



WILLIAM & MARY

CHARTERED 1693



## **MINERvA Recent Results On the Cross Section Road**

**Edgar Valencia-Rodriguez**

On Behalf the MINERvA Experiment  
September 25, 2017

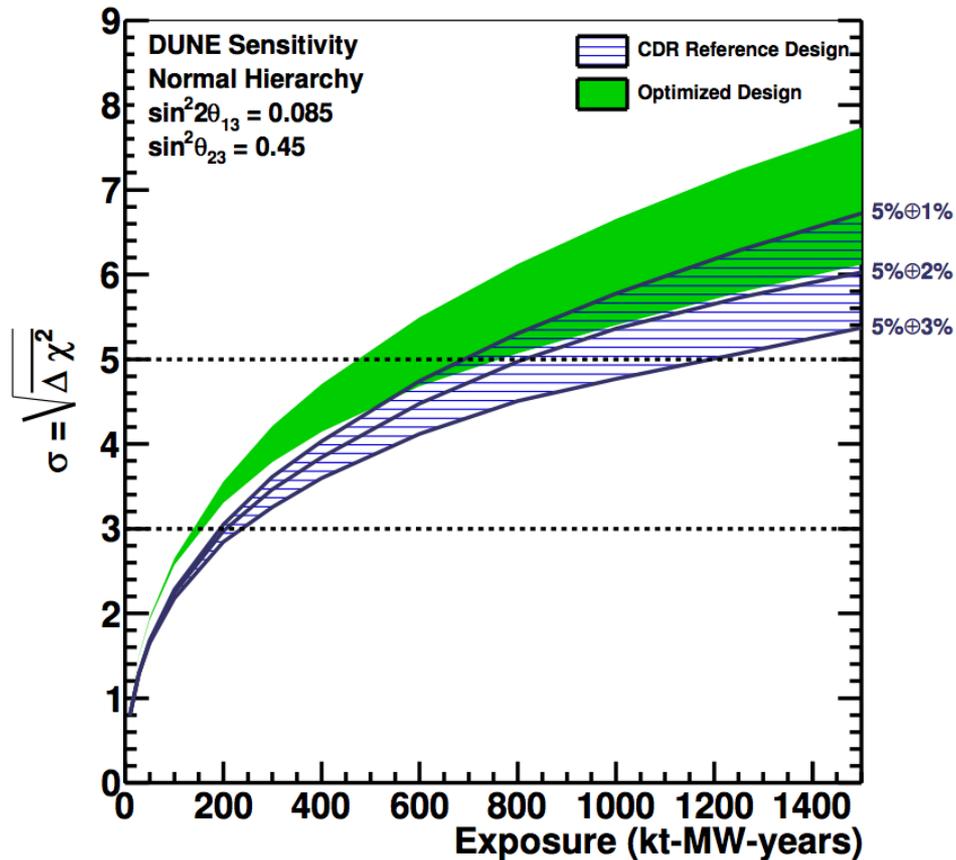


# Introduction



DUNE CDR, arXiv:1512.06148

50% CP Violation Sensitivity



- Systematic errors due to neutrino interaction cross sections are a large fraction of the error.
- Reaching low systematics goals requires control of all systematics, e.g. neutrino interaction cross sections.
- Accelerator-based oscillation experiments rely on neutrino-nucleus interaction models in neutrino event generators.
- Need high precision data to improve Models: MINERvA goals



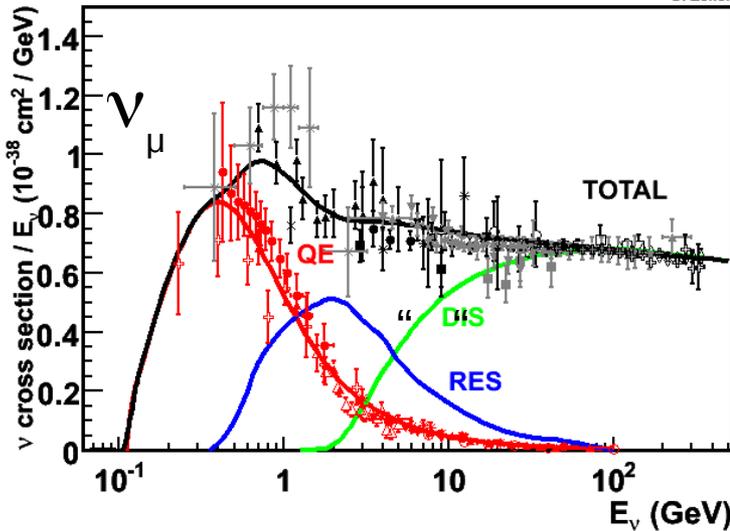
# Introduction

## Charge Current Interactions

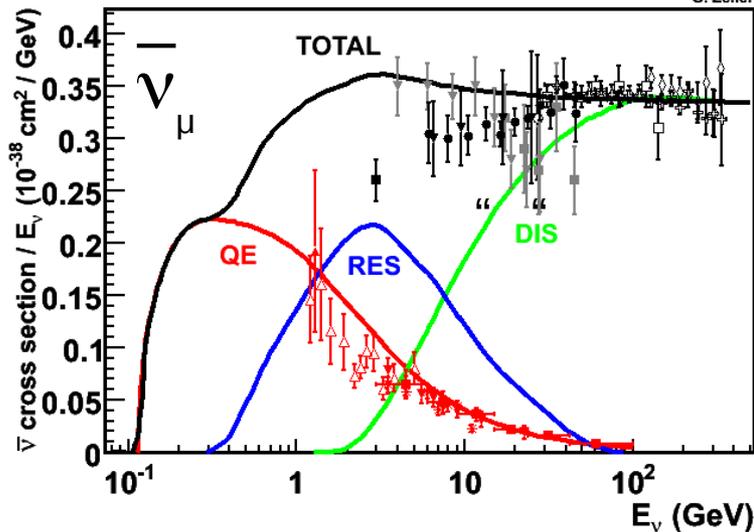


Rev. Mod. Phys. 84, 1307–1341 (2012)  
(includes MiniBooNE results)

G. Zeller

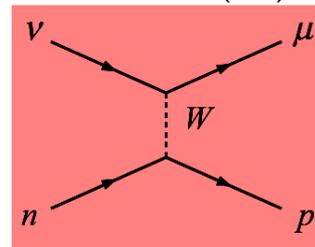


G. Zeller

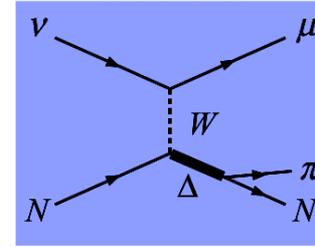


- Oscillation experiments (DUNE, NOvA, T2K, etc.) measure neutrino energy  $E_\nu$  in the 0.5-20 GeV region, where many interactions channels are open.
- This energy range is complicated.
- These interactions channels are signal and the majority of backgrounds in the oscillation experiment.

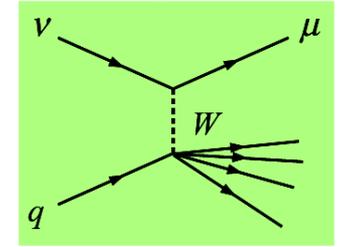
Quasielastic (QE)



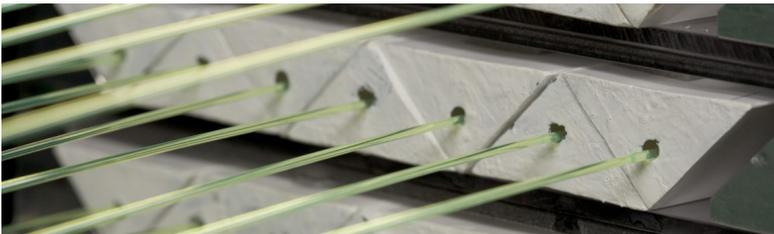
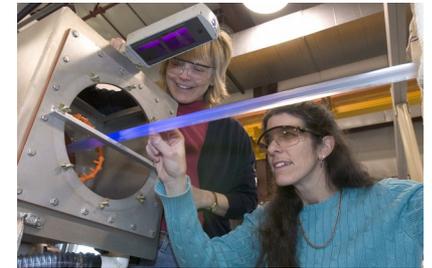
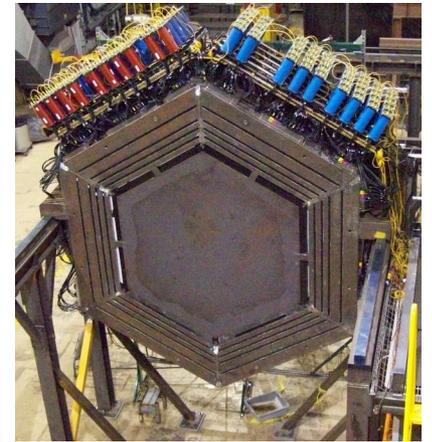
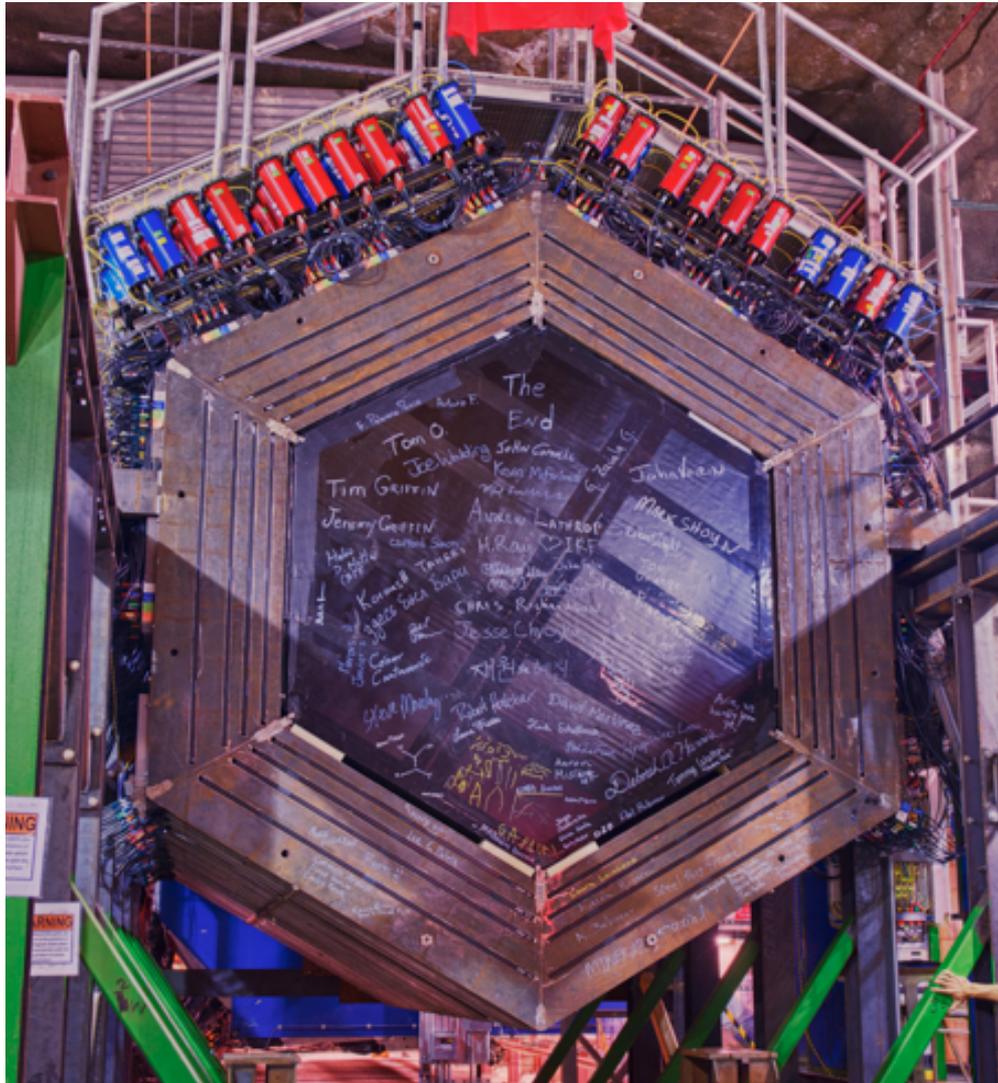
Resonance



DIS



# The MINERvA Experiment





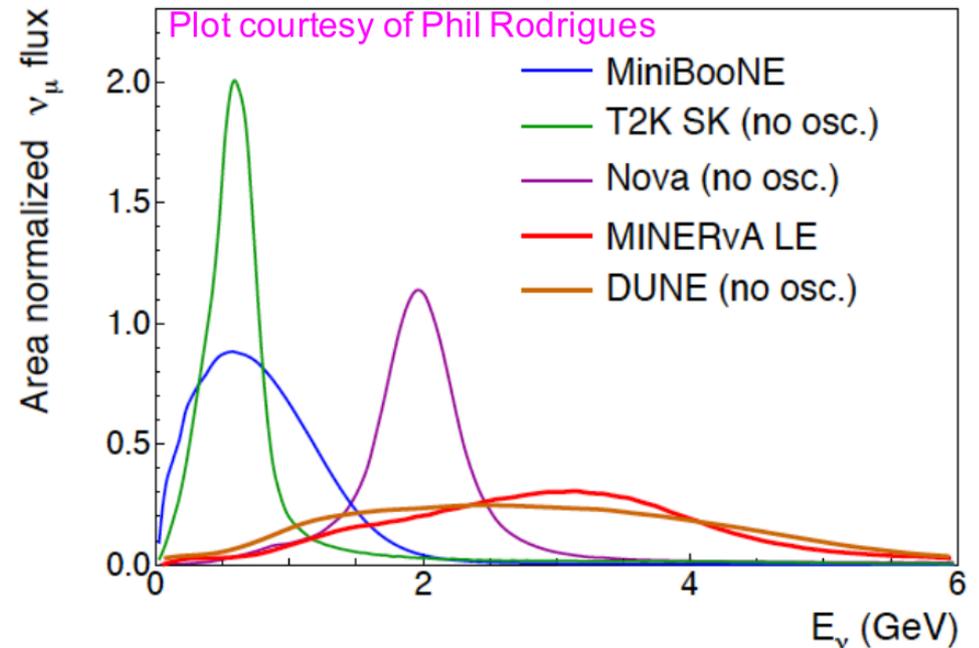
# MINERvA Experiment

## Overview



- High precision measurement of neutrino interactions in  $E_\nu = 0.5 \sim 10$  GeV
- Located  $\sim 100$  m underground at Fermilab in the NuMI beamline.
- Exposed to neutrino/antineutrino beams in several different wide-band tunes
- Many different nuclei in the same beam (He, H<sub>2</sub>O, C, Fe, Pb).
- Inclusive and exclusive final states
- Unique overlap to the DUNE Flux.
- Statistically independent of any oscillation measurement.
- MINERvA's results are very important to improve the modeling in generators.

Dedicated neutrino-nucleus cross-section experiment.



MINERvA  
Main INjector ExperRiment for  $\nu$ -A

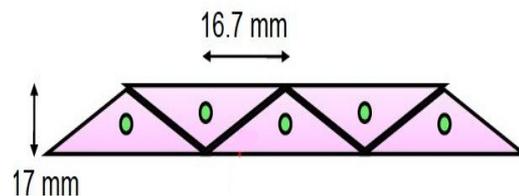
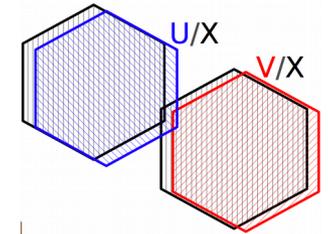
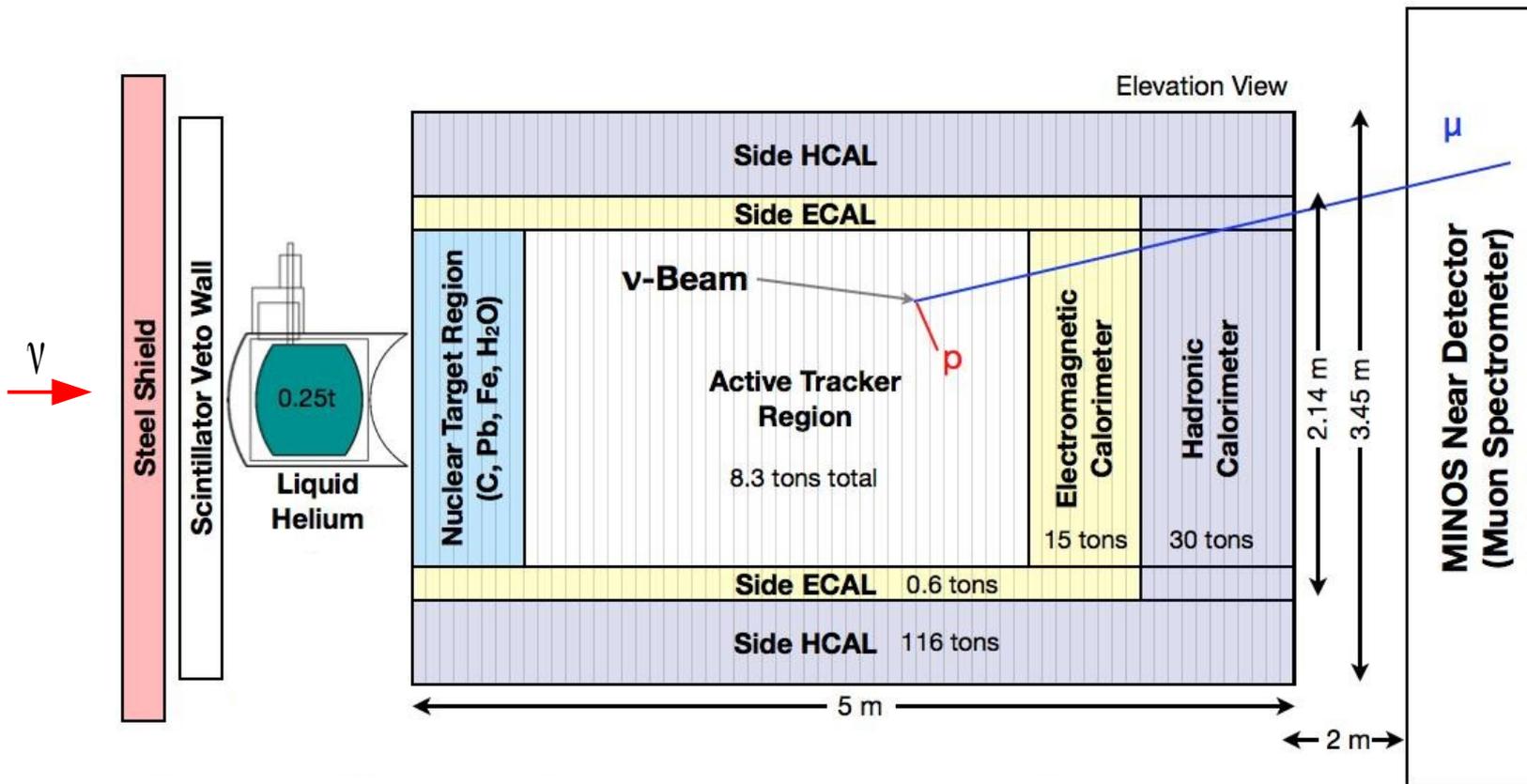


# MINERvA Experiment Detector



Active segmented polystyrene scintillator strips.  
Passive nuclear targets of He, C, Water, Fe and Pb.

