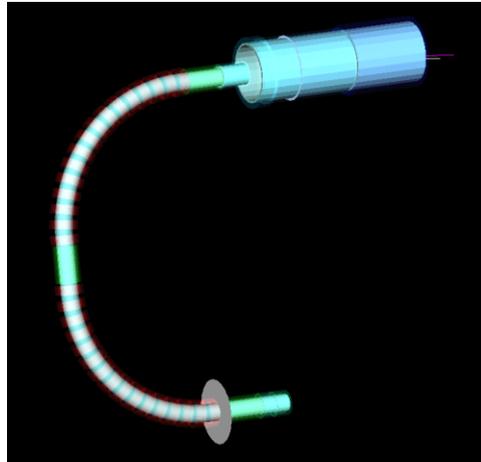
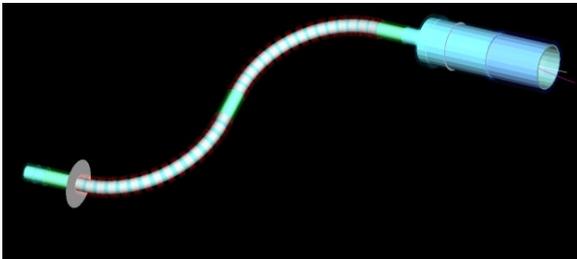
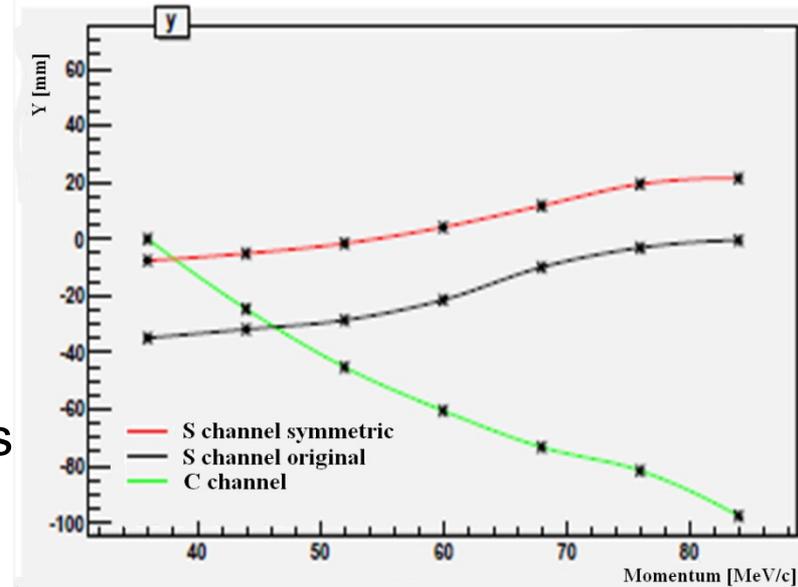
There are indications a new design with very good properties is possible (see later)

# Main challenges before TF started working:

- Matching from the solenoid into FFAG
- Injection/Extraction geometries
- Kicker hardware
- Septum magnet
- RF system
- Beam dynamics in FFAG

# Matching to the FFAG I

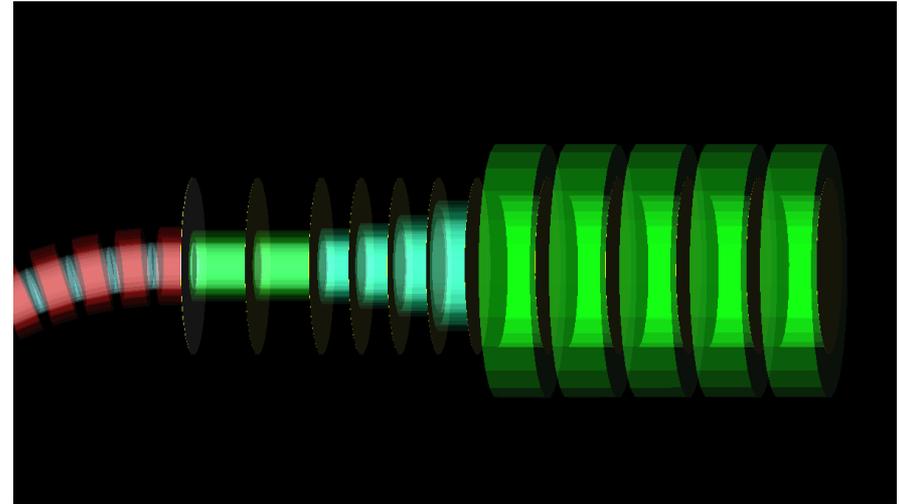
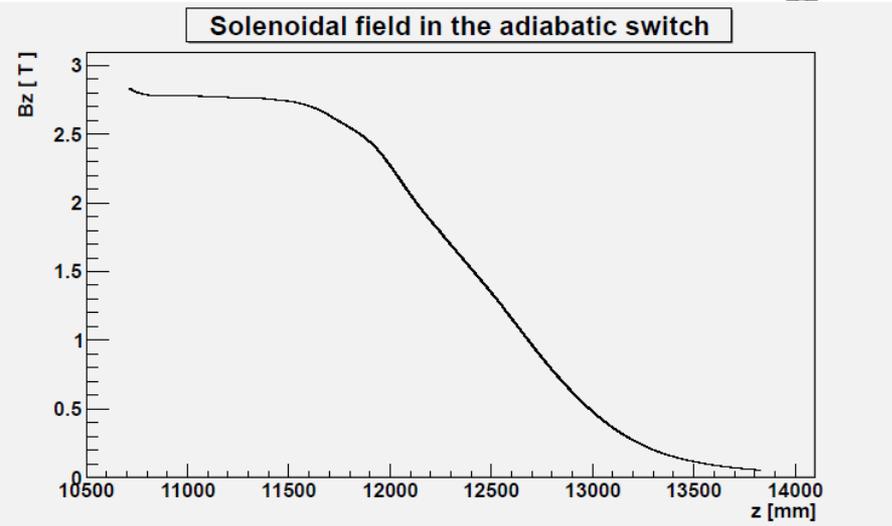
- Muon beam must be transported from **the pion production solenoid to the Alternating Gradient channel.**
- Two scenarios considered, S-shaped and C-shaped.
  - S-shaped with correcting dipole field has the best transmission and the smallest dispersion.



The mean vertical beam position versus momentum at the end of bend solenoid channel for various configurations.

Main conclusion from this study is:  
both S and C geometries could be used  
although S is performing a bit better.

# Matching to the FFAG II



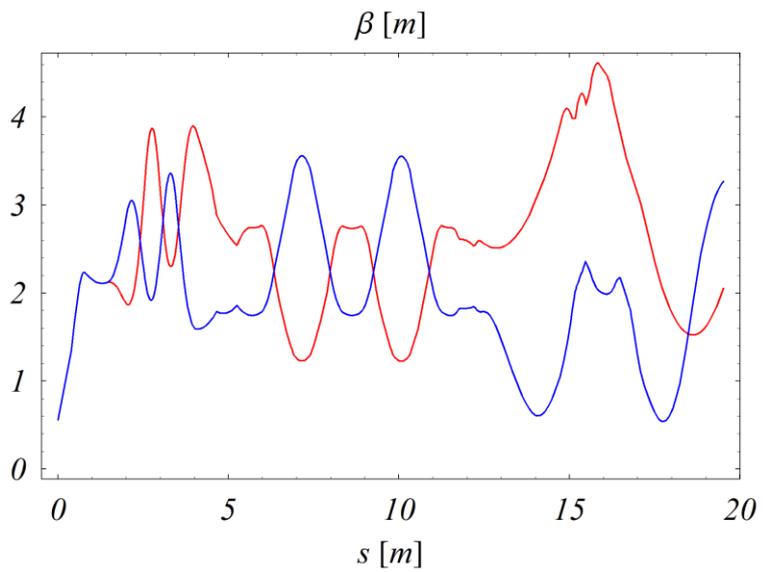
Initial version of the adiabatic switch

Preliminary geometry: the end of the S-channel together with matching solenoids, adiabatic switch and 5 quad lenses.