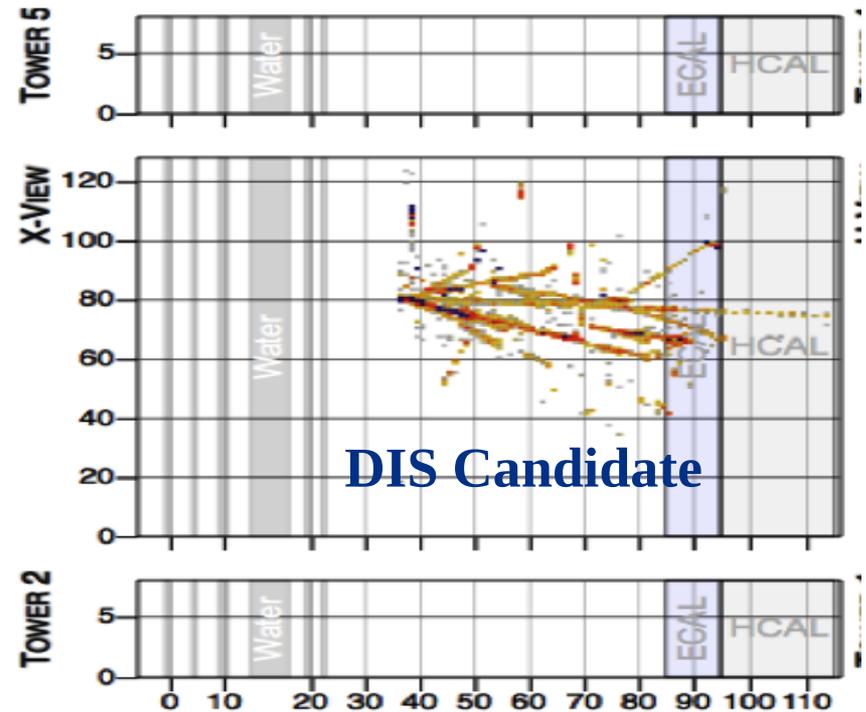
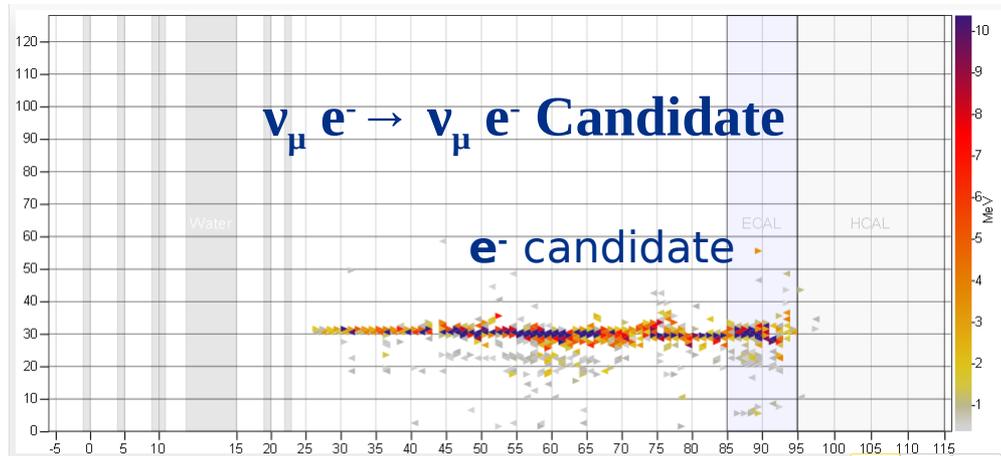
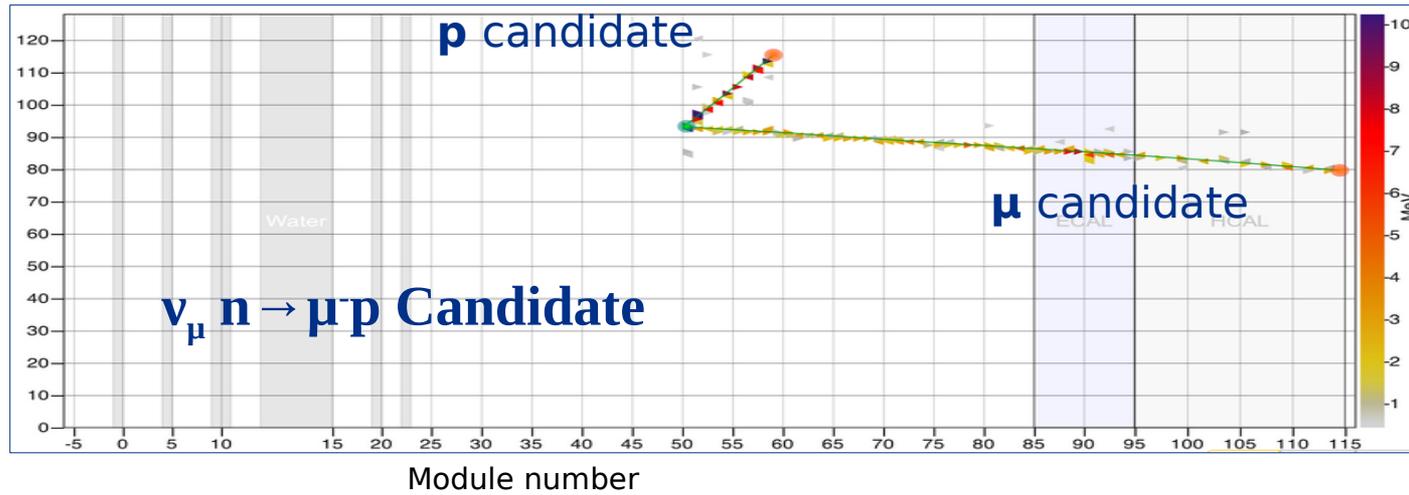
3 strip orientations  
 $-60^\circ, 0^\circ, +60^\circ$



Single Plane Resolution: 2.65 mm.  
Single Hit Timing resolution 4.20 ns.

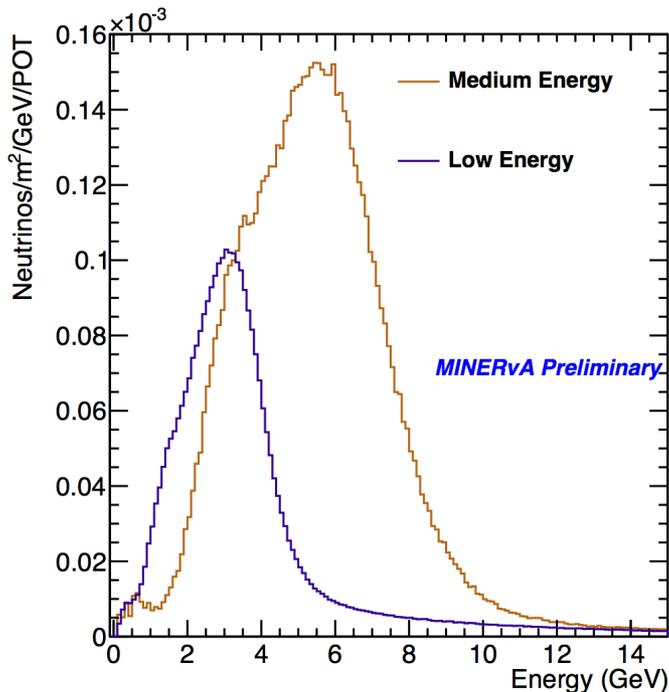
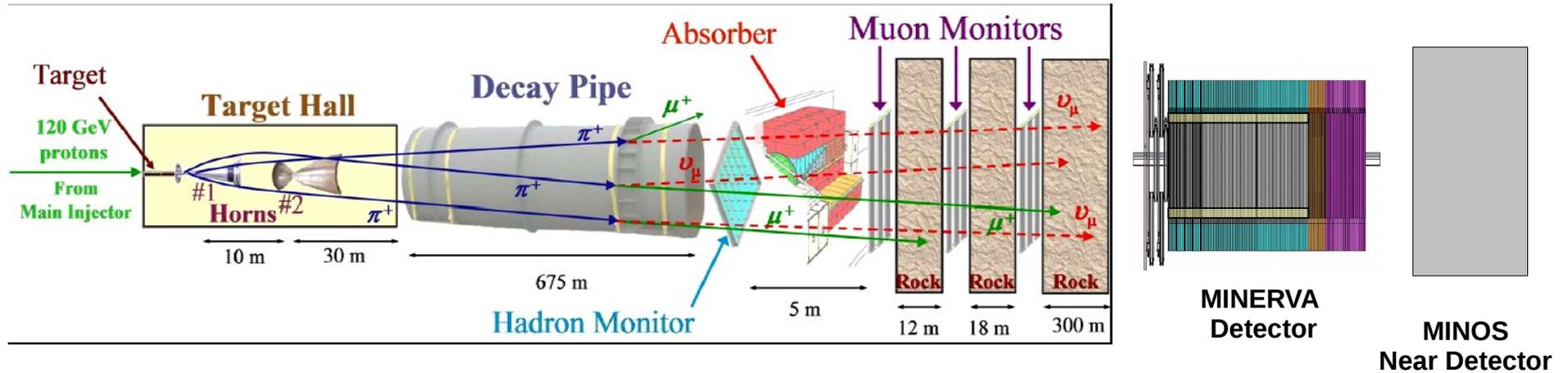


# MINERvA Experiment Event Display





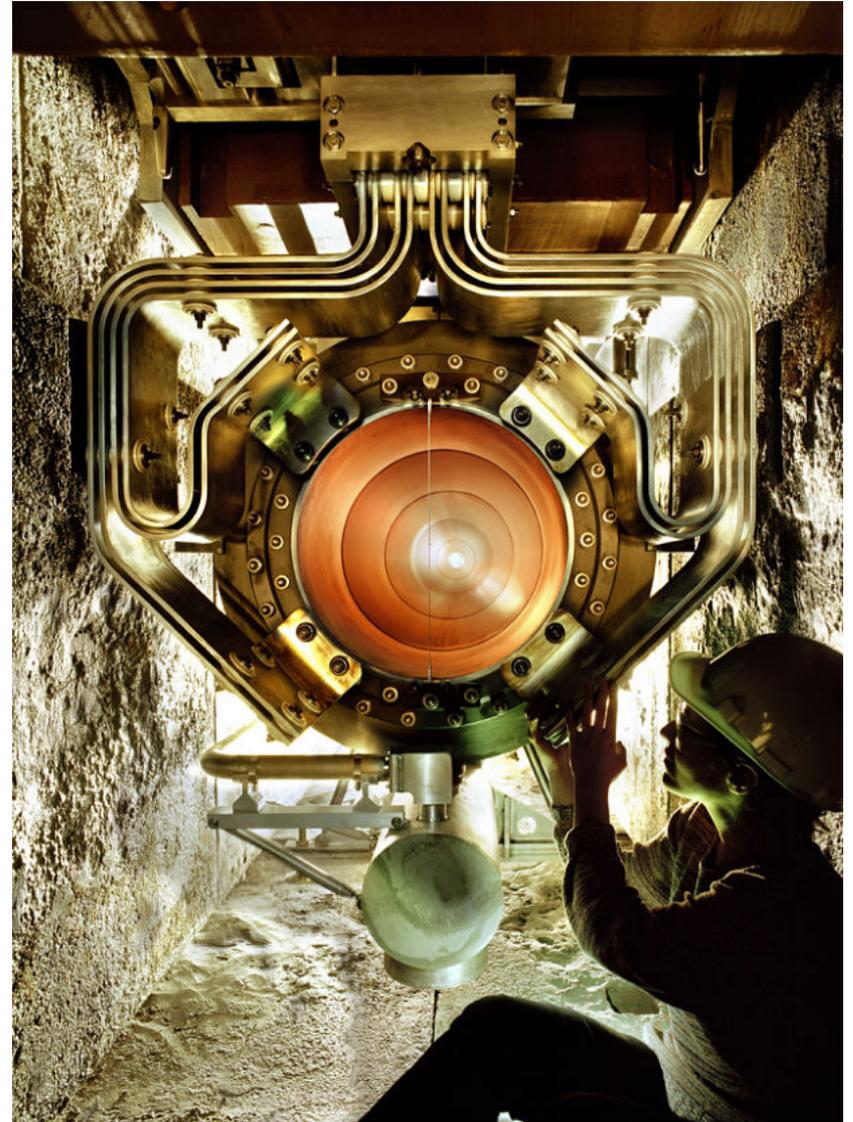
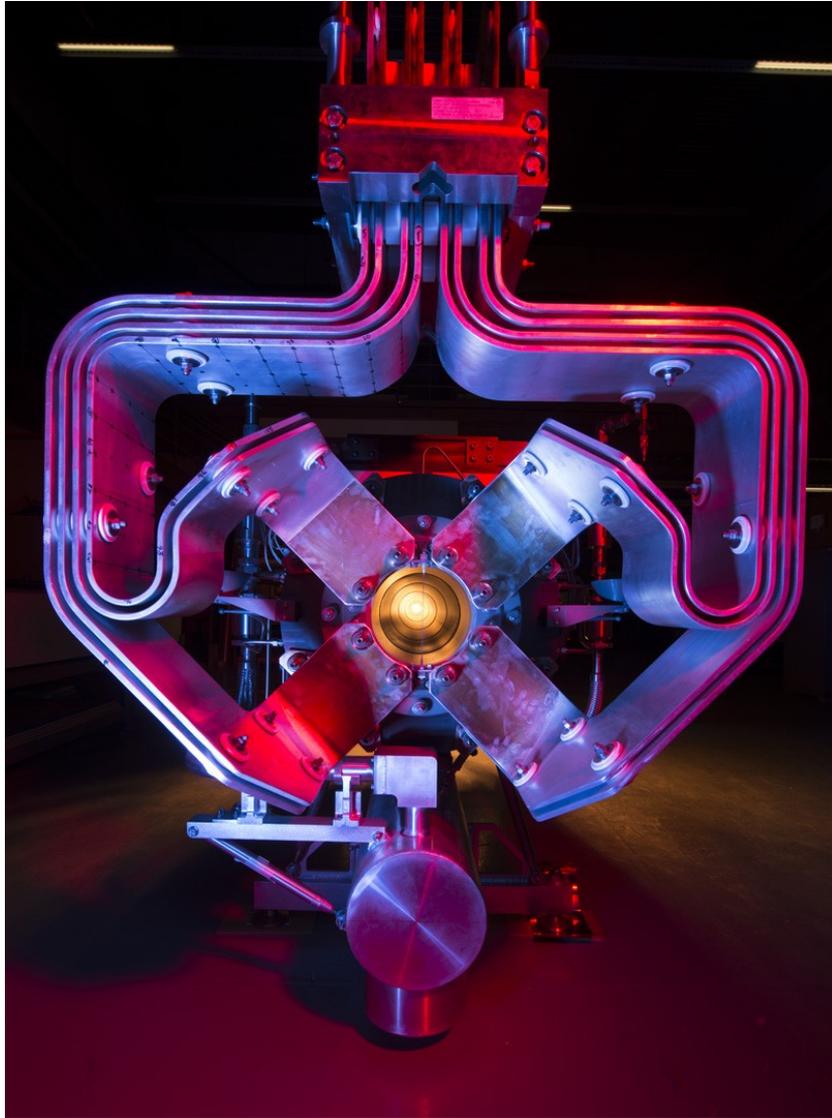
# NuMI Beamline Detector



The NuMI beamline provides the most powerful neutrino flux in the world.

Range	Mode	Exposure (e20 POT)
Low Energy	Neutrino	3.43
Low Energy	Antineutrino	2.01
Medium Energy	Neutrino	9.45
Medium Energy	Antineutrino	Taking Data

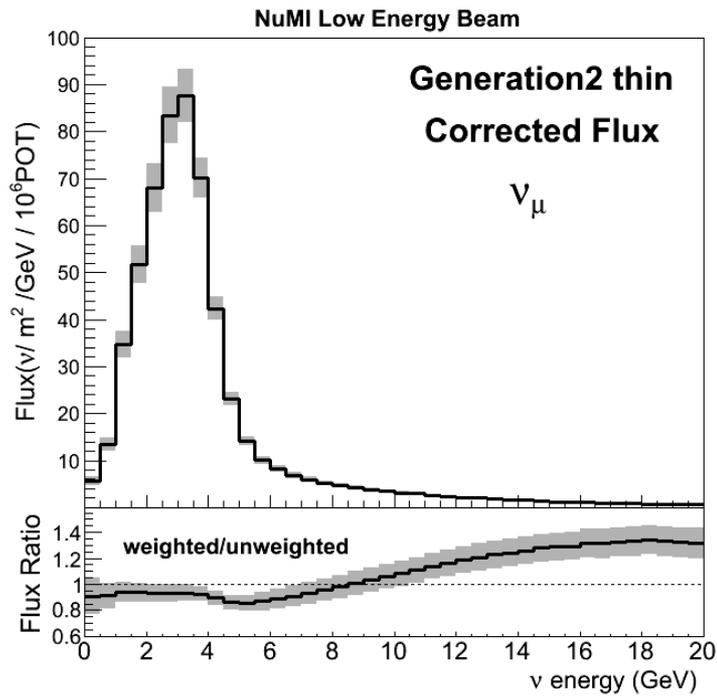
# Determining the Neutrino Flux



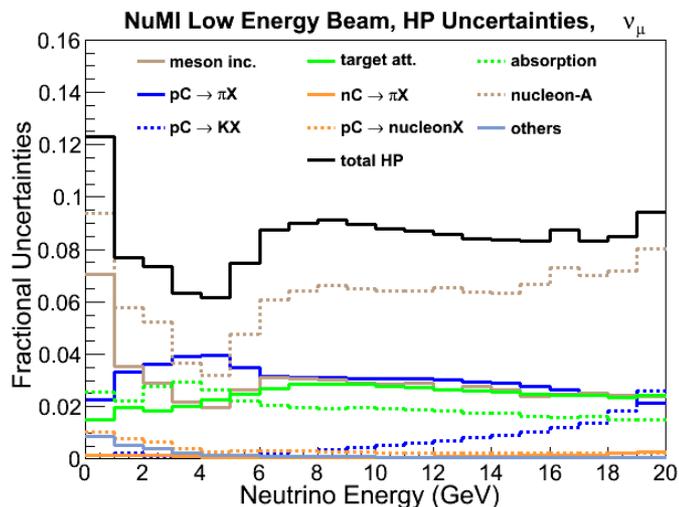


# Flux Predictions Using External Data

Phys. Rev. D 94, 092005 (2016)



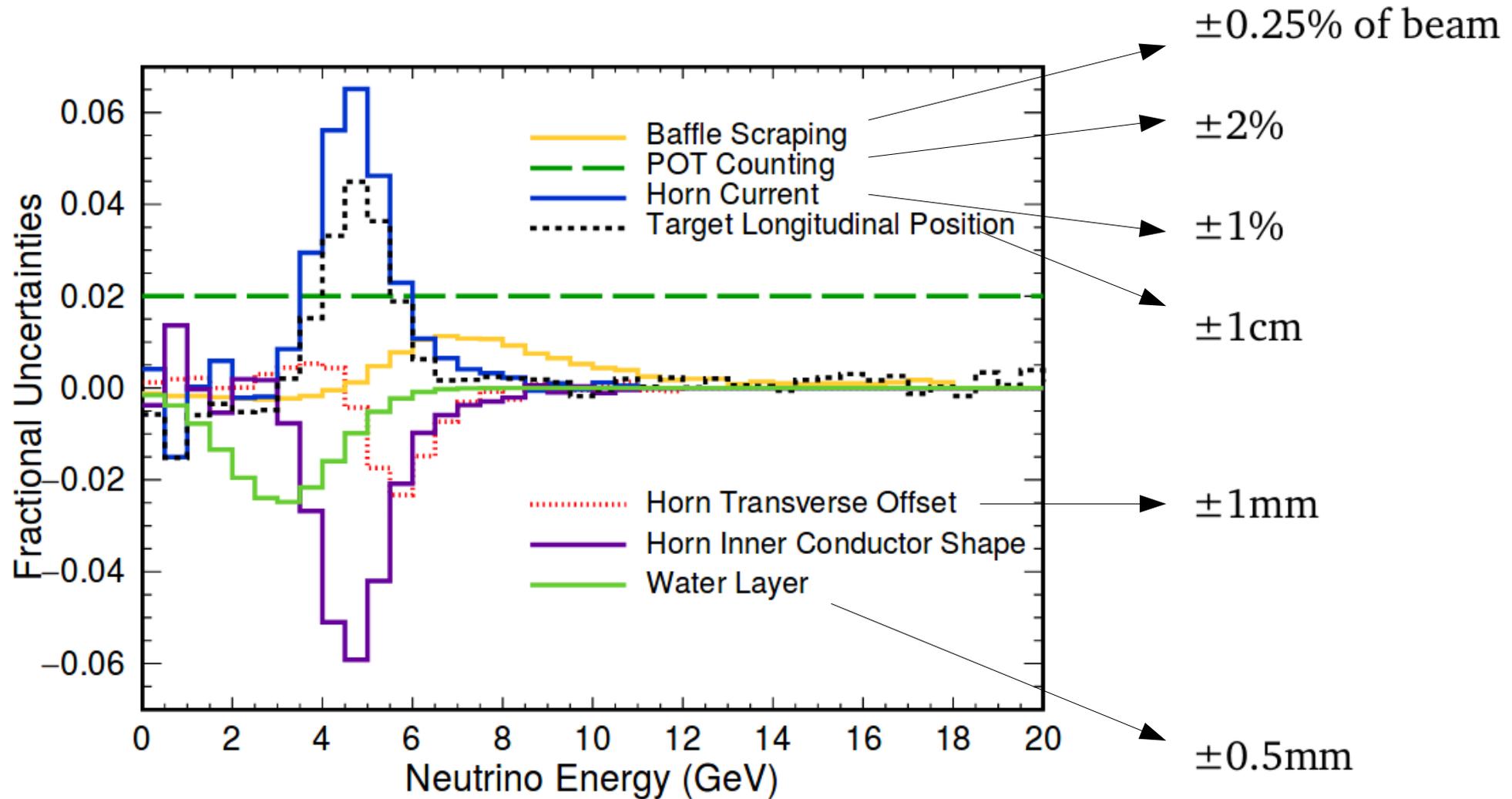
- The flux prediction is made via Geant4 simulation on NuMI beam line with external data from NA49 & NA61 experiments.
- The new flux predictions with its improvements, principal changes to beamline geometry and updates to the simulation called PPFX
- PPFX package available at Fermilab also predicts the DUNE flux.
- We expect ~5% errors for the ME with the addition of constraints from in situ measurements.
- Expect DUNE hadron production uncertainties to look similar, without further hadron production data.





# Flux Predictions Using External Data

## Beam Focusing Uncertainties





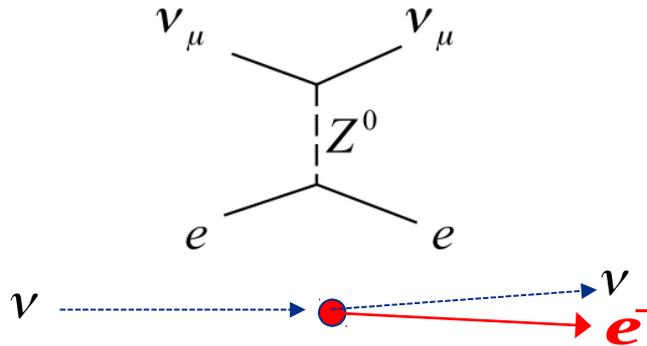
# Flux Constraint from the Internal Data

## Normalization form Neutrino Electron Scattering



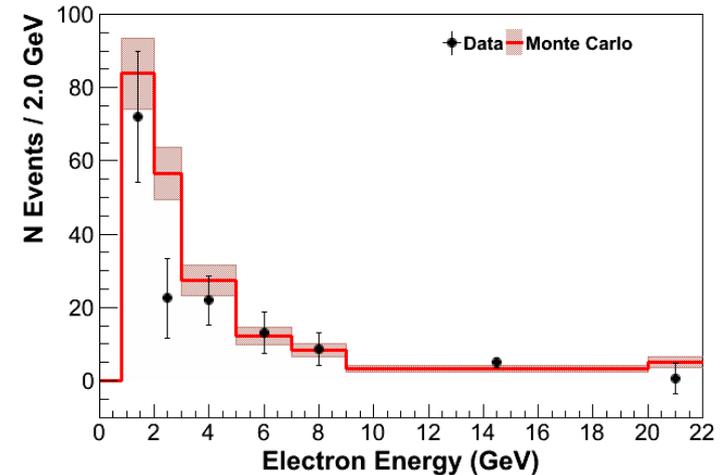
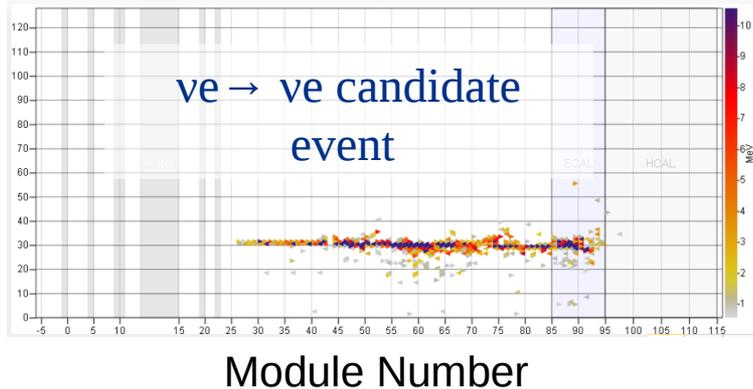
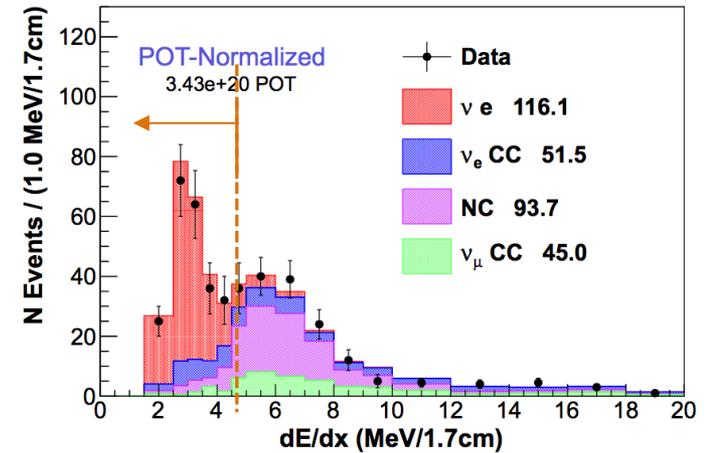
Phys Rev. D 93, 112007 (2016)

Very forward single electron final state



- Well understood electroweak process
- Signal in MINERvA is a single electron moving in the beam direction

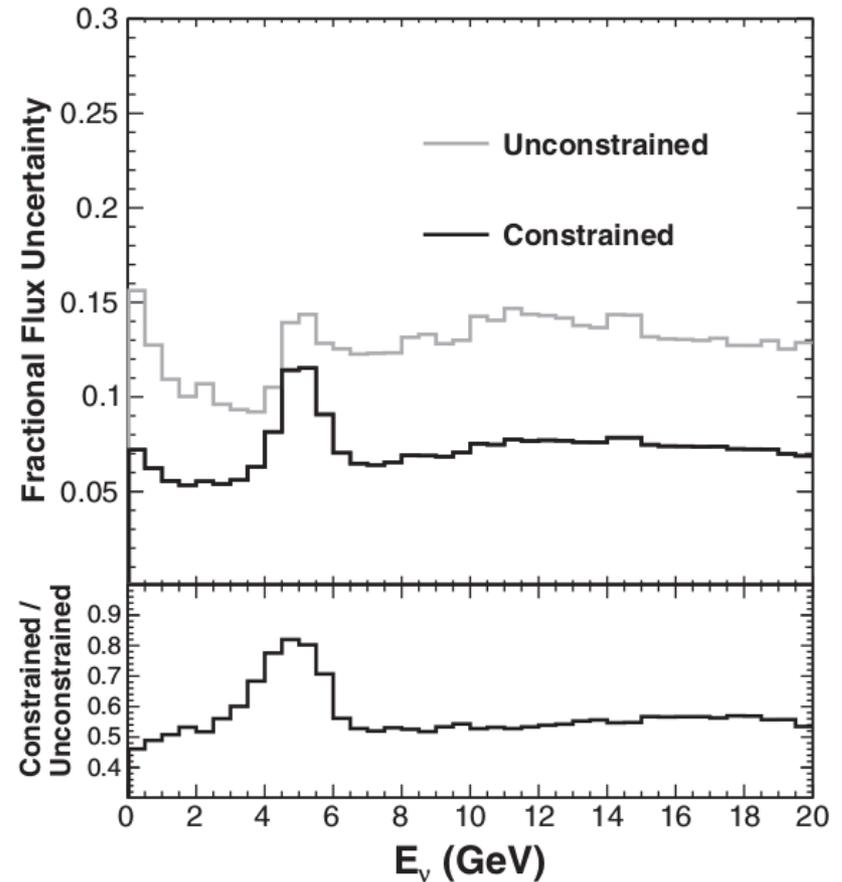
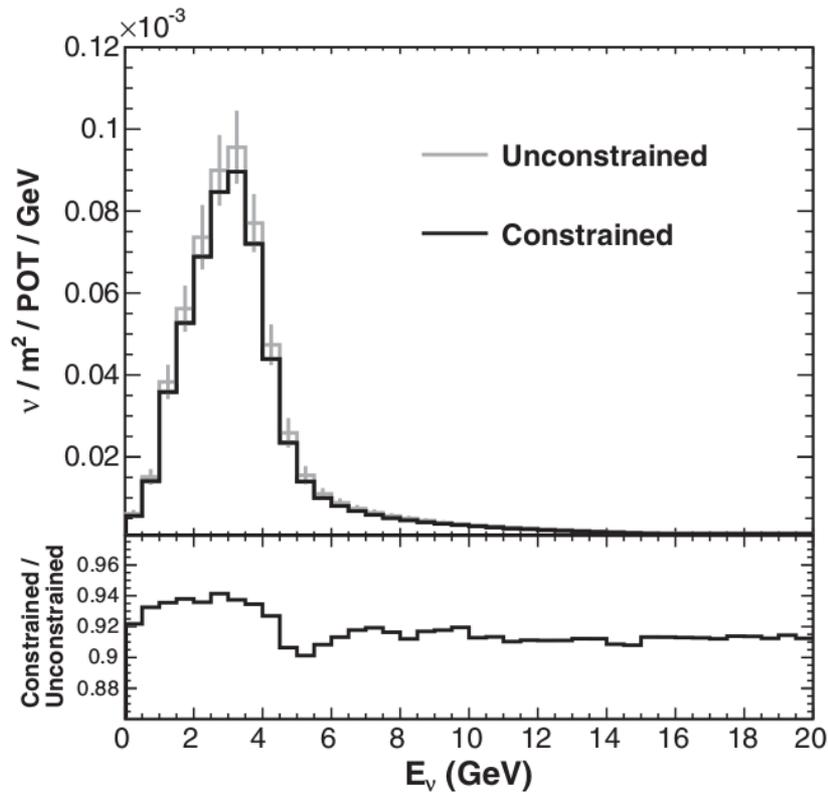
Use early ionization to reject photons and direction to reject interactions on nucleons





# Flux Constraint from the Internal Data

## Normalization from Neutrino Electron Scattering



- This statistically limited result reduces MINERvA's flux uncertainties as a function of energy by 10-20% (of the a priori uncertainties).
- Systematics estimation shows what uncertainties DUNE will need to reduce to achieve 1-2% flux constraint with this method: mostly related to neutrino-nucleus interaction modeling.



# Flux Constraint from the Internal Data

## Flux Shape from Low Nu Scattering

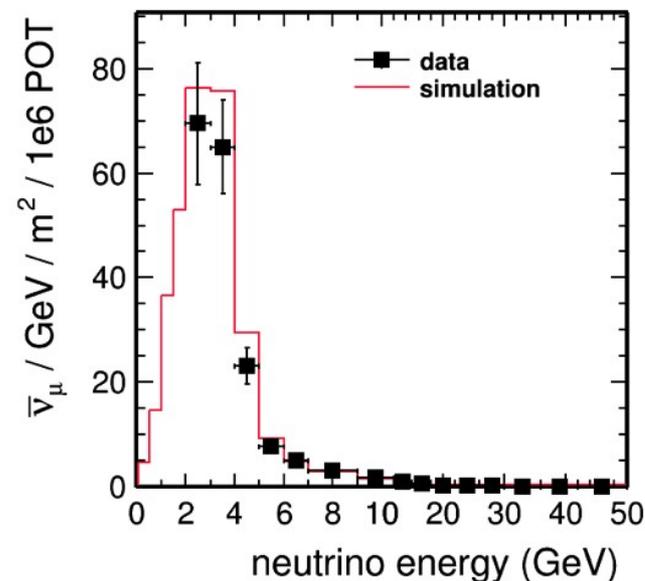
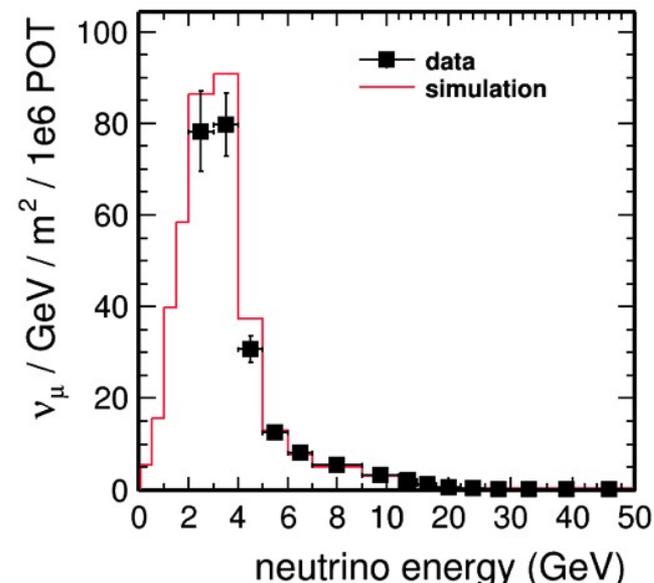


Phys. Rev. D 94, 112007 (2016)

- Charged-current scattering with low hadronic recoil energy  $\nu$  is flat as a function of  $E_\nu$

$$\frac{d\sigma}{d\nu} = A \left( 1 + \frac{B \nu}{A E_\nu} - \frac{C \nu^2}{A 2E_\nu^2} \right)$$

- where A, B, and C depends on Integrals over structure functions or form factors, in the low energy limit.
- Gives a measurement of the flux shape
- Low- $\nu$  method confirms the flux prediction made with external data: PRD 95, 072009(2017), PRD 93, 112007(2016).





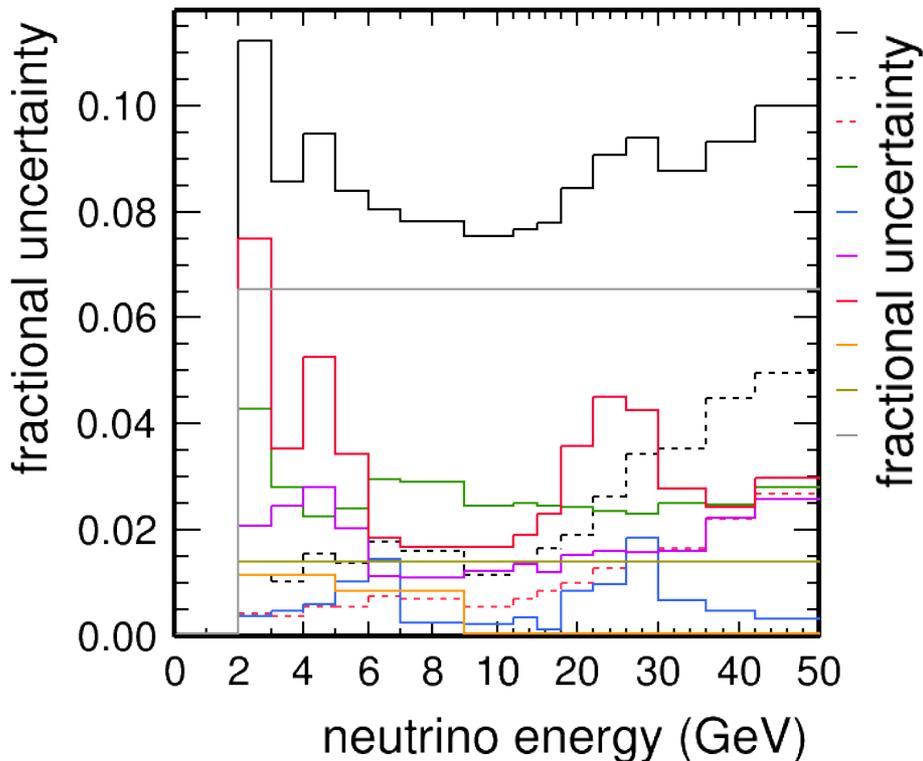
# Flux Constraint from the Internal Data

## Normalization from Low Nu Scattering

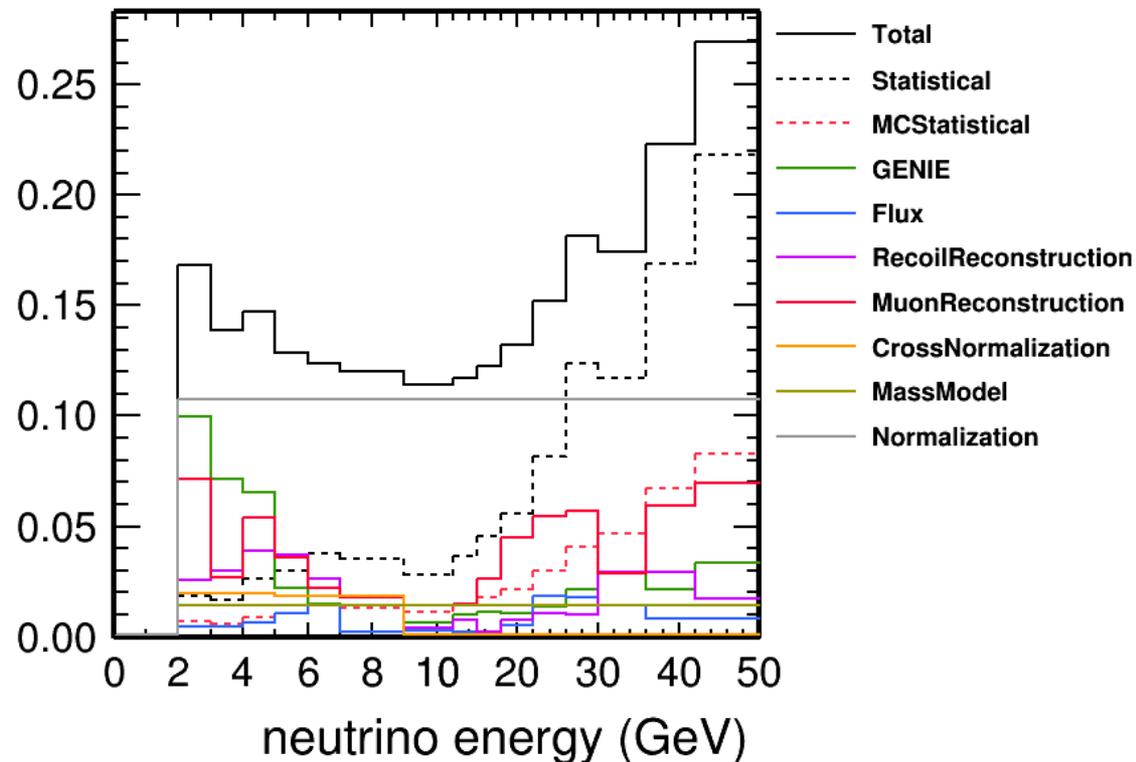


- The external normalization uncertainty dominates over the shape-dependent uncertainties.
- Muon energy reconstruction contributes a significant uncertainty at lower neutrino energies.