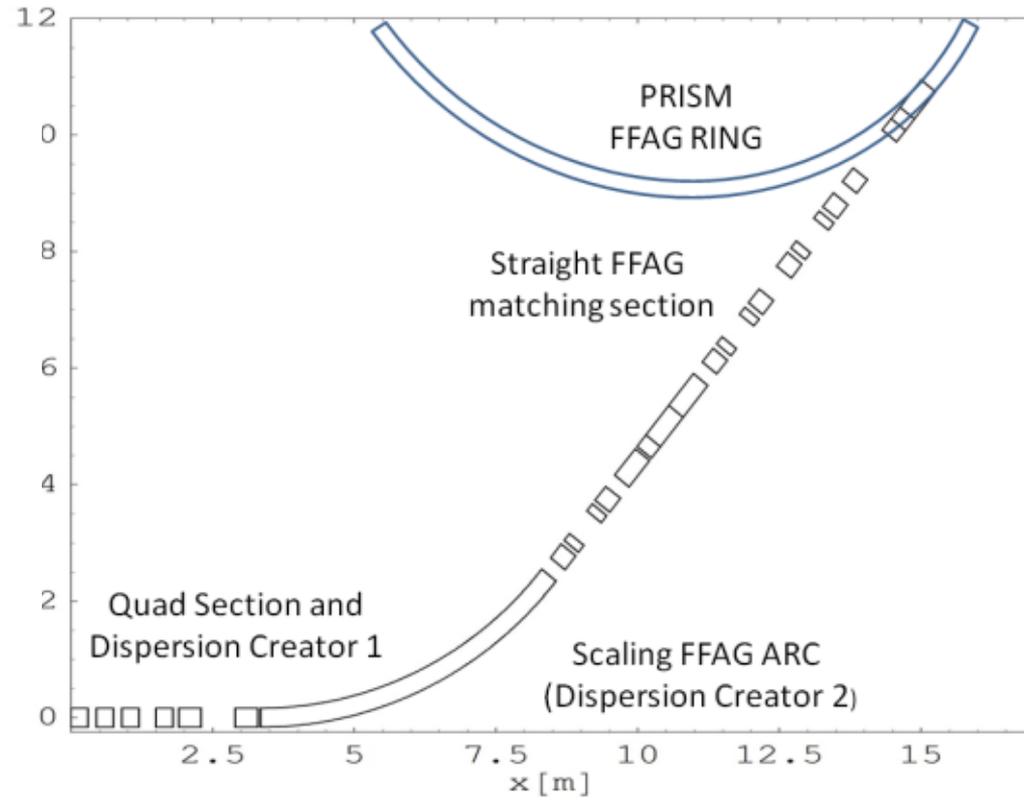
Current best version includes:

- adiabatic switch from 2.8 to 0.5 T (to increase the beam size),
- additional solenoidal lens to match  $\alpha=0$  (not shown in the pictures above),
- 5 quad lenses,

- A dedicated transport channel has been designed to match dispersions and betatron functions.



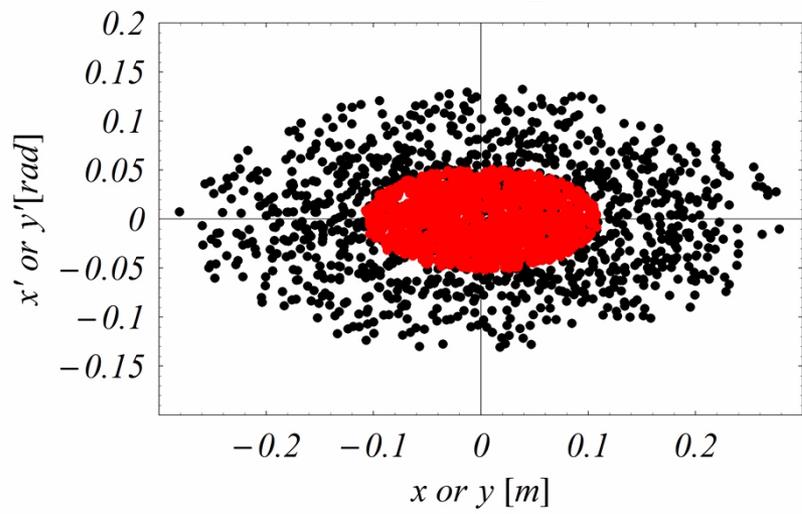
Horizontal (red) and vertical (blue) betatron functions in the PRISM front end.



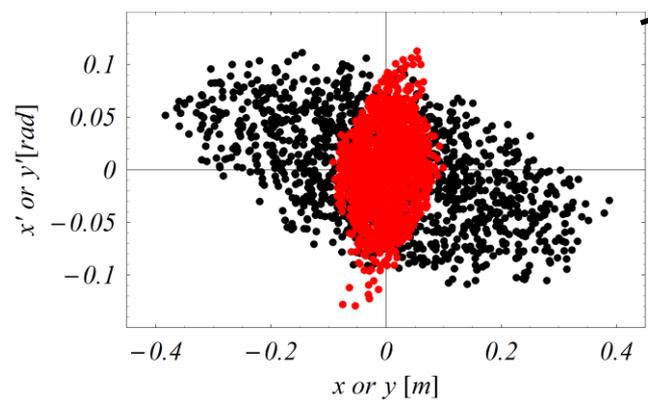
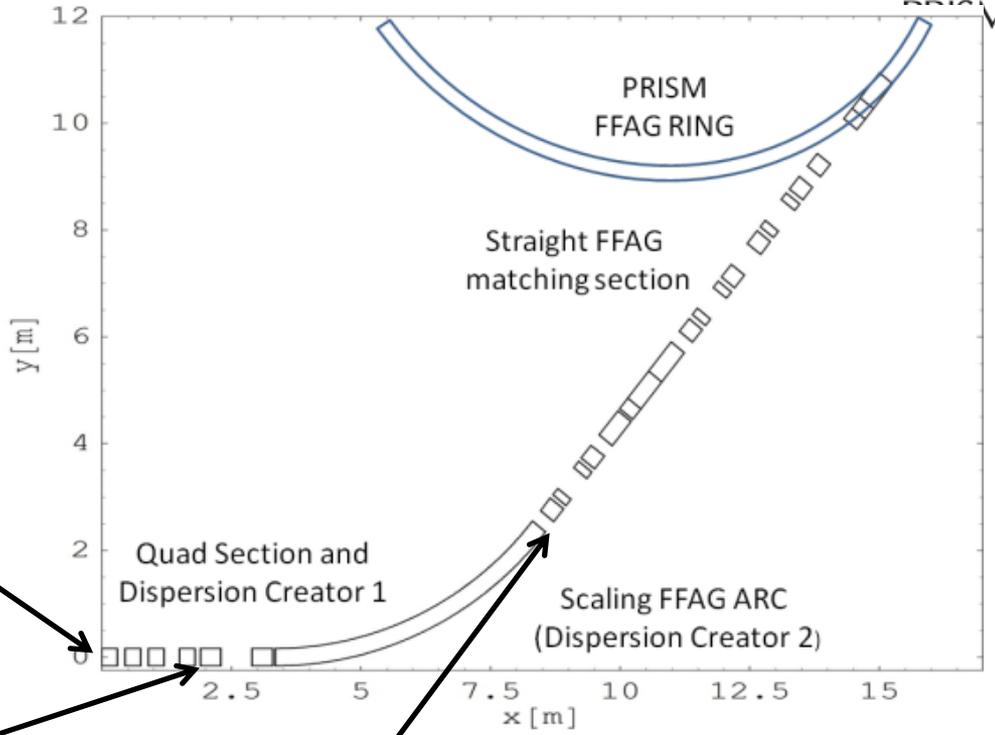
Layout of the matching section seen from the above.