$\nu_\mu$  in FHC



$\bar{\nu}_\mu$  in RHC



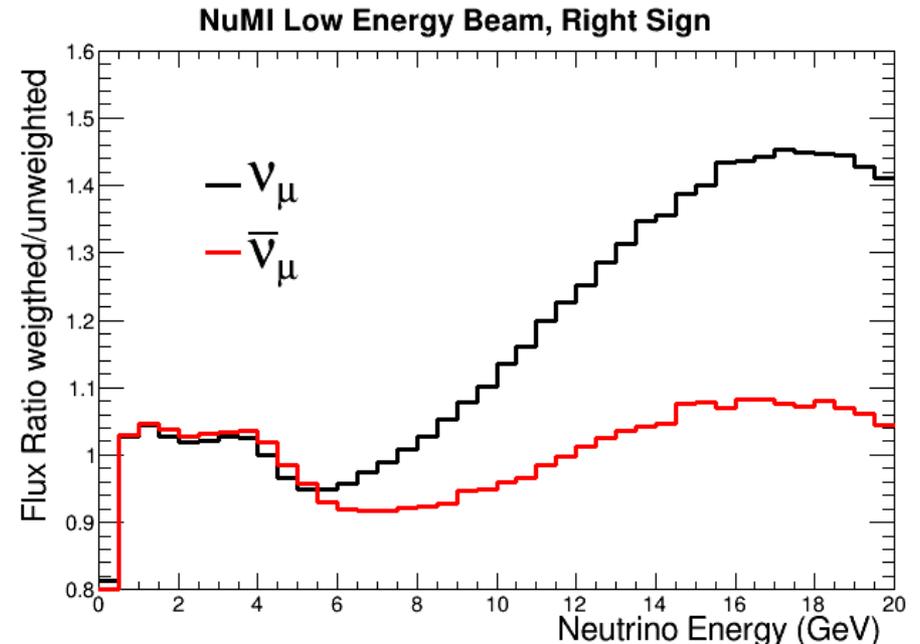
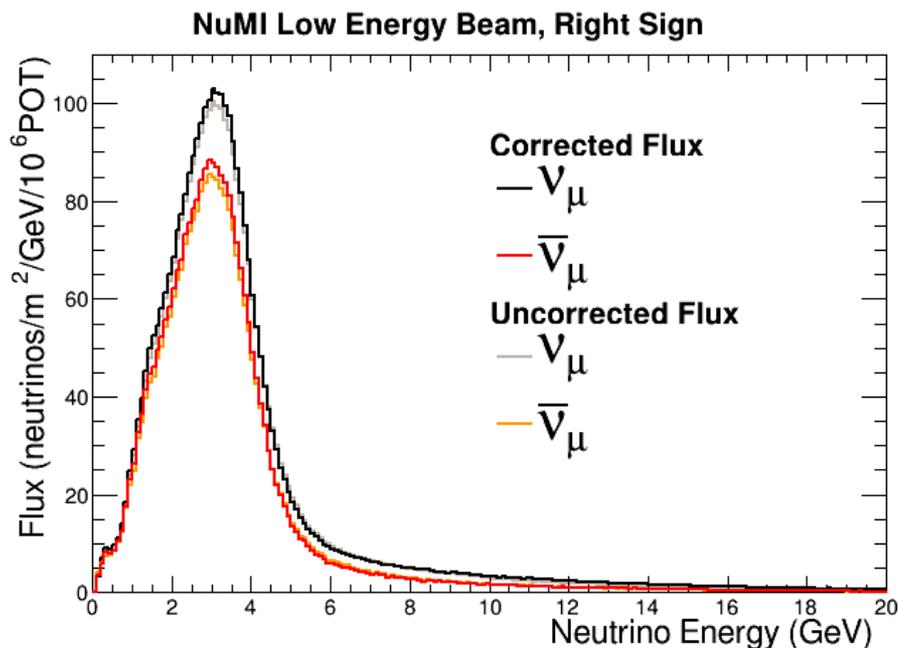


# Flux Constraint from the Internal Data

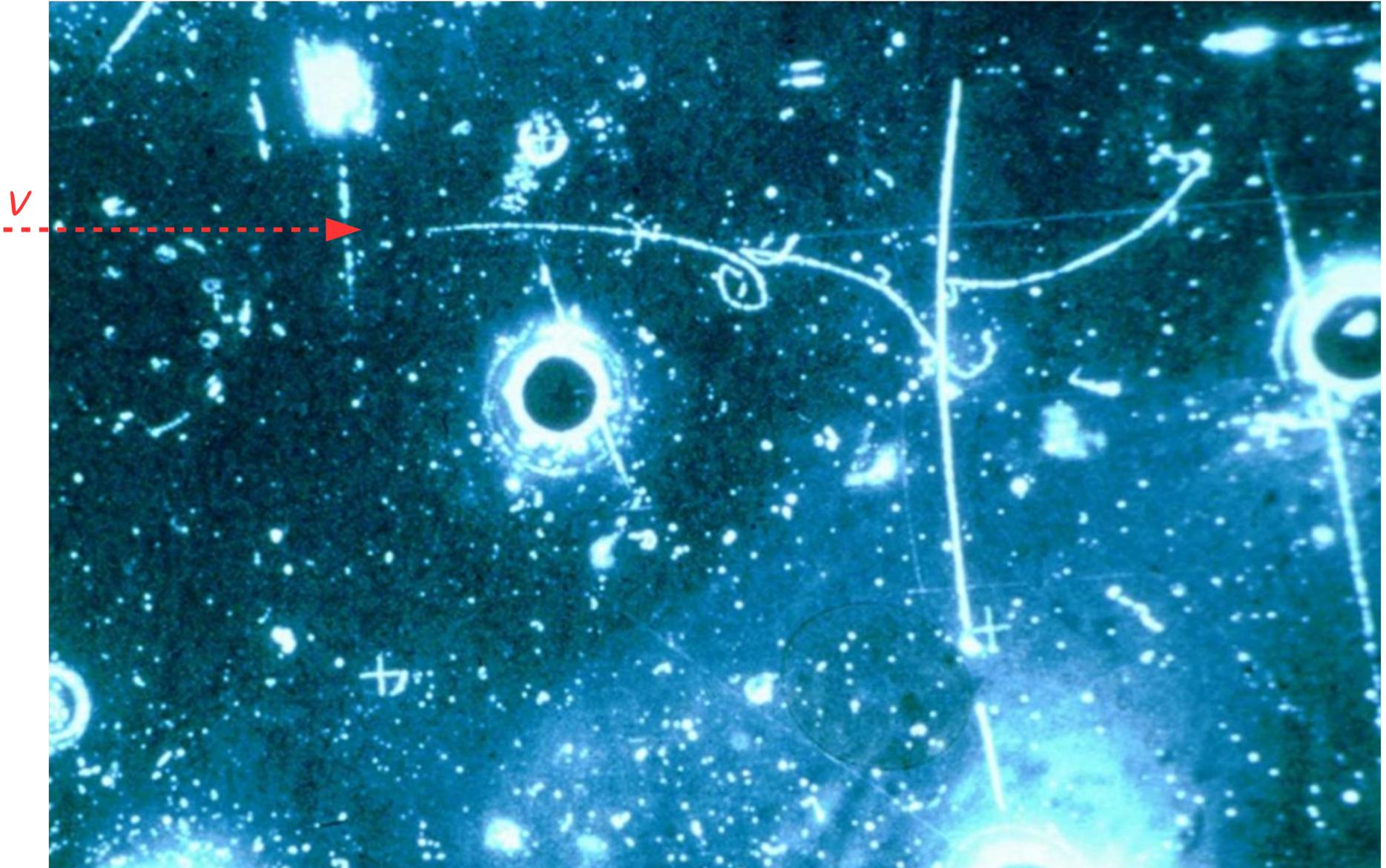
## Normalization from Low Nu Scattering



- A byproduct of this analysis is the  $\nu_\mu$  and  $\bar{\nu}_\mu$  flux measurements, both for the forward and reverse horn polarities that have been used in the Low Energy NuMI beamline configuration.
- This is the first time a low- $\nu$  based technique has been used in the NuMI antineutrino-enhanced beam tune.
- This measurement is the lowest energy application of the low- $\nu$ -flux technique, and demonstrates that the technique is applicable to future neutrino beams operating at few-GeV energies



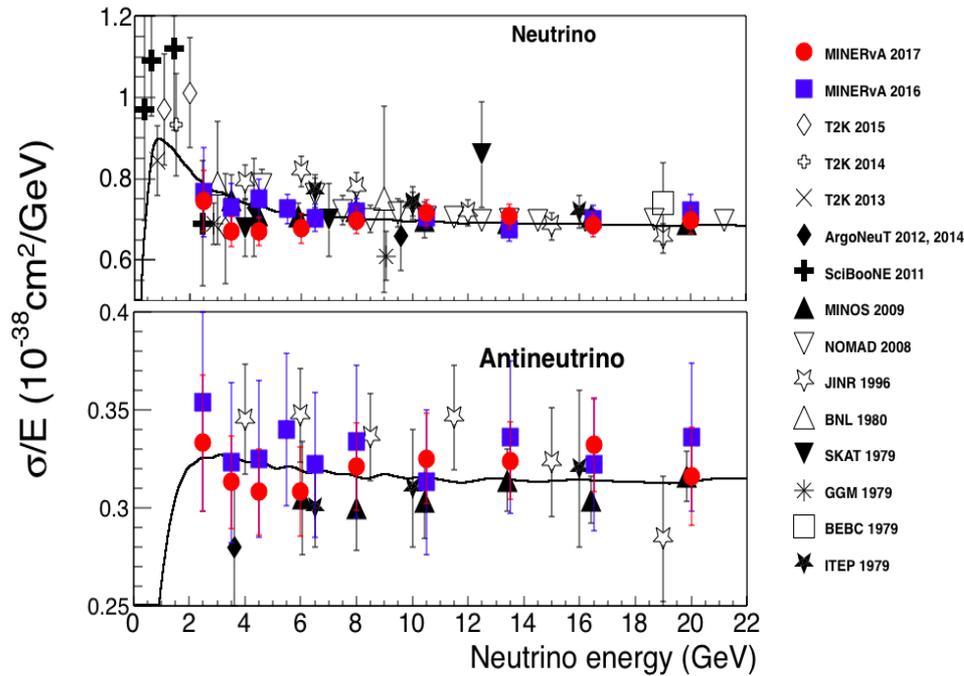
# Cross Sections





# Inclusive CC Scattering

Phys. Rev. D 95, 072009 (2017)

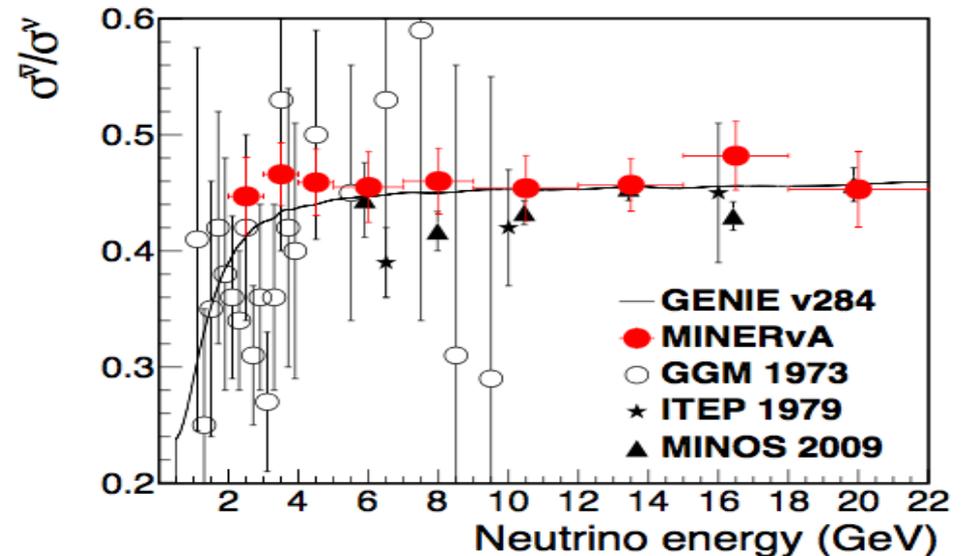


- Antineutrino cross section result is the most precise to date below 6 GeV (errors dominated by statistical precision)
- Shows that the technique is applicable to future neutrino experiments operating at multi-GeV energies

- Long-Baseline oscillation experiments will measure a ratio of oscillation probabilities to constraint CP violation.

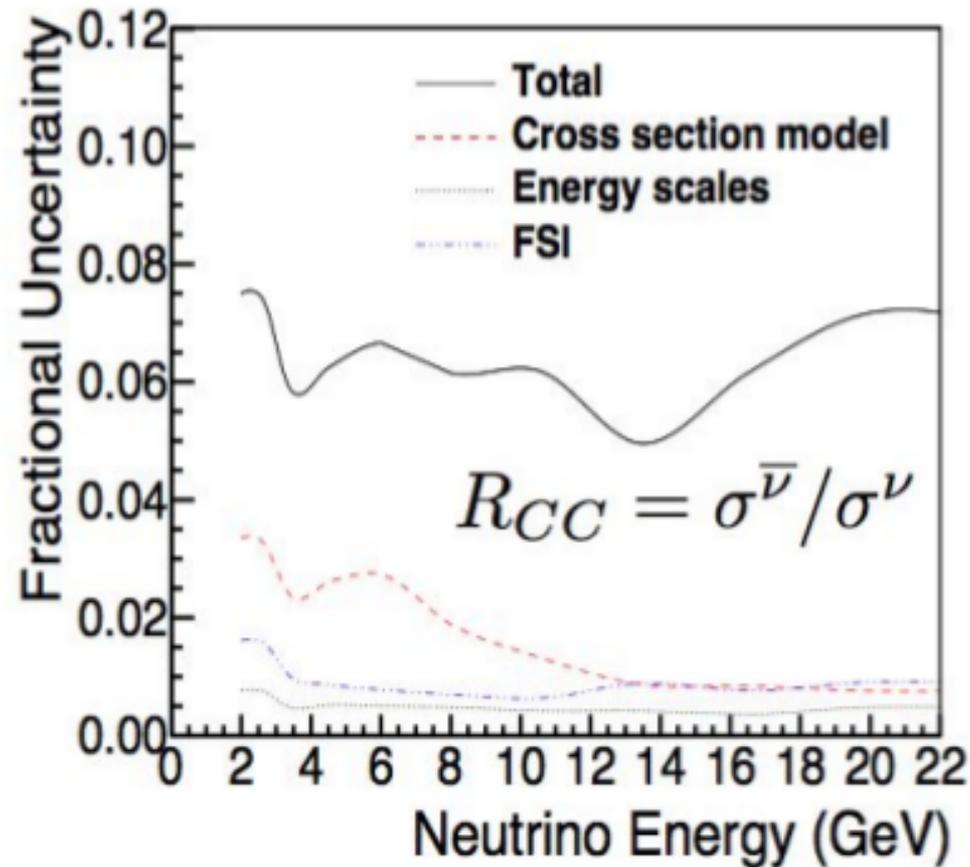
$$A_{CP} = \frac{P(\nu_{\mu} \rightarrow \nu_e) - P(\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e)}{P(\nu_{\mu} \rightarrow \nu_e) + P(\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e)}$$

- New precise  $\sigma_{\nu}/\sigma_{\bar{\nu}}$  ratio relevant to  $\delta_{CP}$  measurement using the Low Nu Method.





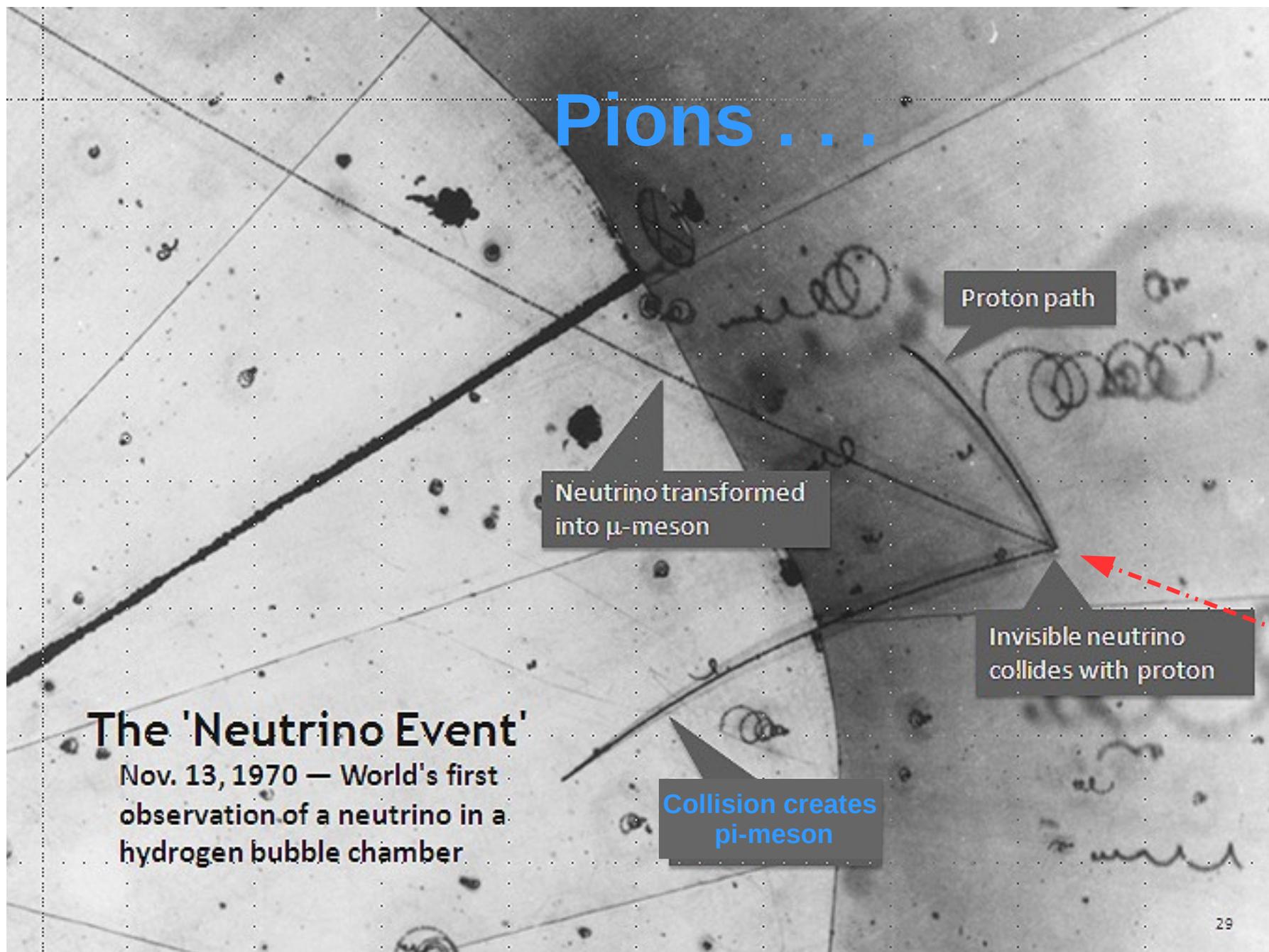
# Inclusive CC Scattering Systematics Uncertainties



## › Ratio

- › Common systematics of neutrino and antineutrino cross sections partially cancel in the ratio.
- › Statistical uncertainty dominates

# Pions . . .



Neutrino transformed into  $\mu$ -meson

Proton path

Invisible neutrino collides with proton

Collision creates pi-meson

## The 'Neutrino Event'

Nov. 13, 1970 — World's first observation of a neutrino in a hydrogen bubble chamber



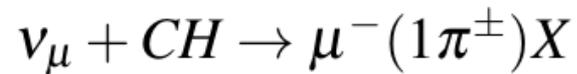
# Neutrino and Antineutrino Single Pions Production

Phys. Rev. D 94, 052005 (2016)

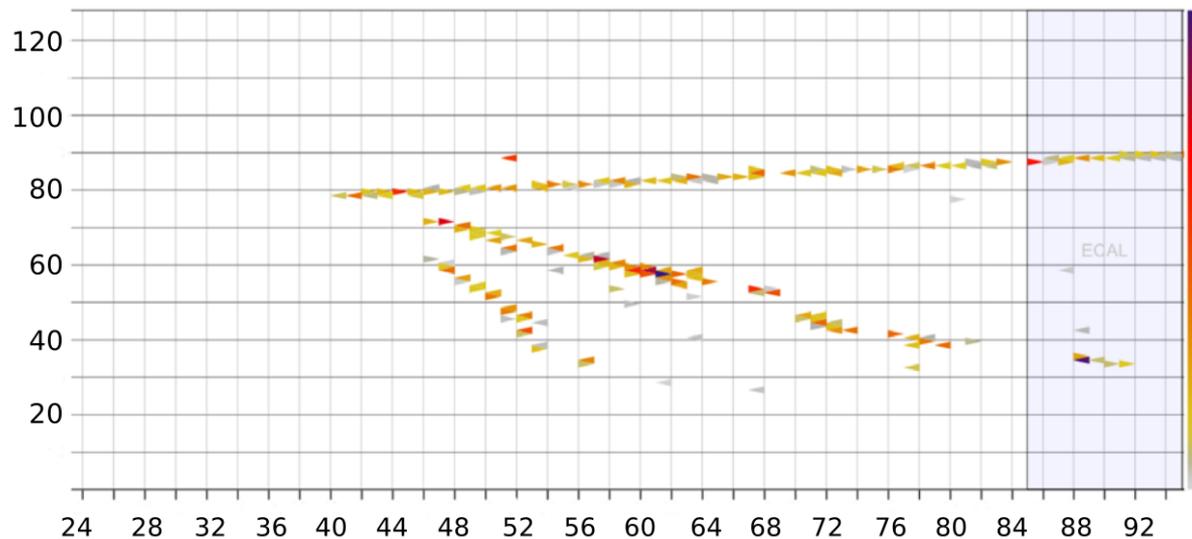
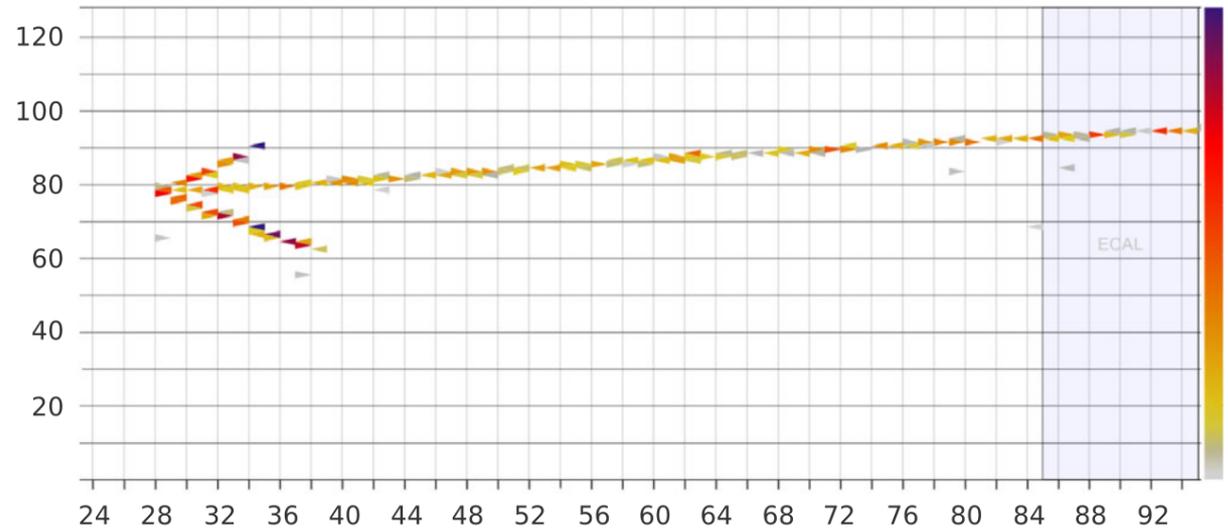


## Neutrino

Single charged pion production

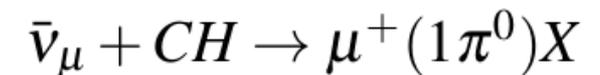


$X$  can contain any number of  $\pi^0$ s,  
no charged pions



## Antineutrino

Single neutral pion production



$X$  contains no mesons



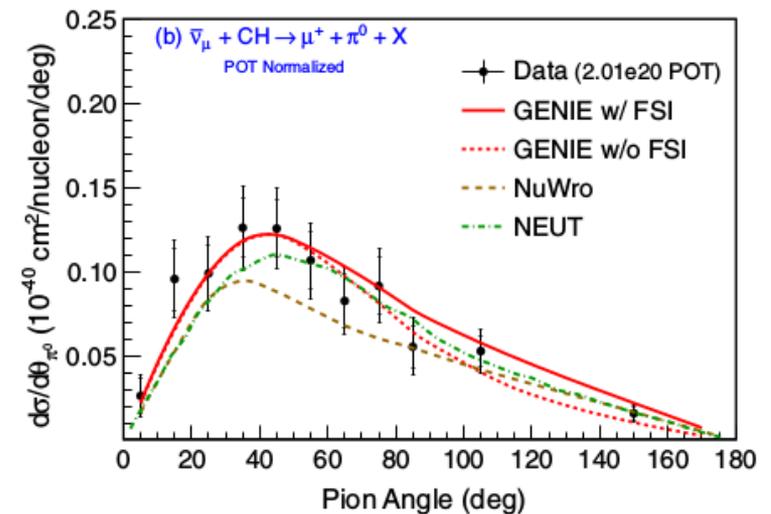
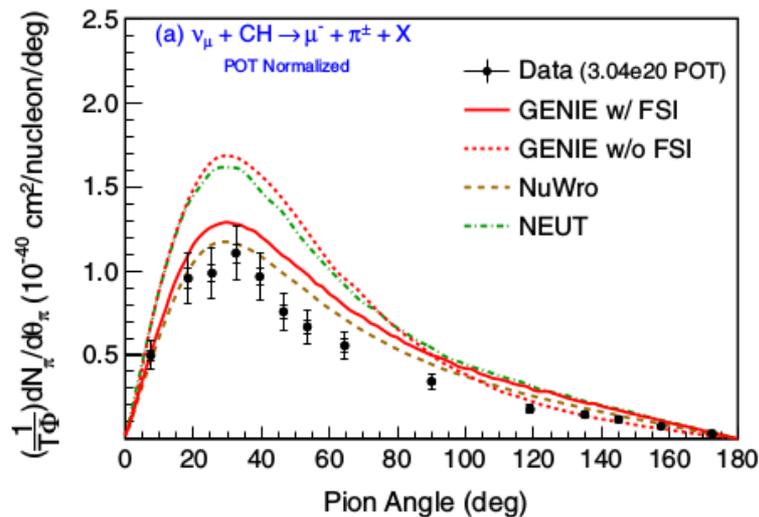
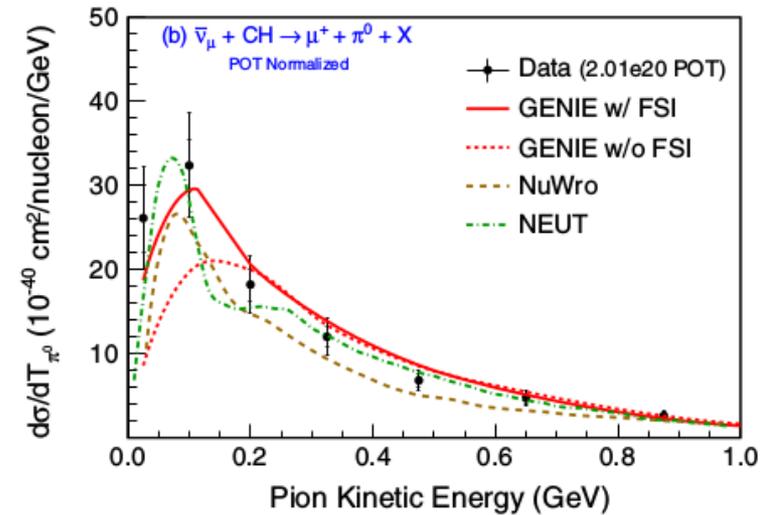
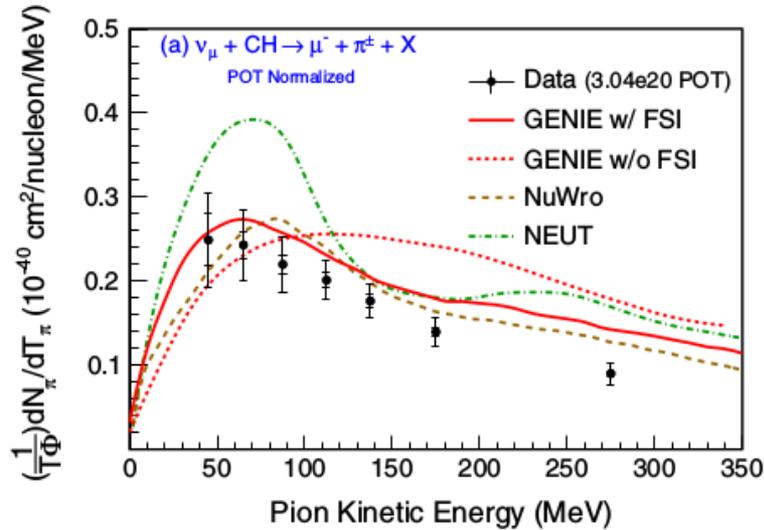
# Neutrino and Antineutrino Cross Section from Pions

## Generators Comparison



Phys. Rev. D 94, 052005 (2016)

- Shape of charged current pion production cross section versus pions kinematics is independent of FSI model.



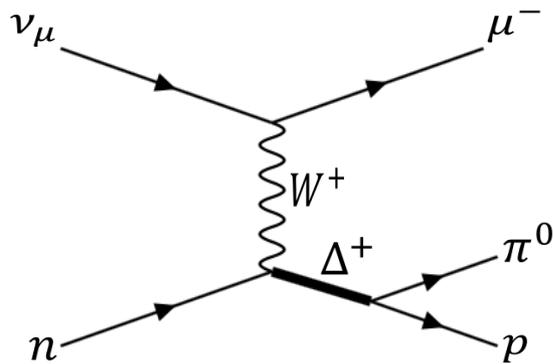


# $\nu_\mu$ CC Single $\pi^0$ Production

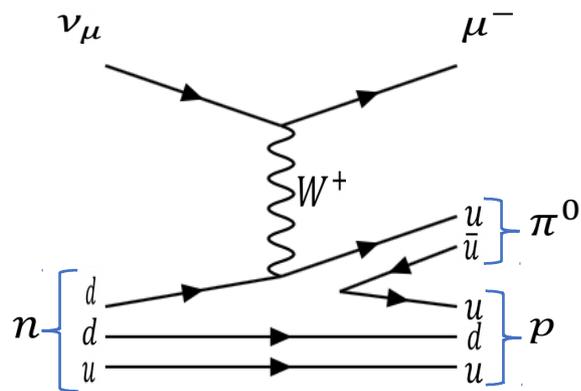
arXiv:1708.03723



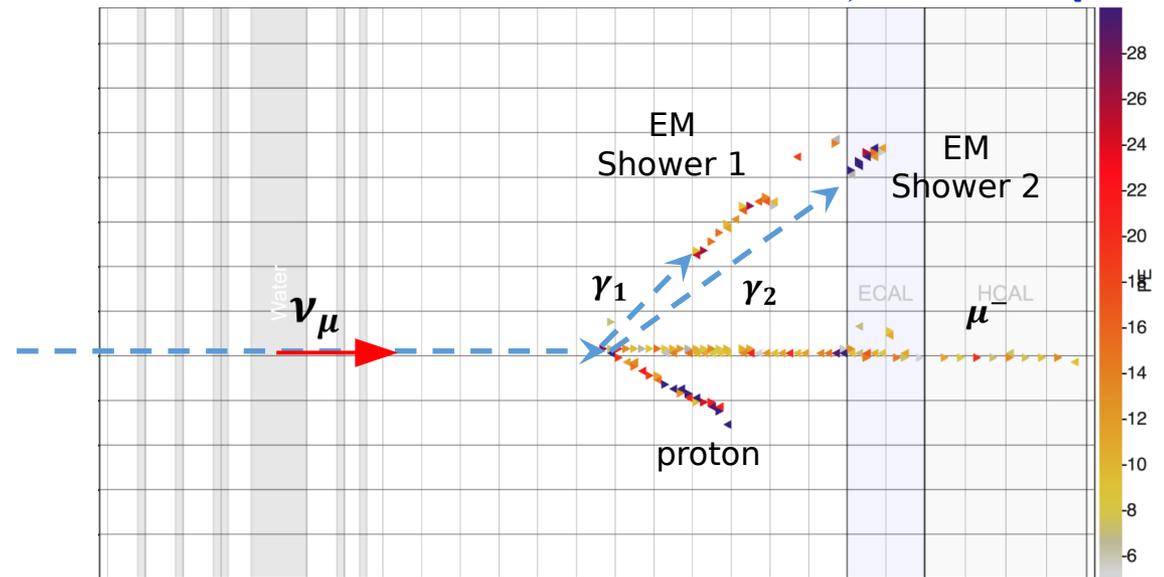
## Baryon Resonance Production $\Delta^+(1232)$ , higher-mass $N^*$



## Non-Resonant Production and Deep Inelastic Scattering



Example:  $\nu_\mu + \{n\}_C \rightarrow \mu^- + \pi^0 + p$   
 $\pi^0 \rightarrow 2\gamma$



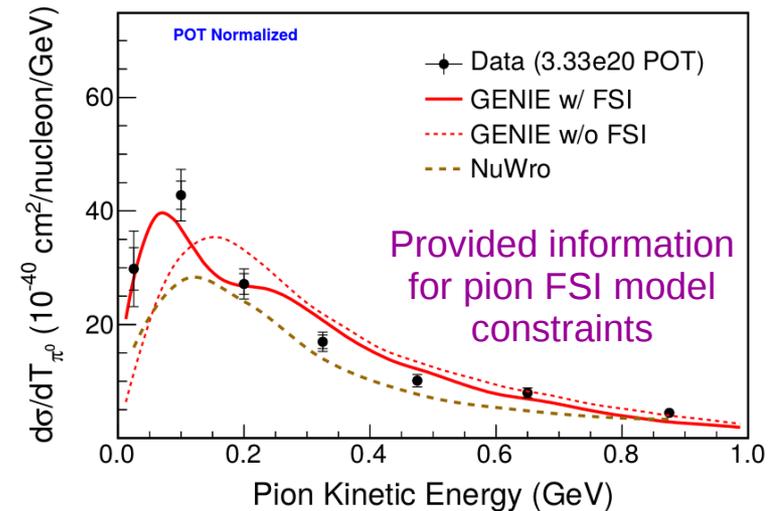
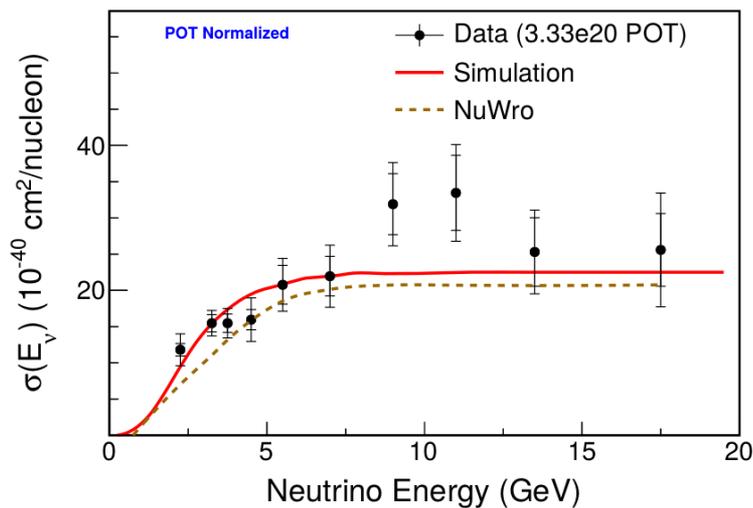
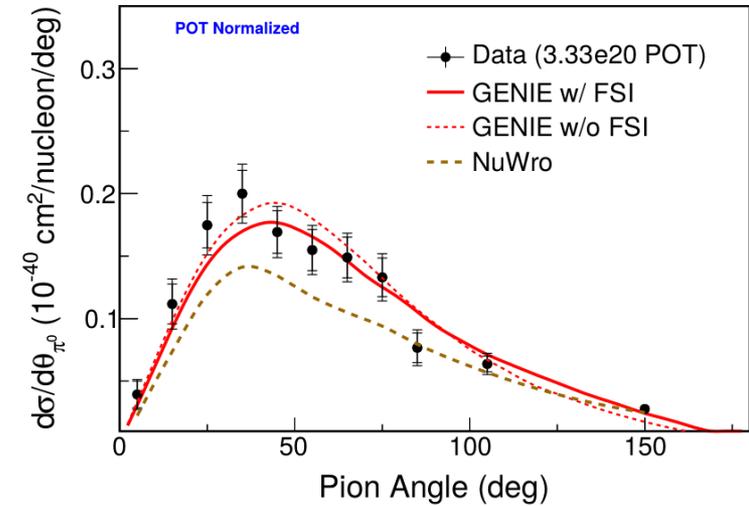
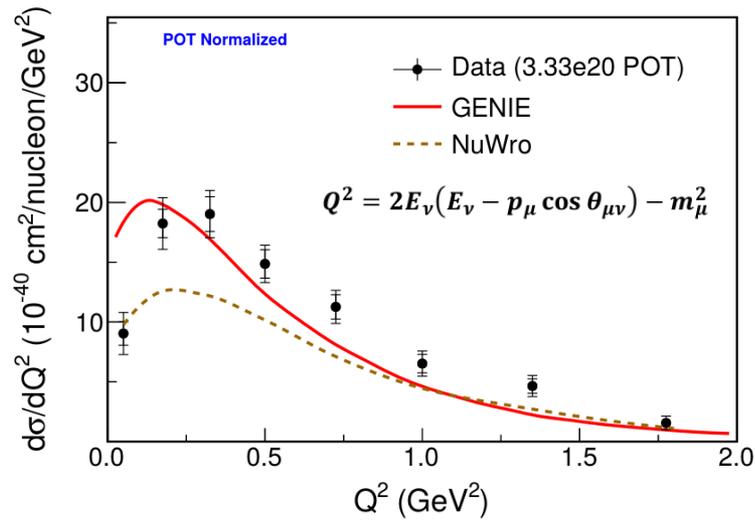


# $\nu_\mu$ CC Single $\pi^0$ Production

## Kinematic Variables



- These new cross section measurements provide a detailed view of the signal channel.