# Matching to the FFAG IV

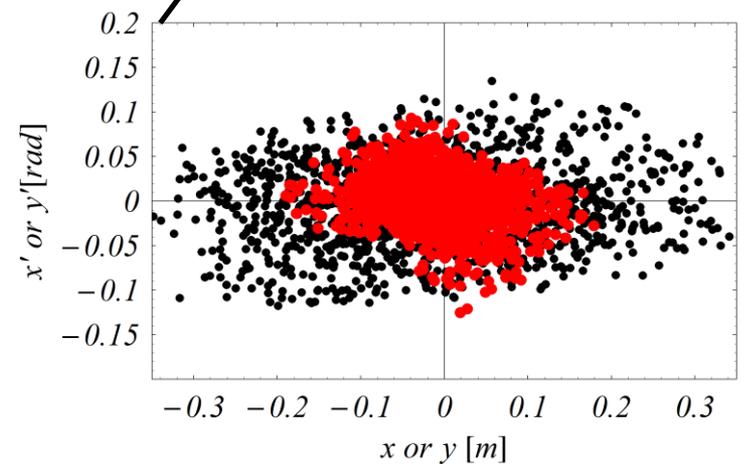
- Tracking status (work in progress)



Horizontal (black) and vertical (red) phase spaces at the input to the AG part of the PRISM muon front end.



At the end of the quad Channel



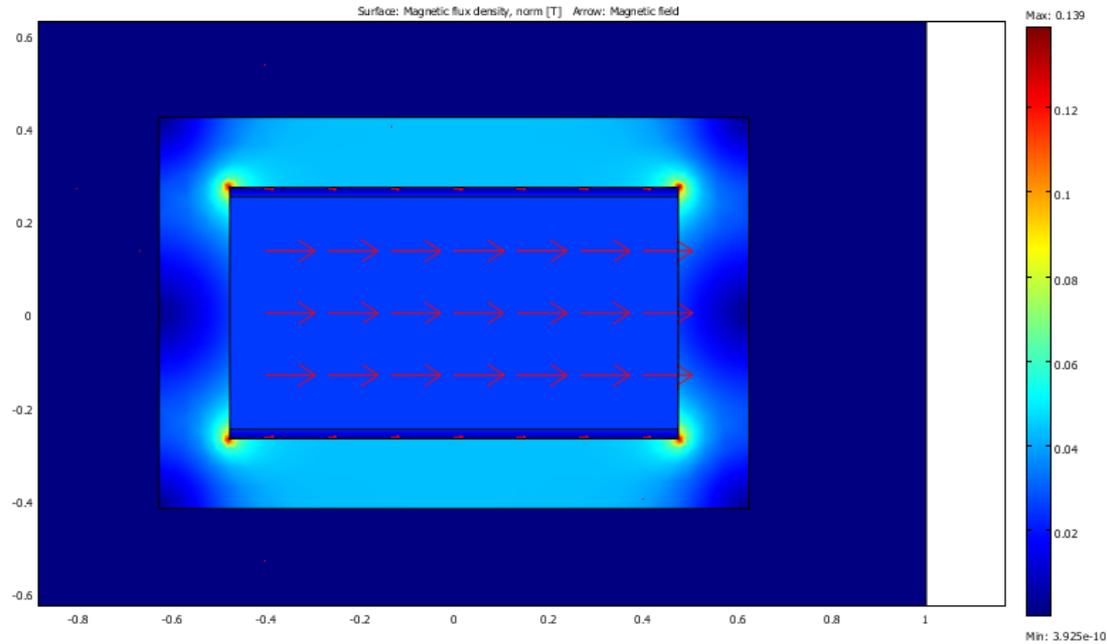
At the end of the horizontal dispersion creator (transmission 97%)

Main conclusion from this study is:  
matching from the solenoid and  
dispersion creation can be done without  
big losses within the FFAG acceptances.

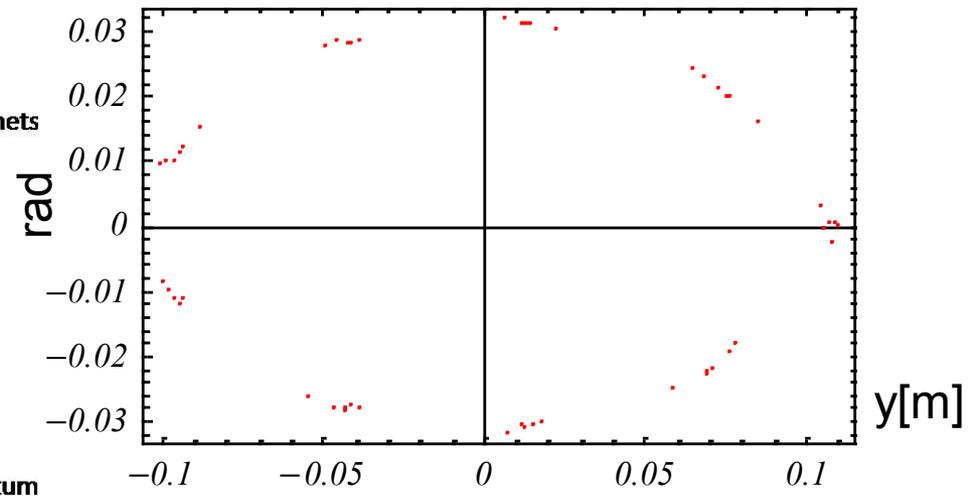
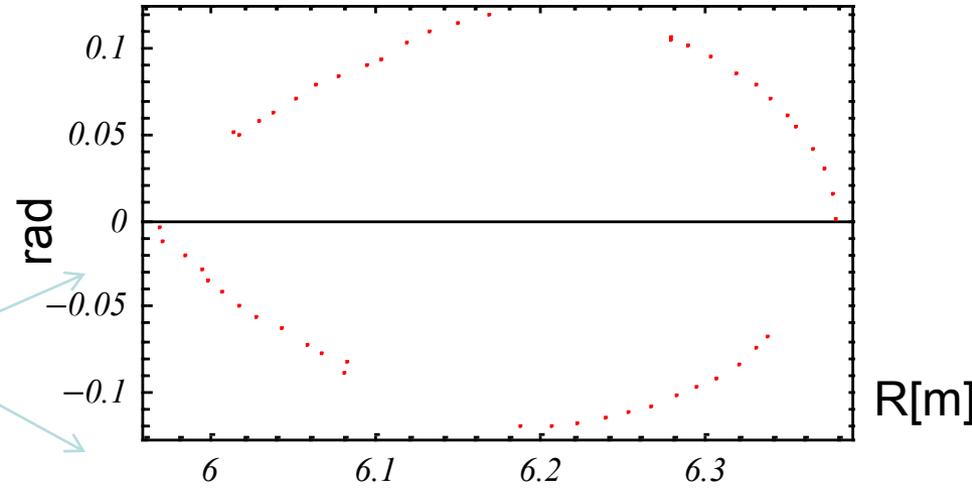
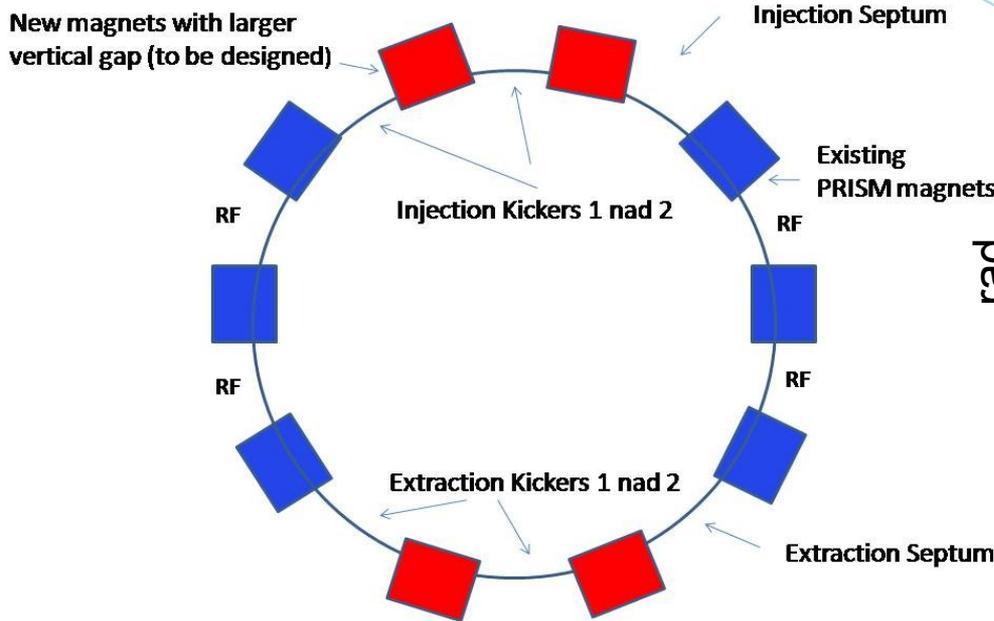
Further optimization and full tracking  
studies are still required!