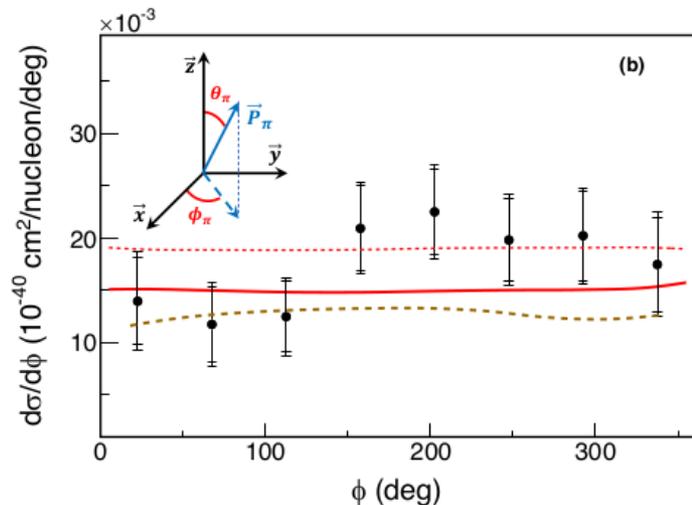
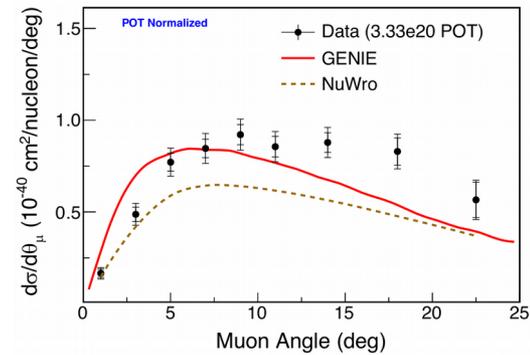
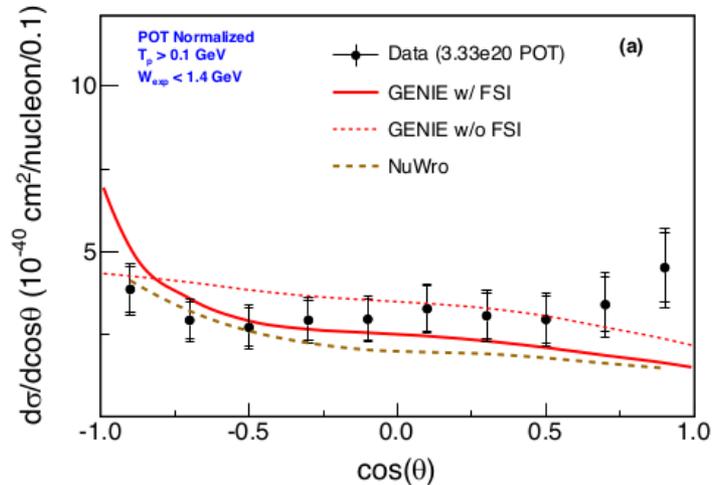


# $\nu_\mu$ CC Single $\pi^0$ Production Hadronic System

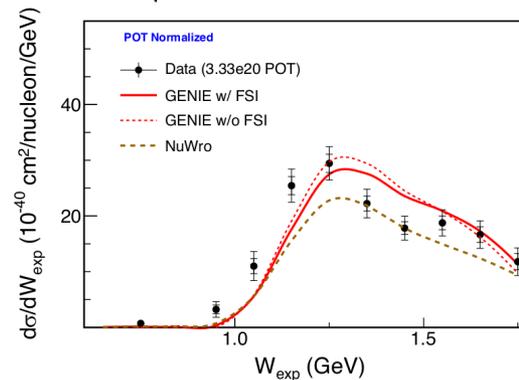


- $\Delta^+$  (1232) decay angles are measured for the first time!

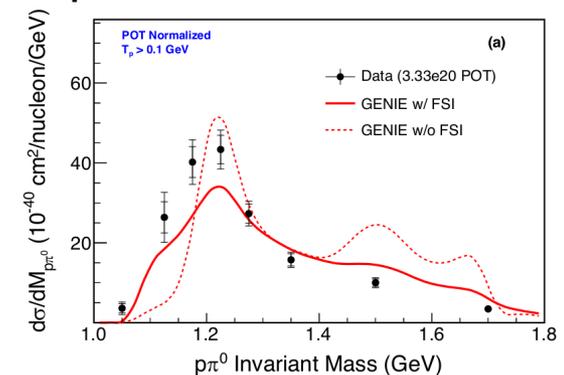
- These disagreements identify areas in need of improvement.



$$W_{exp} = \sqrt{m_n^2 + 2m_n(E_\nu - E_\mu) - Q^2}$$



Invariant Mass calculated with proton and  $\pi^0$  4-momentums



- GENIE and NuWro assume isotropic  $\Delta^+$  (1232) decay

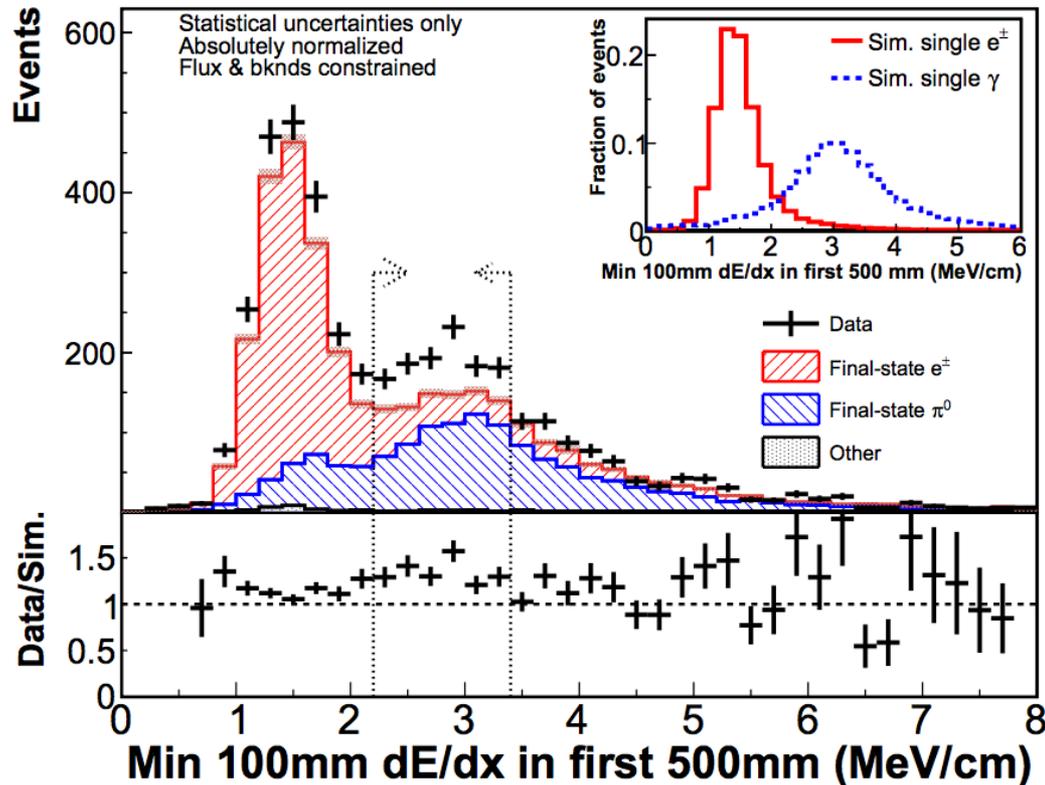


# Diffractive Neutral Pion Production

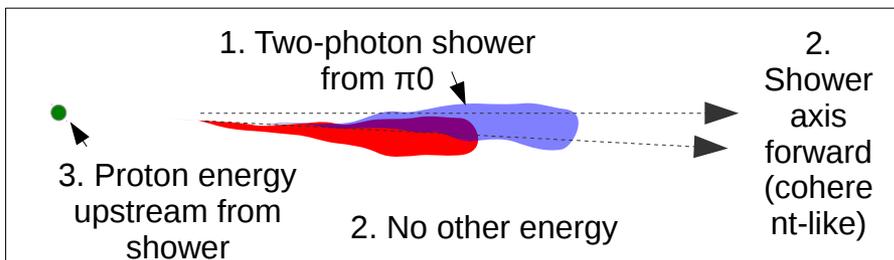
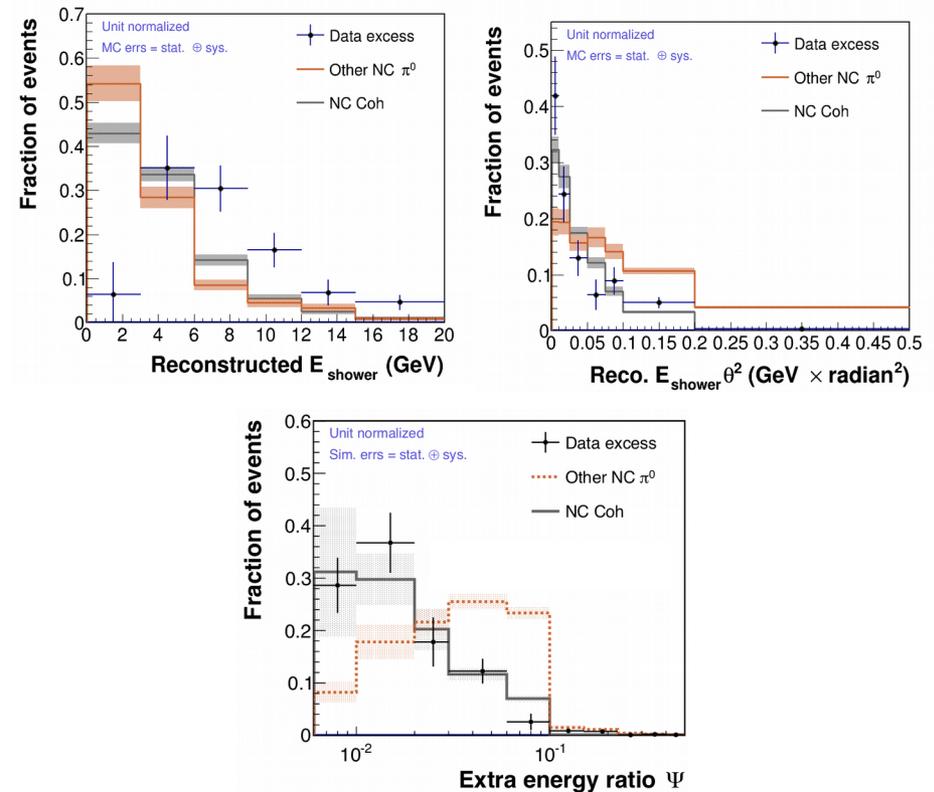
Phys. Rev. Lett. 117, 111801 (2016)



Observed as excess EM shower events in photon region of front dE/dx



Observed energy behavior is very different from any other NC  $\pi^0$  production models



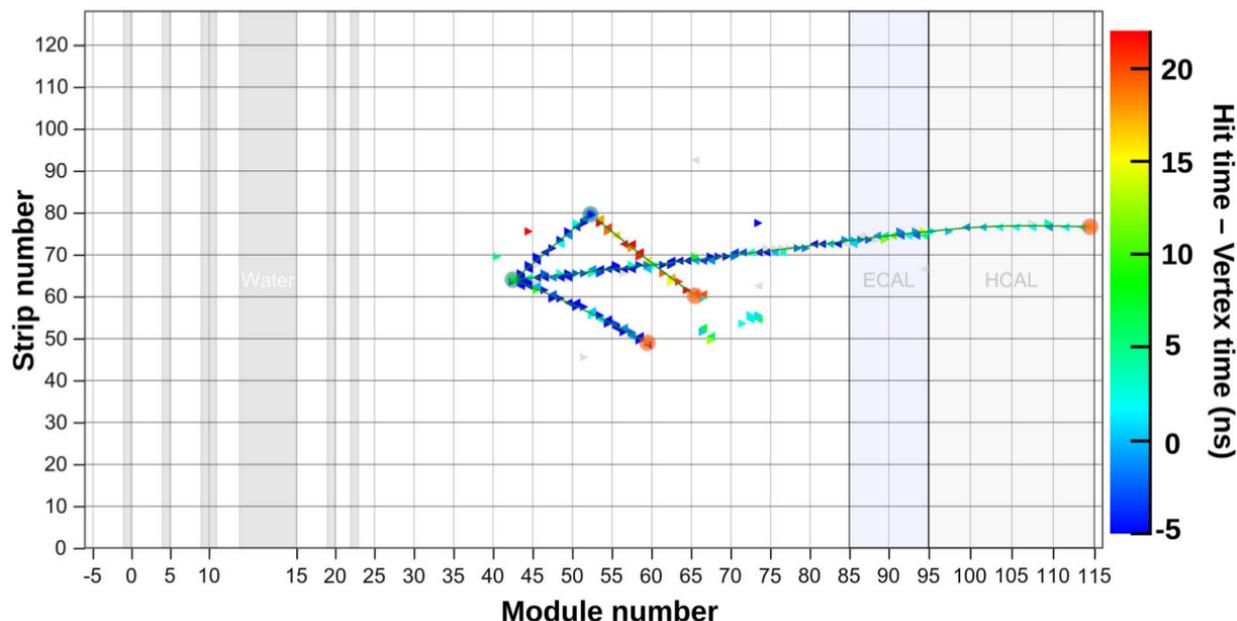
First direct experimental observation and characterization of this process!

Kaons . . .

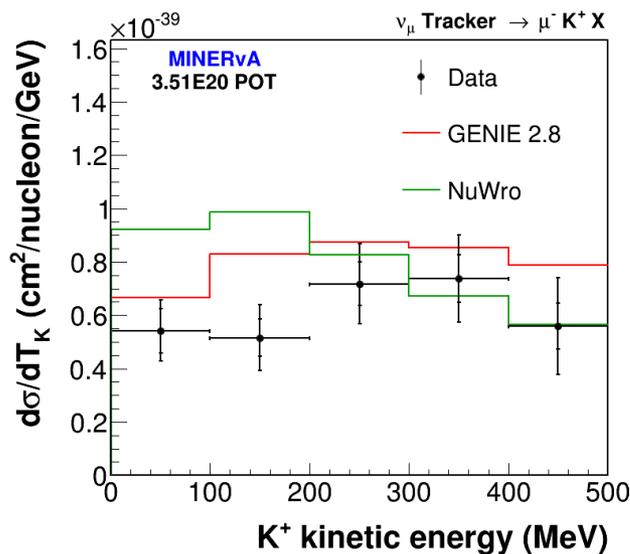
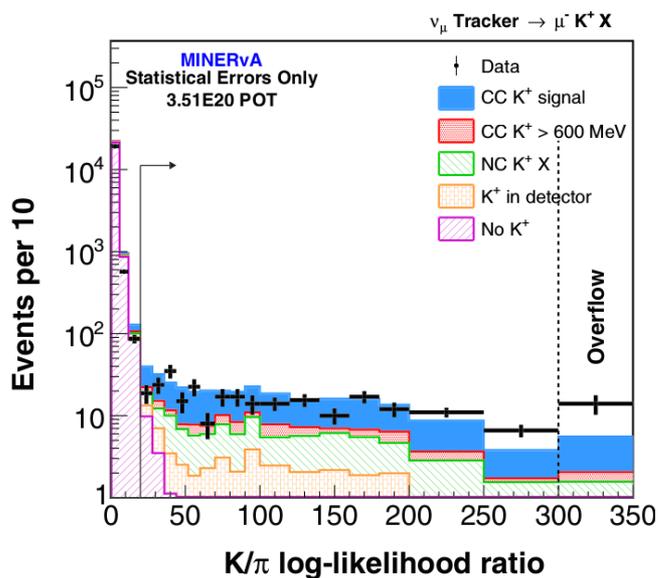


# Charge Current $K^+$ Production

Phys. Rev. D 94 012002 (2016)



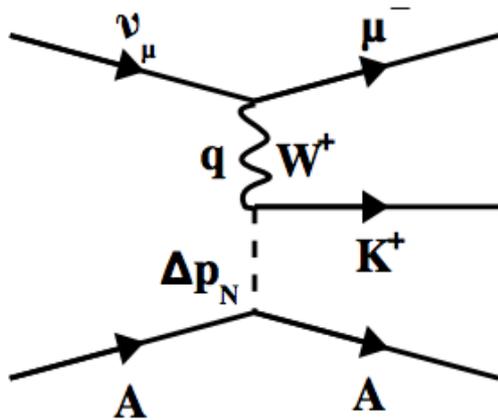
- Timing information used to isolate 885 CC candidate events.
- First high statistics measurement of the  $K^+$  energy spectrum for kaon production in  $\nu_\mu$  CC interactions.
- Provides an additional constraint on  $K^+$  FSI.
- The signal spectrum in  $p \rightarrow K^+ \nu$  due to kaon rescattering are well modeled in GENIE.
- NuWro disagreement tells the importance of an improved low- $W$  DIS model for  $K^+$  production.



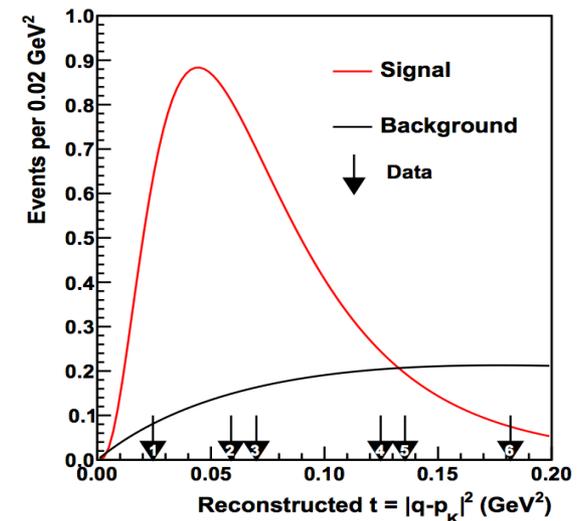
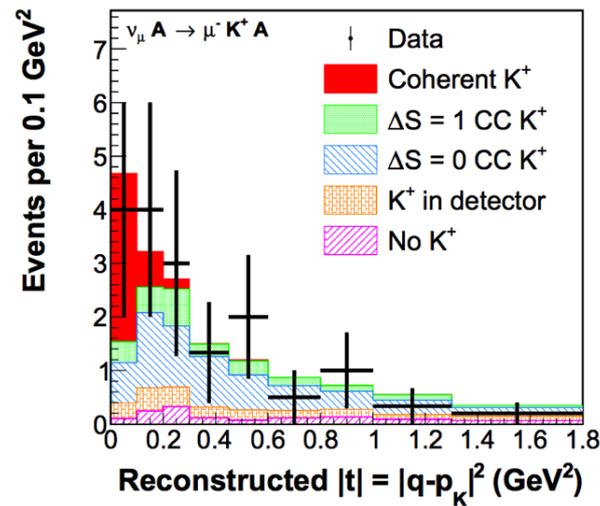
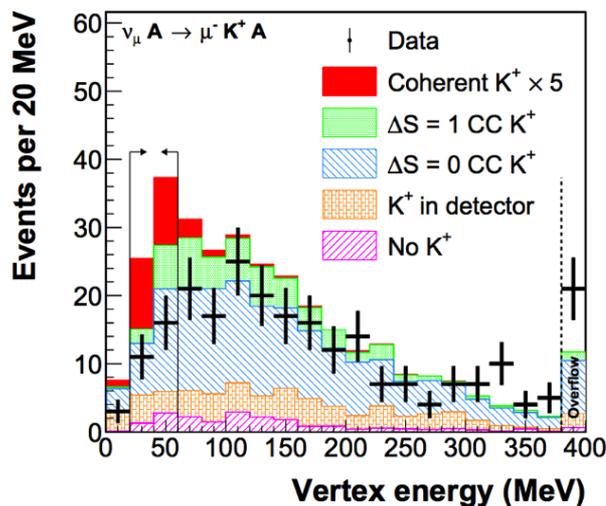


# Coherent $K^+$ Production

Phys. Rev. Lett. 117, 061802 (2016)



- Very rare inelastic electroweak process, brings  $K^+$  on shell and leaves the target nucleus intact in its ground state.
- Kinematics of the FS used to reconstruct the small momentum transfer to the nucleus; model independent characteristic of coherent scattering.
- Identified via cuts on vertex energy and  $t$ , scans to remove  $\pi^0$  contamination.
- 6 events found in signal region; fit estimates  $3.77^{+2.64}_{-1.93}$  signal events at  $3\sigma$ .





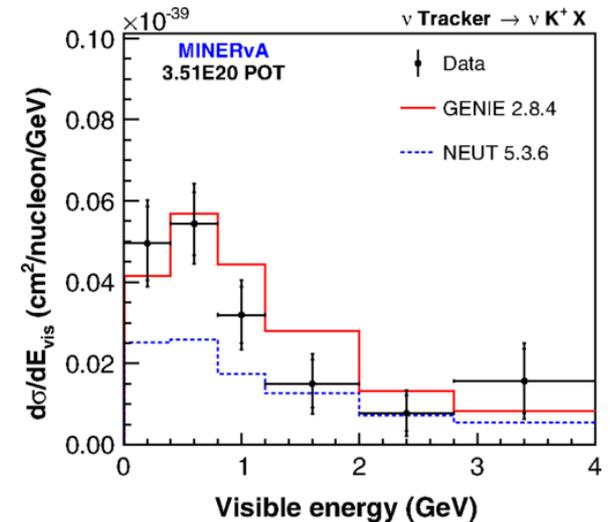
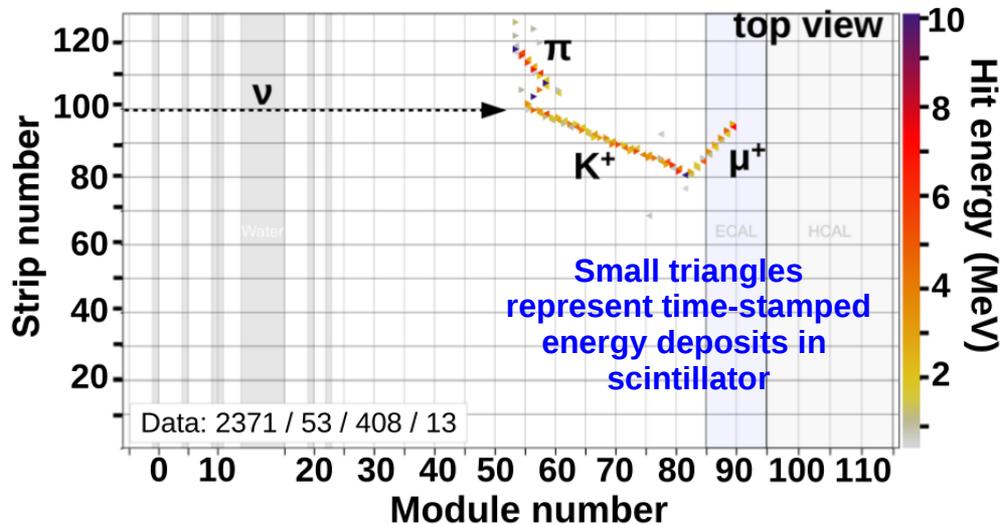
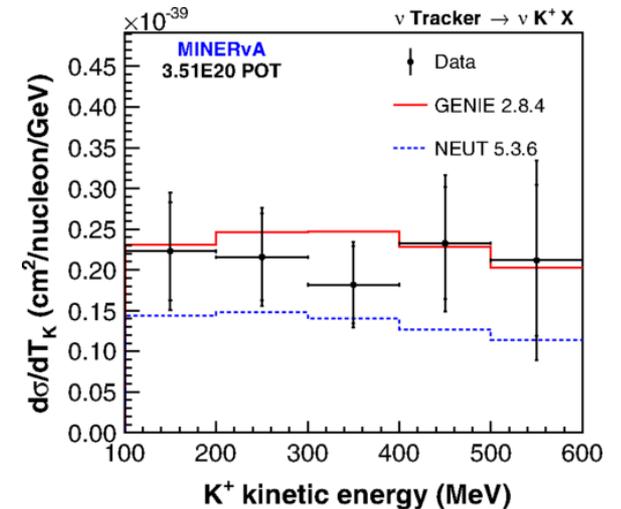
# Neutral Current $K^+$ Production

Phys. Rev. Lett. 199, 0011802 (2017)



- $K^+$  production by atmospheric neutrinos (especially neutral current interactions) are backgrounds for SUSY-preferred proton decay  $p \rightarrow K^+ \nu$
- Particularly problematic in Cherenkov detectors, where NC  $K^+$  event with no particles above Cherenkov threshold will fake the signal process
- Mismodeled rates for  $K^+$  nothing would also be a problem in liquid Argon detectors

Kinematic distributions appear well modeled in GENIE, level in NEUT too low





# . . . and More Results

## From Low Energy Beam Configuration



- > "Direct Measurement of Nuclear Dependence of Charged Current Quasielastic-like Neutrino Interactions using MINERvA" accepted by Phys. Rev. L
- > "Measurement of neutral-current  $K^+$  production by neutrinos using MINERvA", Phys. Rev. Lett. 199, 0011802 (2017)
- > "Measurement of the antineutrino to neutrino charged-current interaction cross section ratio on carbon" Phys. Rev. D 95, 072009 (2017)
- > "Measurements of the Inclusive Neutrino and Antineutrino Charged Current Cross Sections in MINERvA Using the Low- $\nu$  Flux Method", Phys. Rev. D 94, 112007 (2016)
- > "Neutrino Flux Predictions for the NuMI Beam", Phys. Rev. D 94, 092005 (2016)
- > "First evidence of coherent  $K^+$  meson production in neutrino-nucleus scattering", Phys. Rev. Lett. 117, 061802 (2016)
- > "Measurement of  $K^+$  production in charged-current  $\nu\mu$  interactions", Phys. Rev. D 94 012002 (2016)
- > "Cross sections for neutrino and antineutrino induced pion production on hydrocarbon in the few GeV region using MINERvA", Phys. Rev. D 94, 052005 (2016).
- > "Evidence for diffractive neutral pion production from hydrogen in Neutrino Interactions on hydrocarbon", Phys. Rev. Lett. 117, 111801 (2016)
- > "Measurement of Neutrino Flux using Neutrino-Electron Elastic Scattering", Phys. Rev. D 93, 112007 (2016)
- > "Measurement of Partonic Nuclear Effects in Deep-Inelastic Neutrino Scattering using MINERvA", Phys. Rev. D 93, 071101 (2016).
- > "Identification of nuclear effects in neutrino-carbon interactions at low three-momentum transfer", Phys. Rev. Lett. 116, 071802 (2016).
- > "Measurement of electron neutrino quasielastic and quasielastic-like scattering on hydrocarbon at average  $E_\nu$  of 3.6 GeV", Phys.Rev. Lett. 116, 081802 (2016).
- > "Single neutral pion production by charged-current anti- $\nu\mu$  interactions on hydrocarbon at average  $E_\nu$  of 3.6 GeV", Phys.Lett. B749 130-136 (2015).
- > "Measurement of muon plus proton final states in  $\nu\mu$  Interactions on Hydrocarbon at average  $E_\nu$  of 4.2 GeV" Phys. Rev. D91, 071301 (2015).
- > "Measurement of Coherent Production of  $\pi^\pm$  in Neutrino and Anti-Neutrino Beams on Carbon from  $\nu\mu$  of 1.5 to 20 GeV", Phys. Rev.Lett. 113, 261802 (2014).
- > "Charged Pion Production in  $\nu_\mu$  Interactions on Hydrocarbon at average  $E_\nu$  of 4.0 GeV" , Phys.Rev. D92, 092008 (2015).
- > "Measurement of ratios of  $\nu_\mu$  charged-current cross sections on C, Fe, and Pb to CH at neutrino energies 2-20 GeV", Phys. Rev. Lett. 112, 231801 (2014).
- > "Measurement of Muon Neutrino Quasi-Elastic Scattering on a Hydrocarbon Target at  $E_\nu \sim 3.5$  GeV", Phys. Rev. Lett. 111, 022502 (2013).
- > "Measurement of Muon Antineutrino Quasi-Elastic Scattering on a Hydrocarbon Target at  $E_\nu \sim 3.5$  GeV", Phys. Rev. Lett. 111, 022501 (2013).



# ... and More Results

## From Low Energy Beam Configuration



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- > "Measurement of neutral-current  $K^+$  production by neutrinos using MINERvA", Phys. Rev. Lett. 199, 0011802 (2017)
- > "Measurement of the antineutrino to neutrino charged-current interaction cross section ratio on carbon" Phys. Rev. D 95, 072009 (2017)
- > "Measurements of the Inclusive Neutrino and Antineutrino Charged Current Cross Sections in MINERvA Using the Low-Energy Beam Configuration", Phys. Rev. D 94, 112007 (2016)
- > "Neutrino-Induced  $K^+$  Production in the MINERvA Low-Energy Beam", Phys. Rev. D 94, 092005 (2016)
- > "First Observation of  $K^+$  Production in Neutrino-Nucleus Scattering", Phys. Rev. Lett. 117, 061802 (2016)
- > "Measurement of Neutral-Current  $\nu_\mu$  Interactions", Phys. Rev. D 94, 012002 (2016)
- > "Cross Section for Neutrino-Induced Pion Production on Hydrocarbon in the Few GeV Region using MINERvA", Phys. Rev. Lett. 116, 081802 (2016)
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- > "Identification of nuclear effects in neutrino-carbon interactions", Phys. Rev. Lett. 116, 071802 (2016)
- > "Measurement of electron neutrino quasielastic and quasielastic-like interactions at average energy of 3.6 GeV", Phys. Rev. Lett. 116, 081802 (2016)
- > "Single neutral pion production by charged-current anti- $\nu_\mu$  interactions at average energy of 3.6 GeV", Phys. Lett. B 749, 130-136 (2015)
- > "Measurement of muon plus proton final states in  $\nu_\mu$  interactions on carbon at average energy of 3.2 GeV", Phys. Rev. D 91, 071301 (2015)
- > "Measurement of Coherent Production of  $\pi^\pm$  in Neutrino and Anti-Neutrino Beams on Carbon from  $\nu_\mu$  of 1.5 to 20 GeV", Phys. Rev. Lett. 113, 261802 (2014)
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- > "Measurement of Muon Neutrino Quasi-Elastic Scattering on a Hydrocarbon Target at Energy  $\sim 3.5$  GeV", Phys. Rev. Lett. 111, 022502 (2013)
- > "Measurement of Muon Antineutrino Quasi-Elastic Scattering on a Hydrocarbon Target at Energy  $\sim 3.5$  GeV", Phys. Rev. Lett. 111, 022501 (2013)

**Sandro's Talk**  
**Tuesday 2:00 pm**

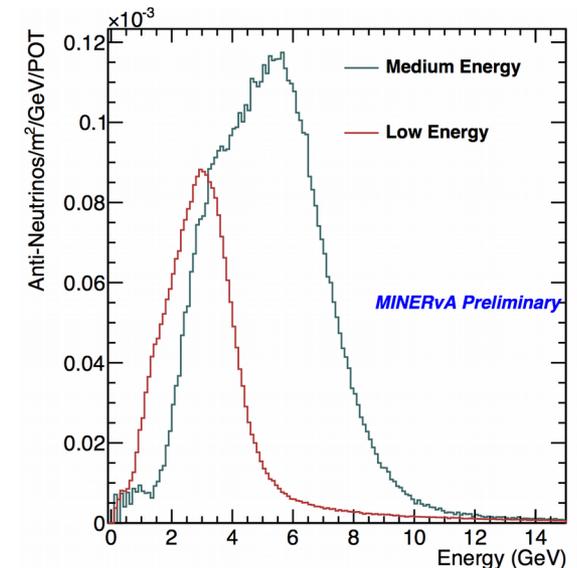
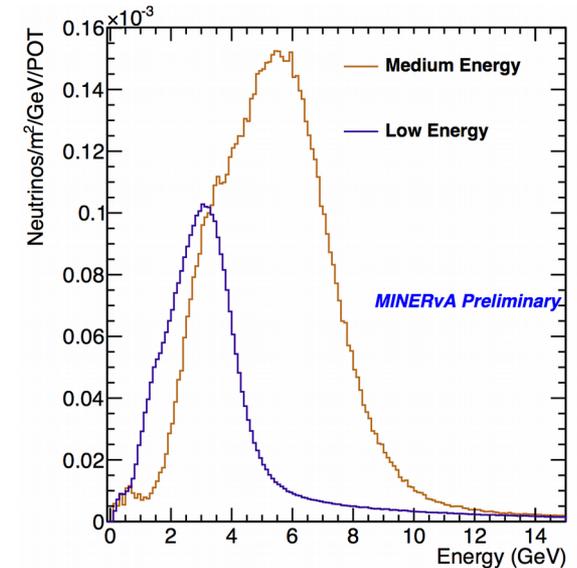
**Cheryl's Talk**  
**Friday 2:00 pm**



# MINERvA Status and Future Plans



- MINERvA is now accumulating many more events in the Medium Energy beam configuration yielding high statistics
- We have over  $10E 20$  POT in the medium energy beam.
- Measurements of quasi-elastic, pion production, DIS and inclusive on iron, lead and carbon using the medium energy.
- Expect reduction in systematics, with a  $\sim$ factor of 10 more statistics for the neutrino-electron scattering flux Constrain
- The higher energy beam tune gives us a much higher reach in four-momentum transfer squared ( $Q^2$ ).
- Results in ME will increase the sensitivity to probe the nuclear effects.





# Conclusions



- **Neutrino cross section measurements are important for neutrino oscillation measurements and to understand the nature of neutrino-nucleus scattering.**
- **MINERvA has precisely studied neutrino interactions in the 1-20 GeV region, improving our knowledge (and models) of:**
  - **Flux Studies**
  - **$\nu$ -CC Interactions**
  - **Neutrino cross sections at low energy, low  $Q^2$  .**
  - **A-Dependence in neutrino interactions (Targets He, C, Fe, Pb and H<sub>2</sub>O)**
- **MINERvA is providing constraints from many channels: inclusive scattering, quasi-elastic scattering, pion production, kaon production, deep inelastic interactions**
- **Providing the first direct data constraint of backgrounds from atmospheric neutrinos to  $p \rightarrow K\nu$  proton decay**
- **These results will help resolve long standing discrepancies between experiments and will be important for minimizing systematic errors in oscillation experiments.**



# From the MINERvA Collaboration Thank You . . .



Back Up



# From the MINERνA Collaboration

## Thank You . . .



To obtain the incident beam flux, we employ the “low- $\nu$ ” method described previously.

The differential dependence of the cross section in terms of  $\nu$  is expanded in  $\nu/E$  as

$$\frac{d\sigma^{\nu,\bar{\nu}}}{d\nu} = A \left( 1 + \frac{B^{\nu,\bar{\nu}}}{A} \frac{\nu}{E} - \frac{C^{\nu,\bar{\nu}}}{A} \frac{\nu^2}{2E^2} \right)$$

Where  $E$  is the incident neutrino energy. The coefficients  $A$ ,  $B^{\nu,\bar{\nu}}$ , and  $C^{\nu,\bar{\nu}}$  depend on integrals over structure functions (or form factors, in the low energy limit)

$$A = \frac{G_F^2 M}{\pi} \int F_2(x) dx,$$

$$B^{\nu,\bar{\nu}} = -\frac{G_F^2 M}{\pi} \int (F_2(x) \mp x F_3(x)) dx,$$

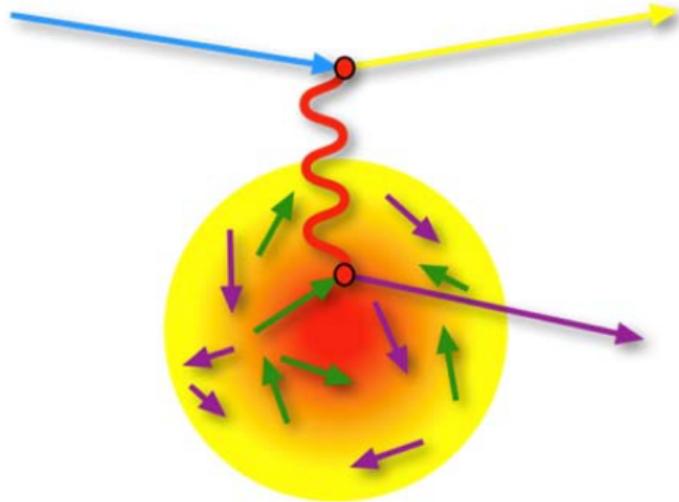
$$C^{\nu,\bar{\nu}} = B^{\nu,\bar{\nu}} - \frac{G_F^2 M}{\pi} \int F_2(x) \left( \frac{1 + \frac{2Mx}{\nu}}{1 + R_L} - \frac{Mx}{\nu} - 1 \right) dx.$$



# Nuclear Effects

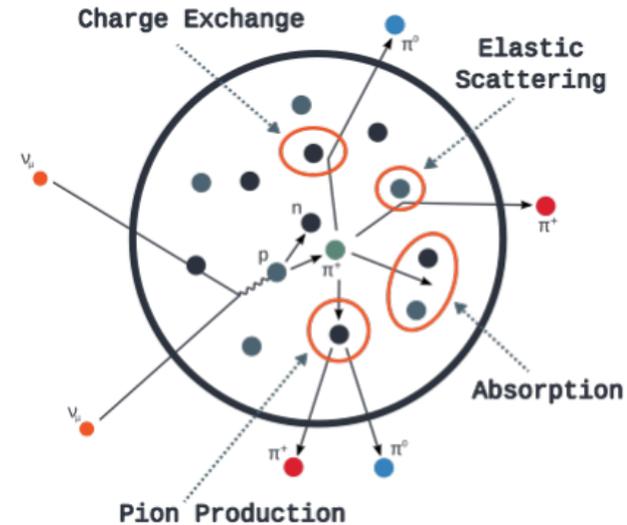


## Initial State Nuclear Effect



- Short, medium, and long range nucleon-nucleon correlations on the initial condition, e.g. “2p2h” effect , “RPA” effect

## Final State Nuclear Effect



- Particles created have to work their way out of the nucleus, e.g. **absorption**

Signal ↔ Background Migration

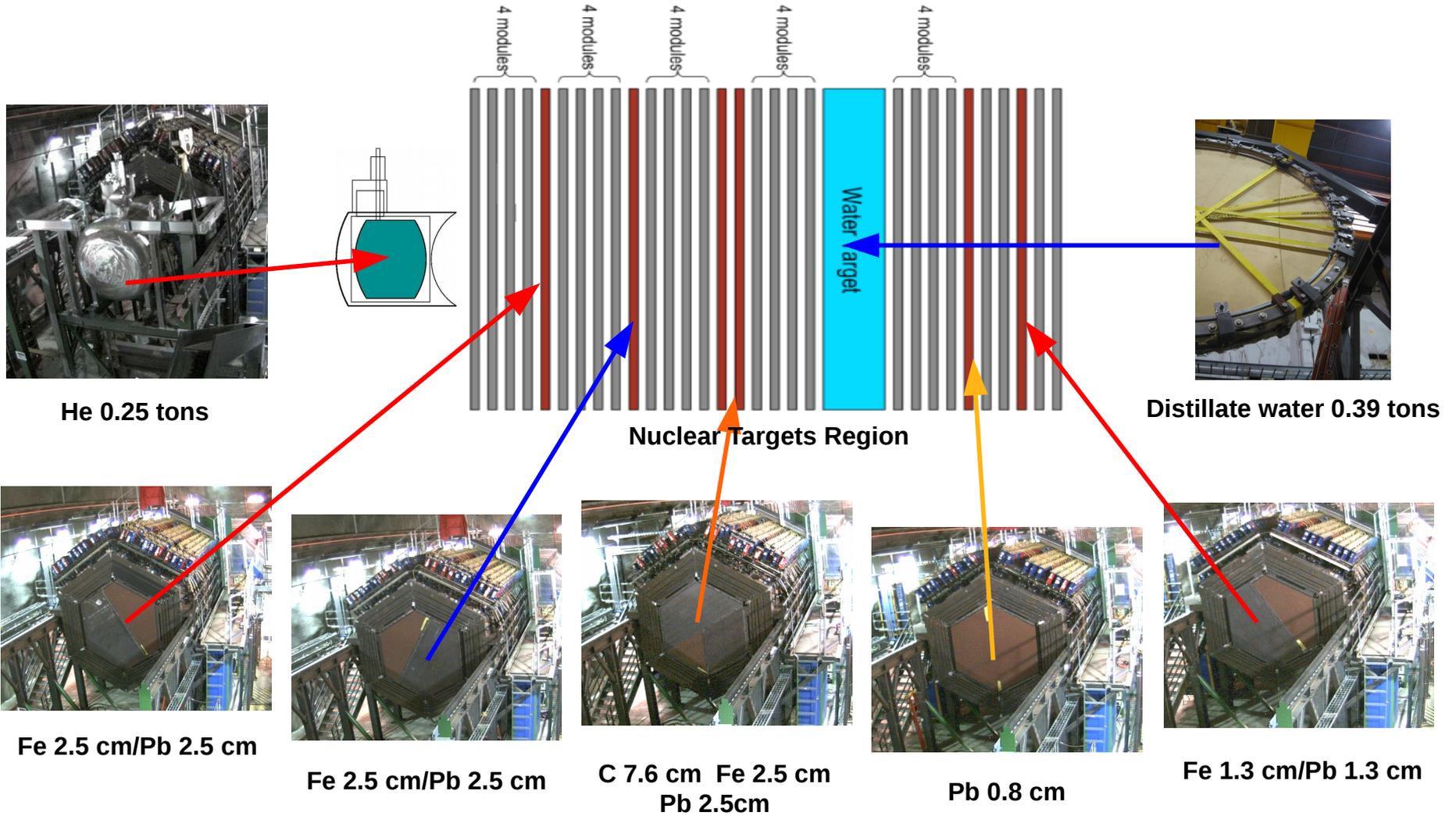
MINERvA provides detailed description of final state particles and information on big source of uncertainties in the neutrino interaction!