# Preliminary PRISM kicker studies

- length 1.6 m
- B 0.02 T
- Aperture: 0.95 m x 0.5
- Flat top 40 / 210 ns (injection / extraction)
- rise time 80 ns (for extraction)
- fall time ~200 ns (for injection)
- $W_{\text{mag}} = 186 \text{ J}$
- $L = 3 \text{ uH}$  (preliminary)
- $I_{\text{max}} = 16 \text{ kA}$



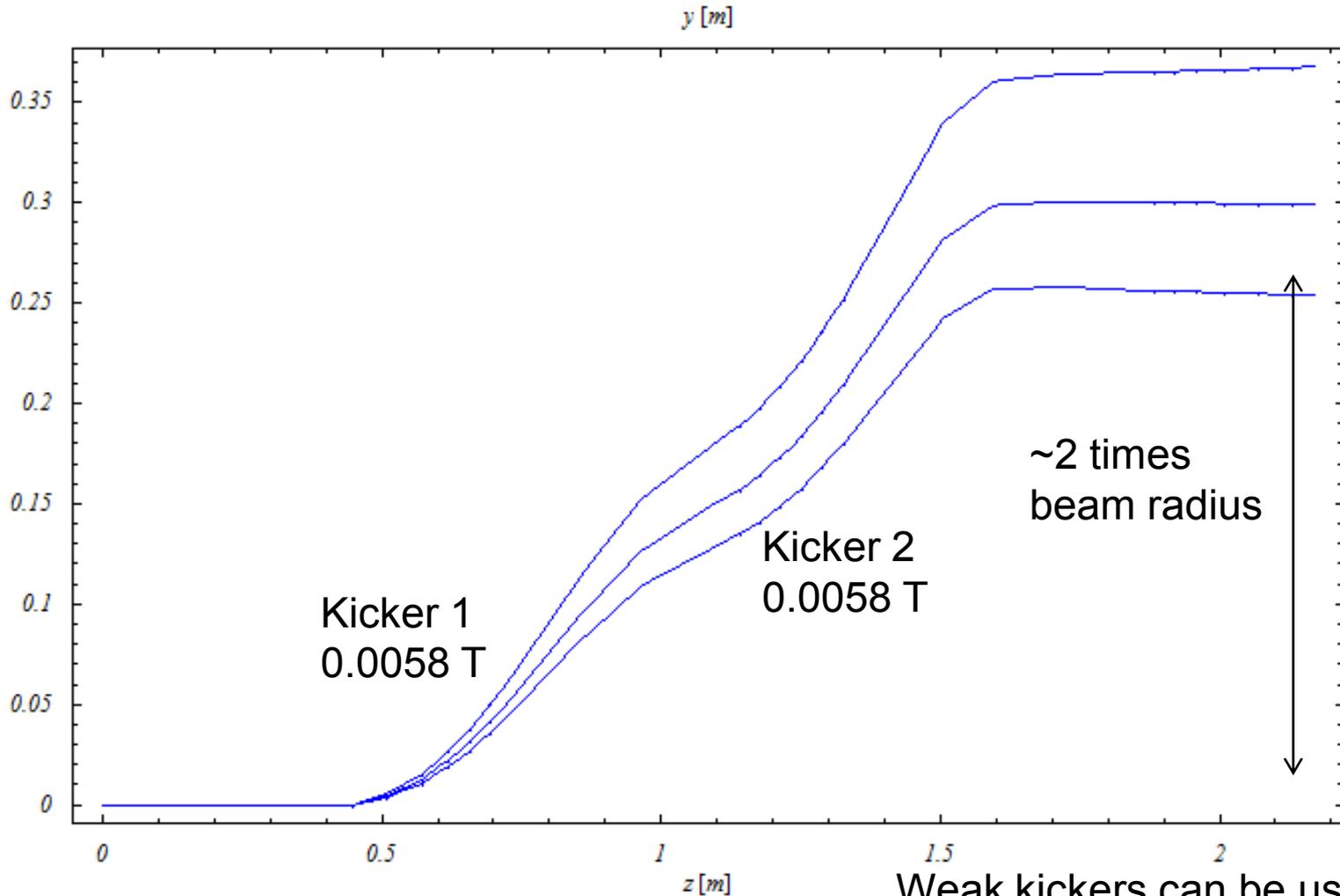
- In order to inject/extract the beam into the reference design, special magnets with larger vertical gap are needed.
- This may be realised as an insertion (shown in red below).
- The introduction of the insertion breaks the symmetry but this does not limit the dynamical acceptance, if properly done!



We can re-use existing magnets!

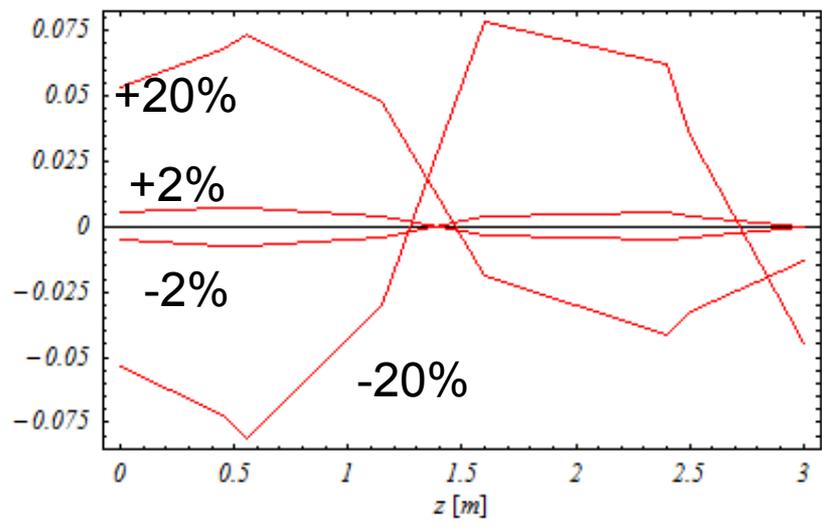
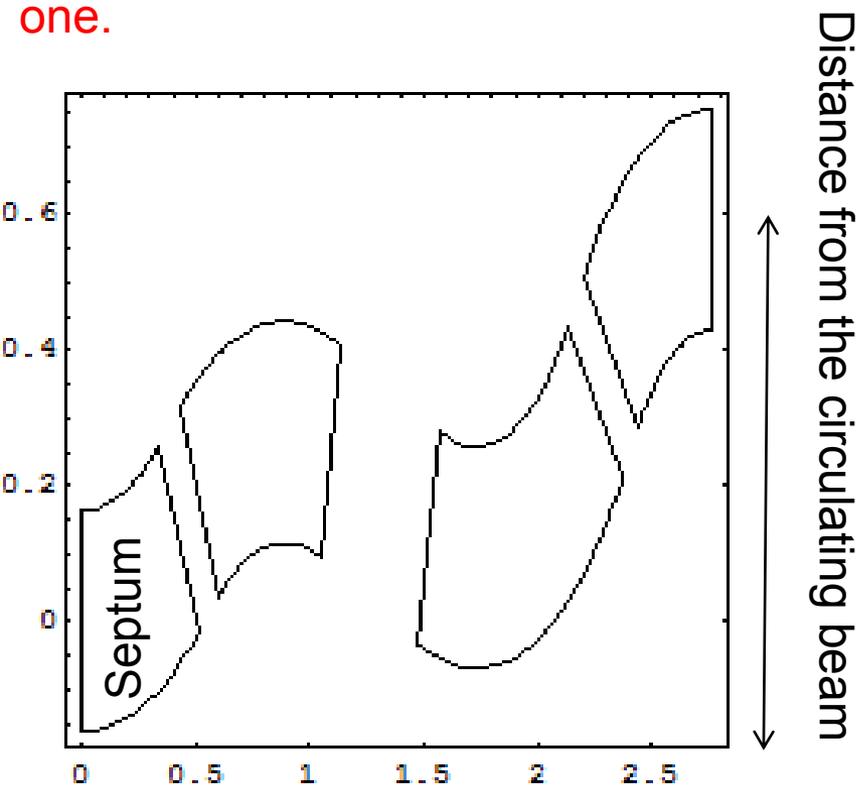
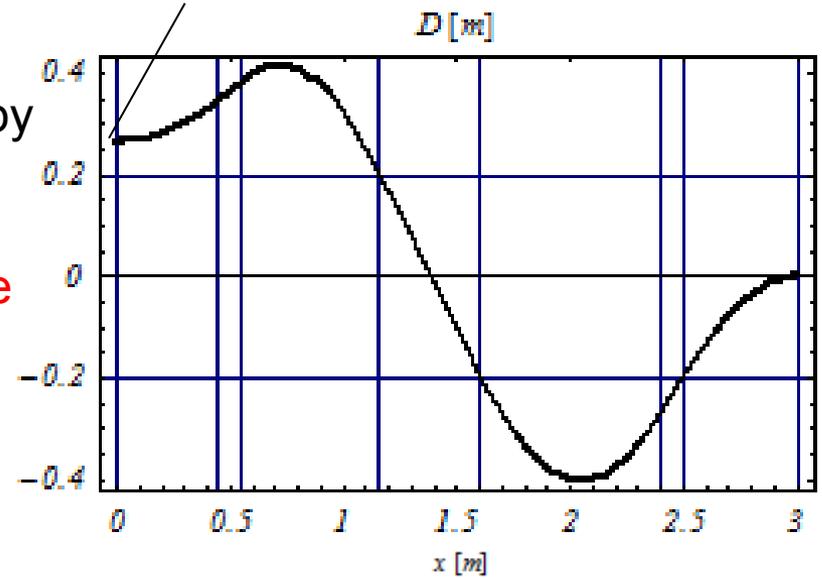
# Vertical injection

## Orbit separation with 2 kickers



Dispersion created by the kicker

- System of vertical deflectors is proposed to suppress the vertical dispersion produced by the kicker and septum.
- It works for small and large positive  $\Delta p/p$ , however there are problems for large negative one.



Difficult matching!

# HFFAG with V bending

- Conventional horizontal FFAG bends in horizontal plane and have horizontal orbit excursion
  - For straight case:  $B_y = B_{y0} \text{Exp}[mx]$
- VFFAG bends in horizontal plane and have vertical orbit excursion
  - For straight case:  $B_y = B_{y0} \text{Exp}[my]$
- We need vertical septum, which keeps the horizontal orbit excursion
  - Straight case would mean  $B_x = B_{x0} \text{Exp}[mx]$

# HFFAG with V bending (2)

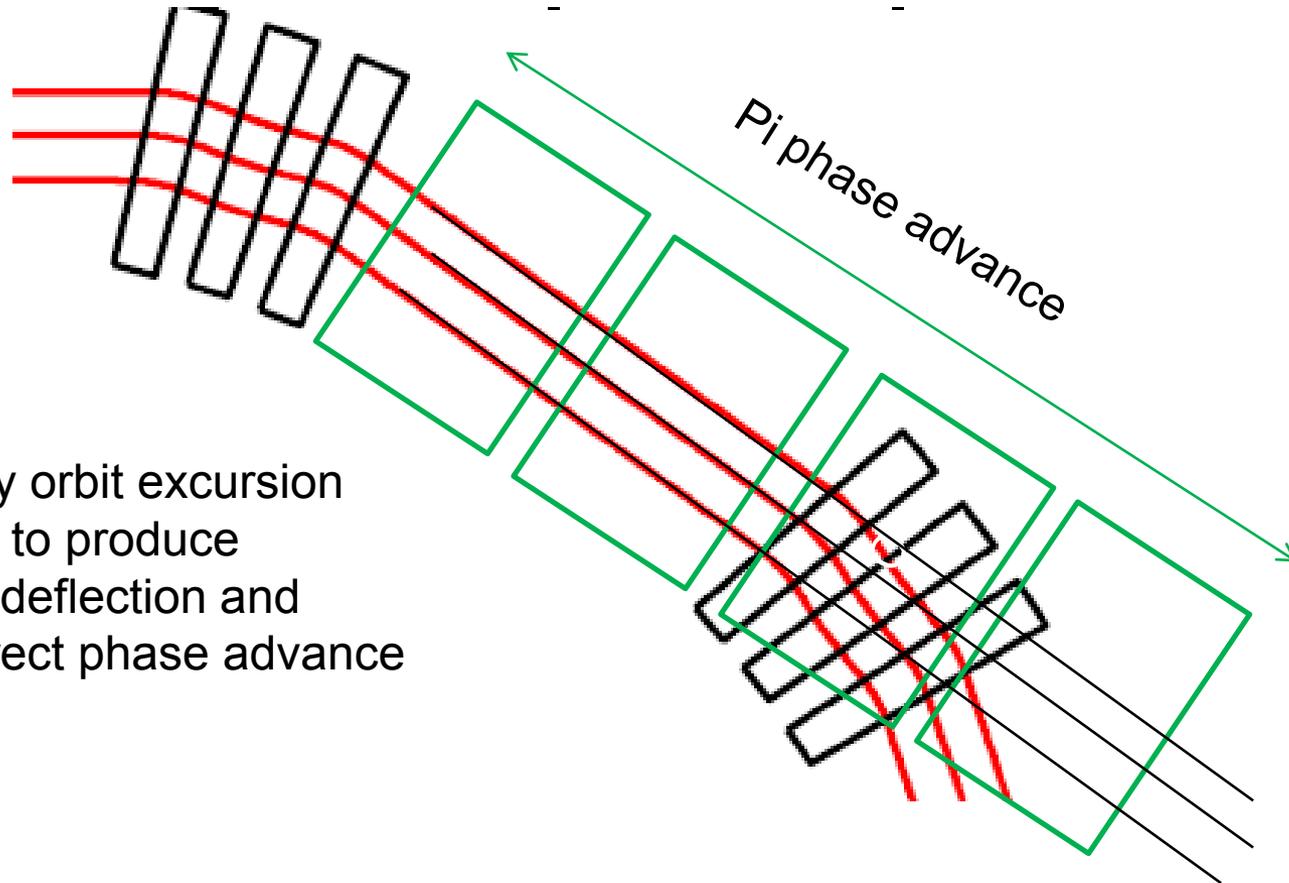
$$B_x = B_{x0} \text{Exp}[mx] = B_{x0} + B_{x0} mx + 1/2 B_{x0} m^2 x^2 + \dots$$

Vertical dipole

Skew quad

Skew sextupole

# HFFAG with V bending (3)



- $m$  is fixed by orbit excursion
- $B_x$  is aimed to produce both enough deflection and to obtain correct phase advance

# HFFAG with V bending (4)

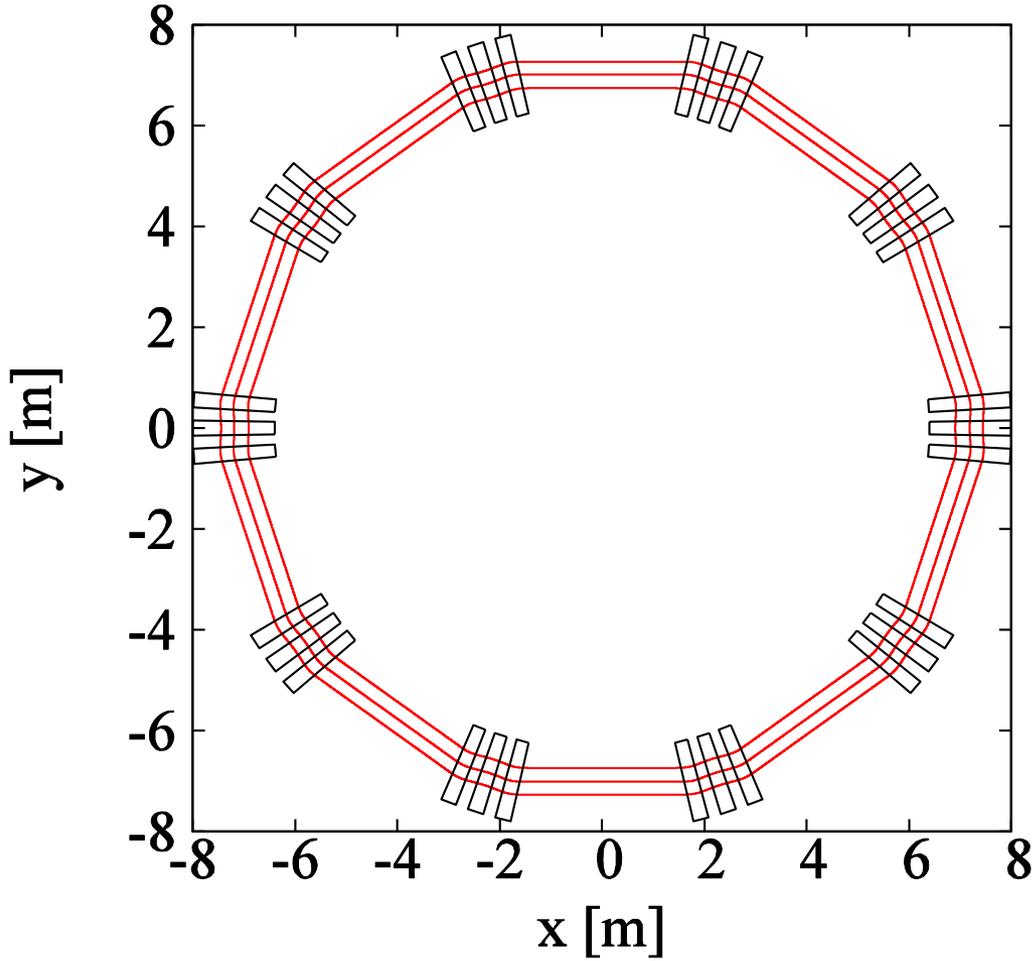
- Preliminary studies confirm the conservation of the orbit excursion
  - Particles with momentum spread but zero betatron amplitude are all deflected by the same angle and reach the same vertical distance even for large  $\Delta p/p$
- They also show strong transverse coupling in H/V planes
  - ...probably the desired phase advance was not achieved, which can be improved
  - However strong H/V coupling in the PRISM system with highly asymmetric emittances is rather challenging!

Main conclusion from this study is:  
Full vertical injection is very difficult!

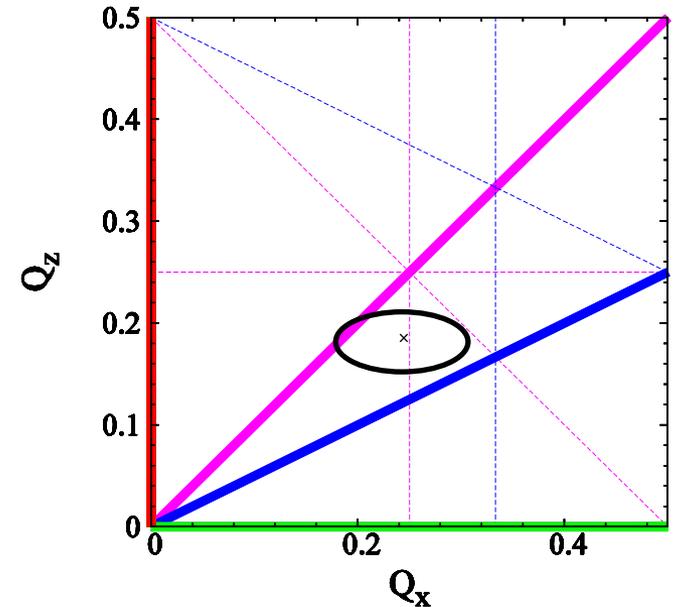
We most likely agree:  
Full horizontal injection is impossible!

We need a new idea!

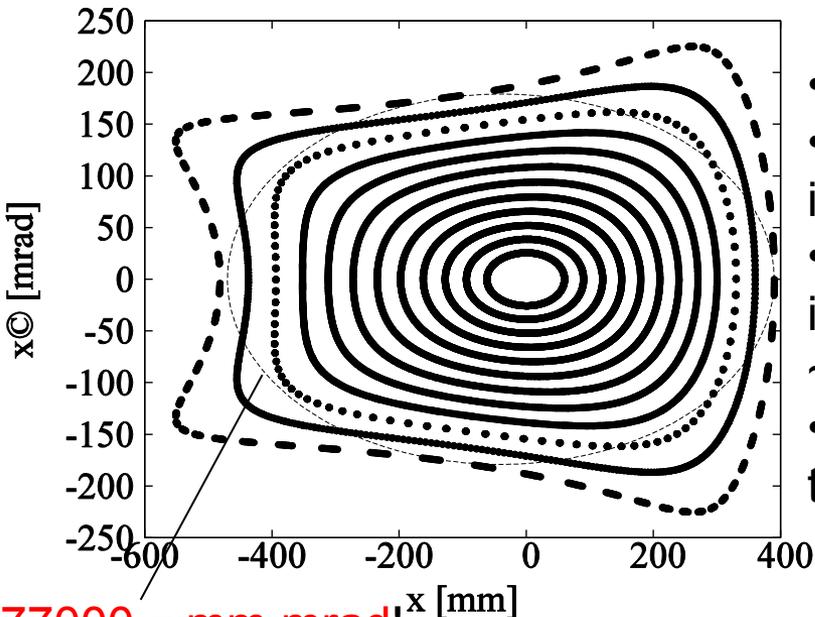
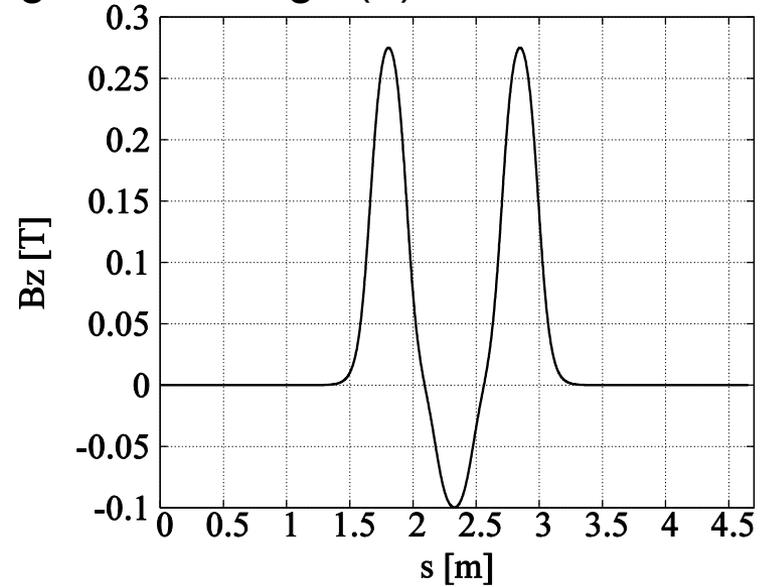
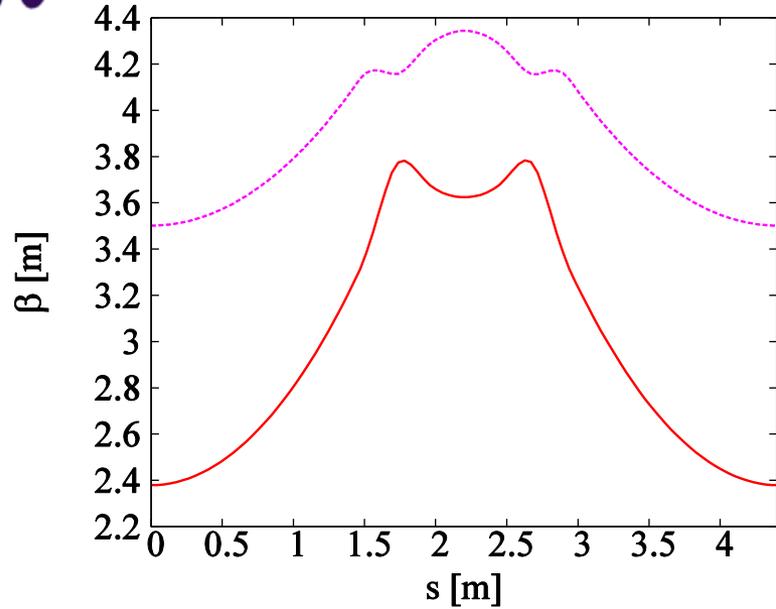
# New FDF scaling FFAG design



- FDF symmetry motivated by the success of ERIT at KURRI
- 10 cells
- $k = 4.3$
- $R_0 = 7.3 \text{ m}$
- $(Q_H, Q_V) = (2.45, 1.85)$
- Minimal drift length 3m



# New FDF scaling FFAG design (2)



- Enge field fall-off used to study fringe fields
- Enormous horizontal acceptance is achieved in simulations
- Vertical long term stability of  $\sim 3000 \pi \cdot \text{mm} \cdot \text{mrad}$  is achieved, however with some optimization  $\sim 5000 \pi \cdot \text{mm} \cdot \text{mrad}$  should be stable for a few turns.
- $5000 \pi \cdot \text{mm} \cdot \text{mrad}$  is what we currently aim for due to injection limitations.

**77000  $\pi \cdot \text{mm} \cdot \text{mrad}$ !**



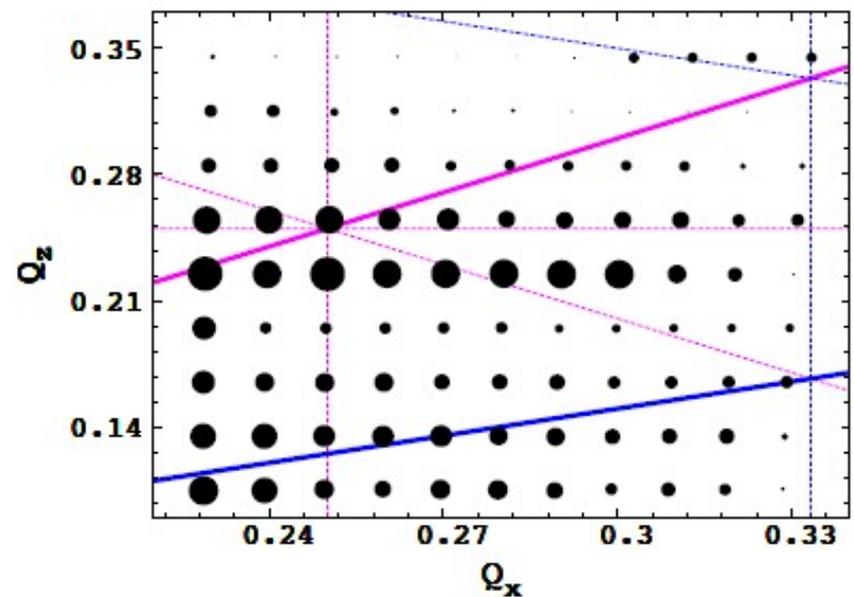
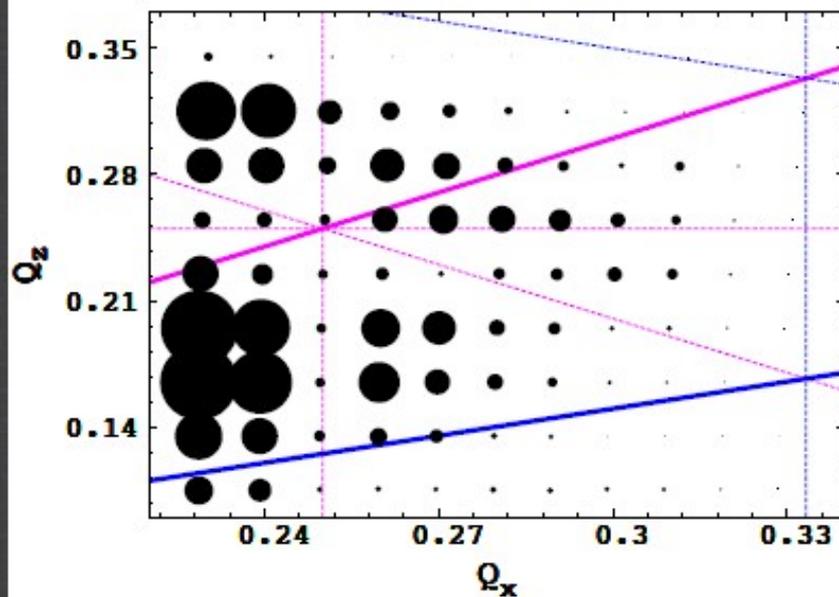
# Phase rotator (3)

Study of DA for new design

10-cell FDF FFAG

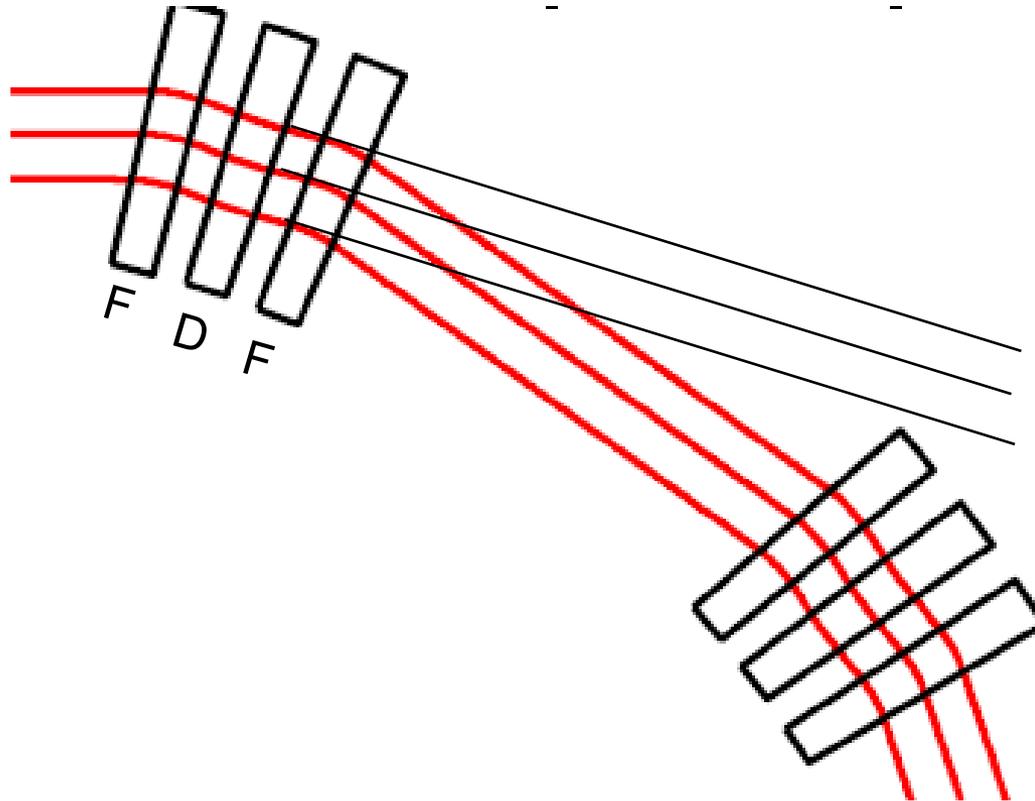
Horizontal

Vertical



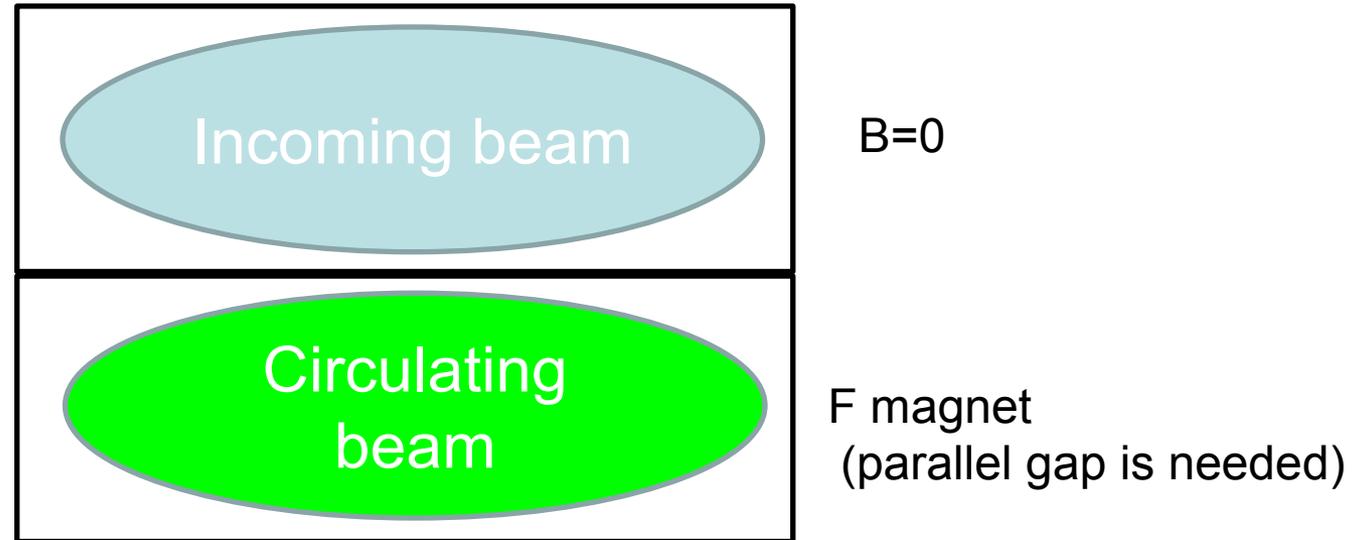
>50 / >3 mm.mrad (H/V) achieved.

# New injection concept (1)



If one could switch off the F magnet...

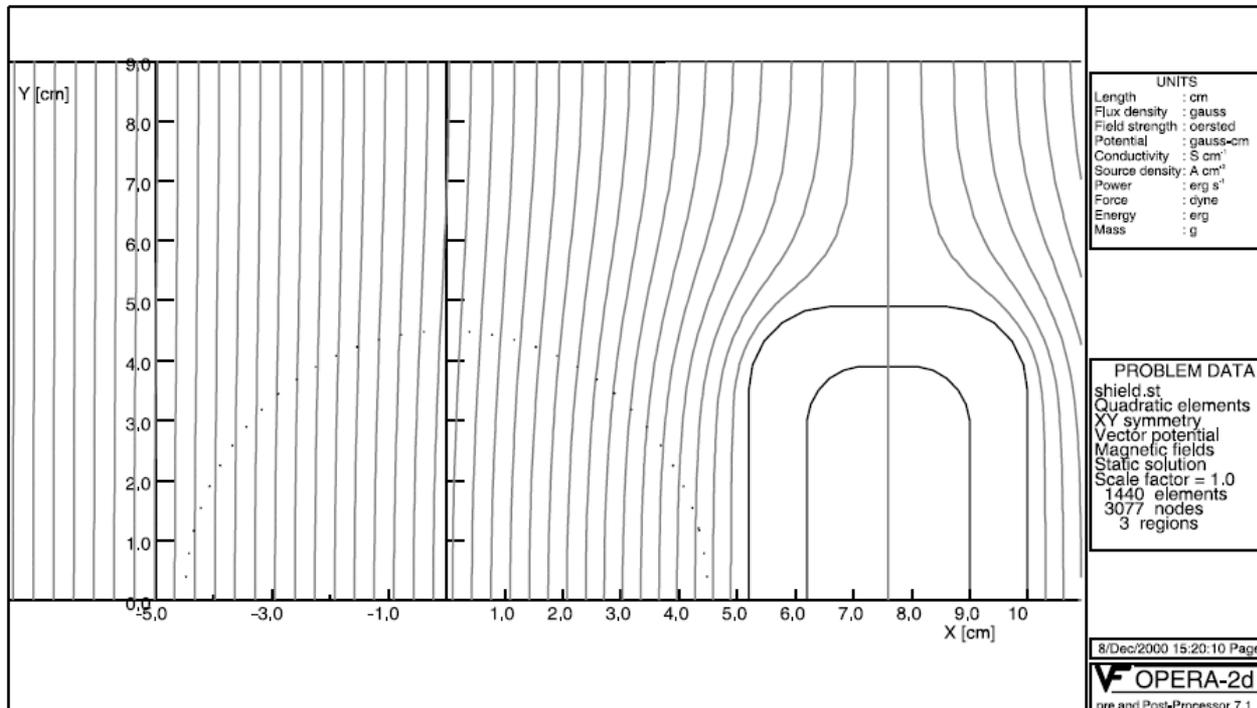
# Inflector, flux shielding channel



Injected beam can be put on orbit using vertical kicker(s).

# Similar ideas have been studied for g-2 experiment

*A. Yamamoto et al. / Nuclear Instruments and Methods in Physics Research A 491 (2002) 23–40*



# Main challenges at present:

- Matching from the solenoid into FFAG
- Injection/Extraction geometries
- Kicker hardware
- Septum magnet
- RF system
- Beam dynamics in FFAG -> we believe we have now improved ring design.

- Vertical injection is proven to be very **challenging** due to huge perturbation caused by the septum magnet(s).
- Concept of the **inflector** effectively “switching off” one of the magnets followed by vertical kicker looks promising.
- The new FDF ring seems to be performing very well, further optimisation studies are needed.
- **PRISM is becoming a serious choice for the next generation cLFV experiment.**