# MINERvA Experiment Detector



Beam Direction →

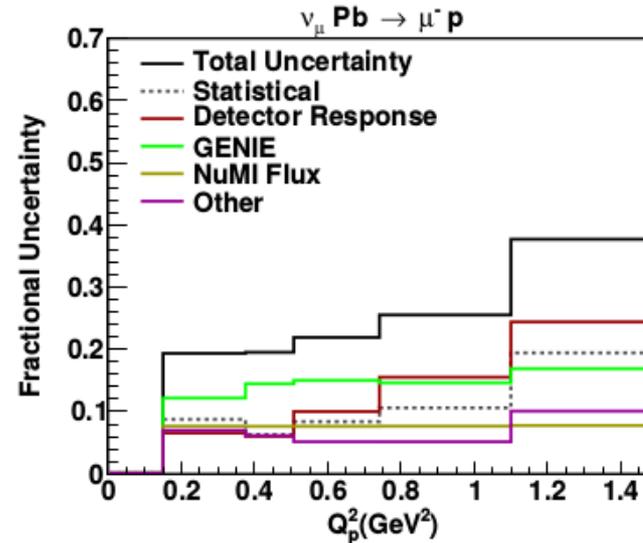
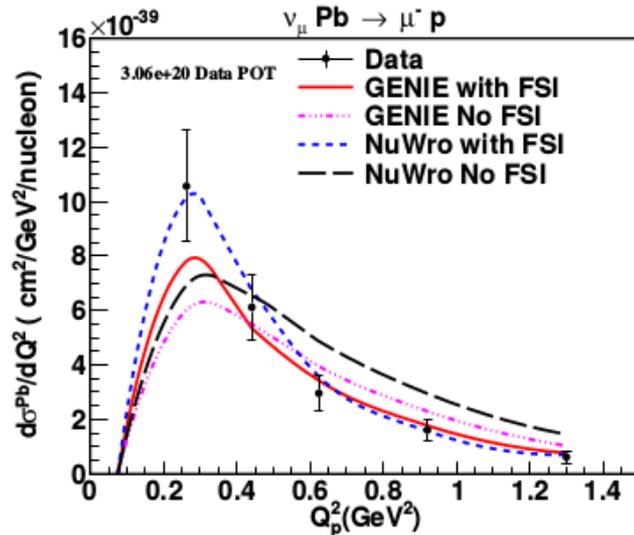
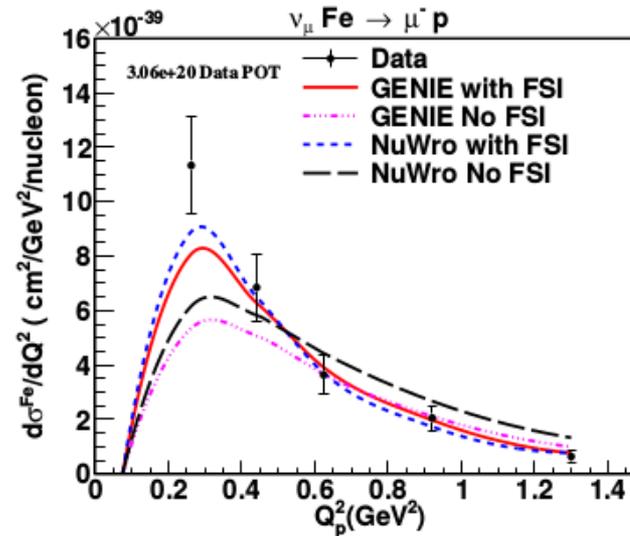
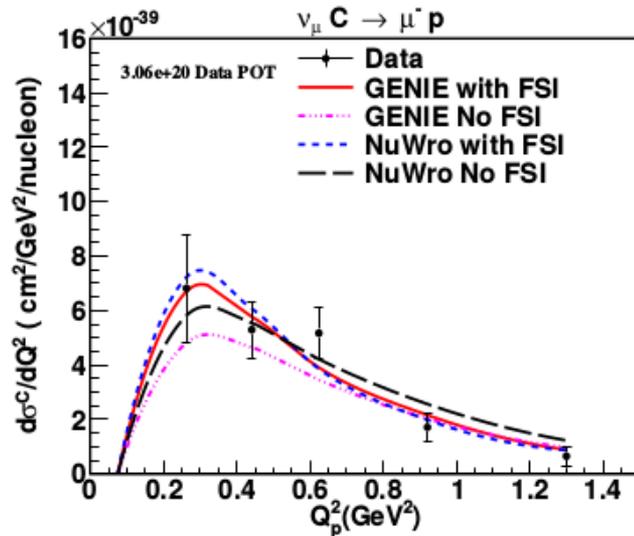




# Nuclear Dependence of CC Quasielastic-like Models Generators Comparison



The transferred four-momentum squared to the target nucleus,  $Q^2$ , is reconstructed based on the kinematics of the leading proton,



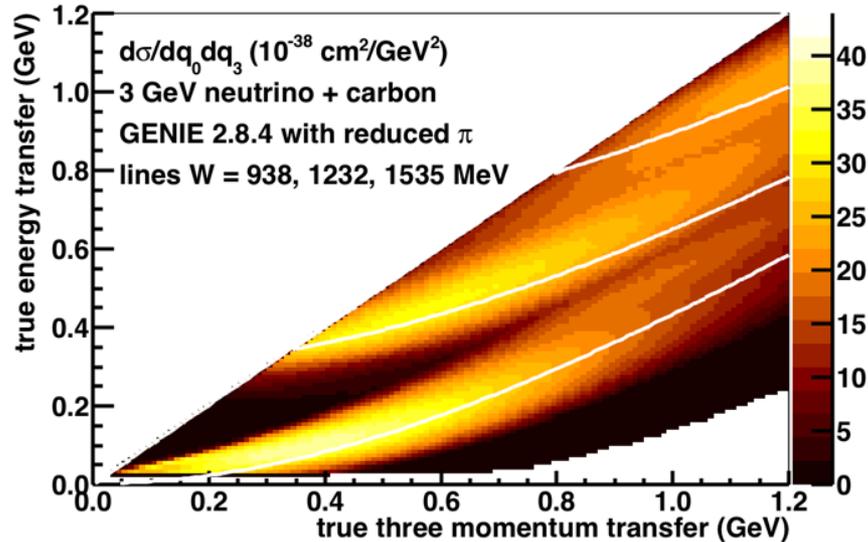
M. Betancourt FNAL  
JETP Seminar  
Oct 2016

Accepted by  
Phys. Rev. L.

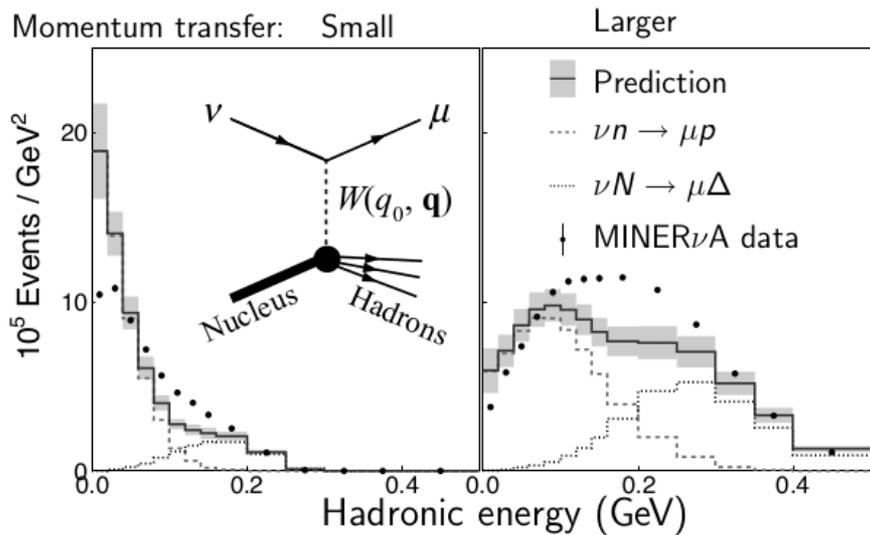


# Nuclear Effects at Low Three-Momentum Transfer

Phys. Rev. Lett. 116, 071802 (2016)



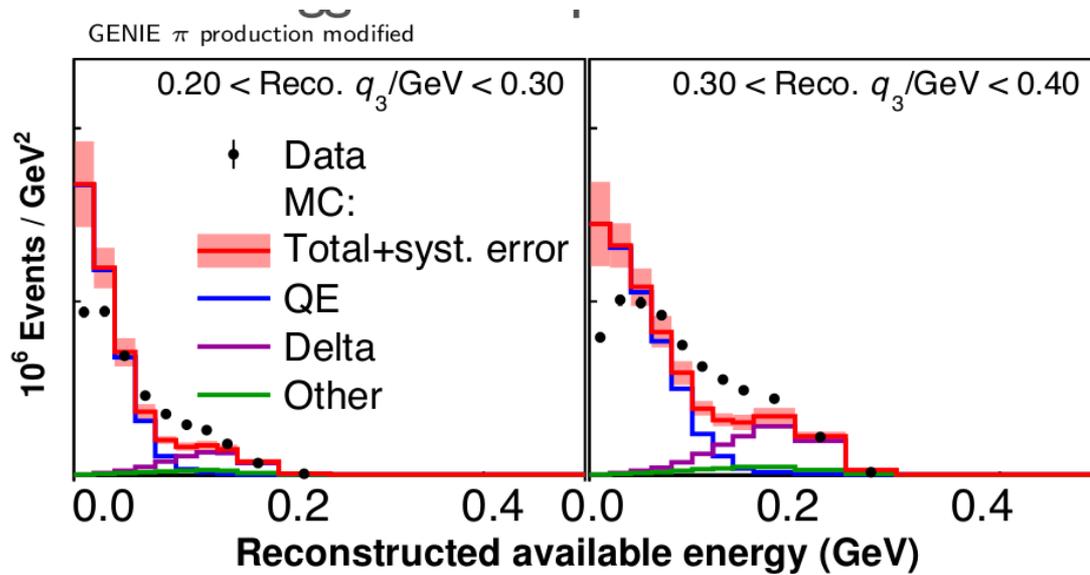
- Look at inclusive scattering in 2 kinematic dimensions.
- Separate the four-momentum transfer squared;  $Q^2$ , into energy transfer  $q_0$  and 3-momentum transfer  $q_3$
- Reconstructing energy and momentum transfer allows us to isolate channels in a fashion (somewhat) analogous to electron scattering.
- We observe a small cross section at very low energy transfer that matches the expected screening effect of long-range nucleon correlations.



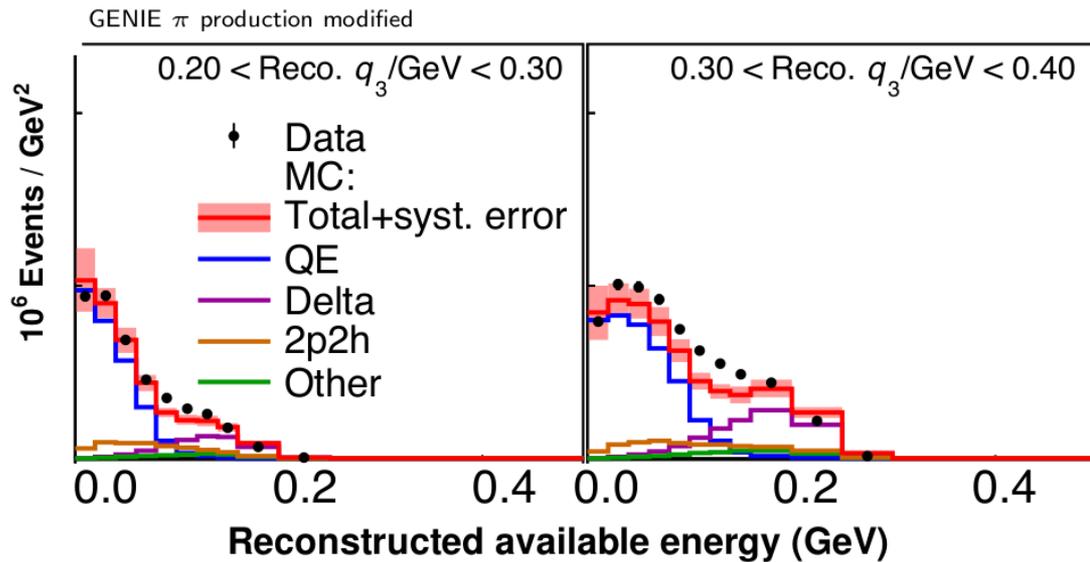


# Nuclear Effects at Low Three-Momentum Transfer

Phys. Rev. Lett. 116, 071802 (2016)



➤ Default nuclear model struggles to explain data



➤ Including more sophisticated nuclear models (2p2h effects and RPA)

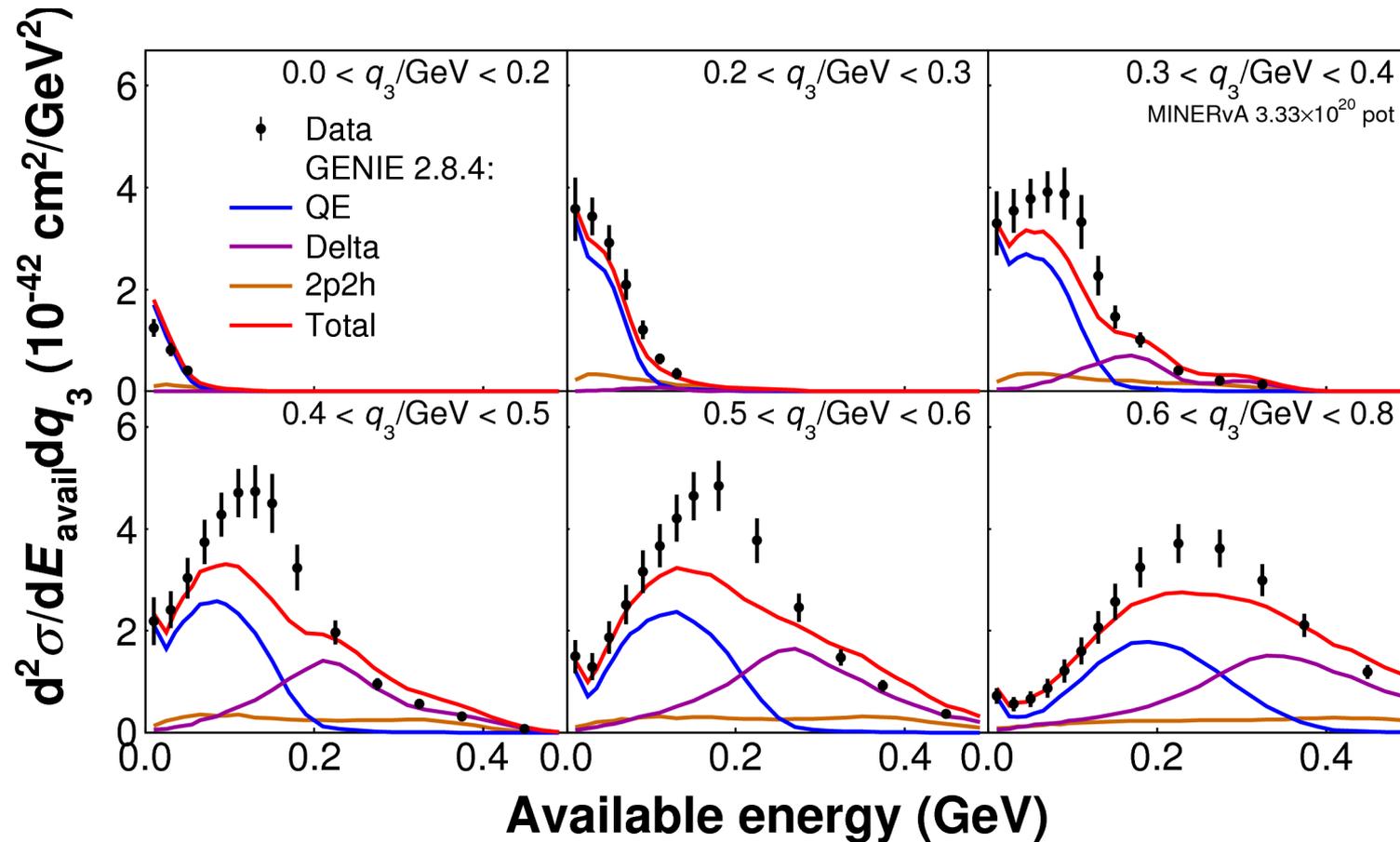


# Nuclear Effects at Low Three-Momentum Transfer

Phys. Rev. Lett. 116, 071802 (2016)



$$E_{\text{avail}} = \sum (\text{Proton and } \pi^{\pm} \text{ KE}) + (\text{Total } E \text{ of other particles except neutrons})$$

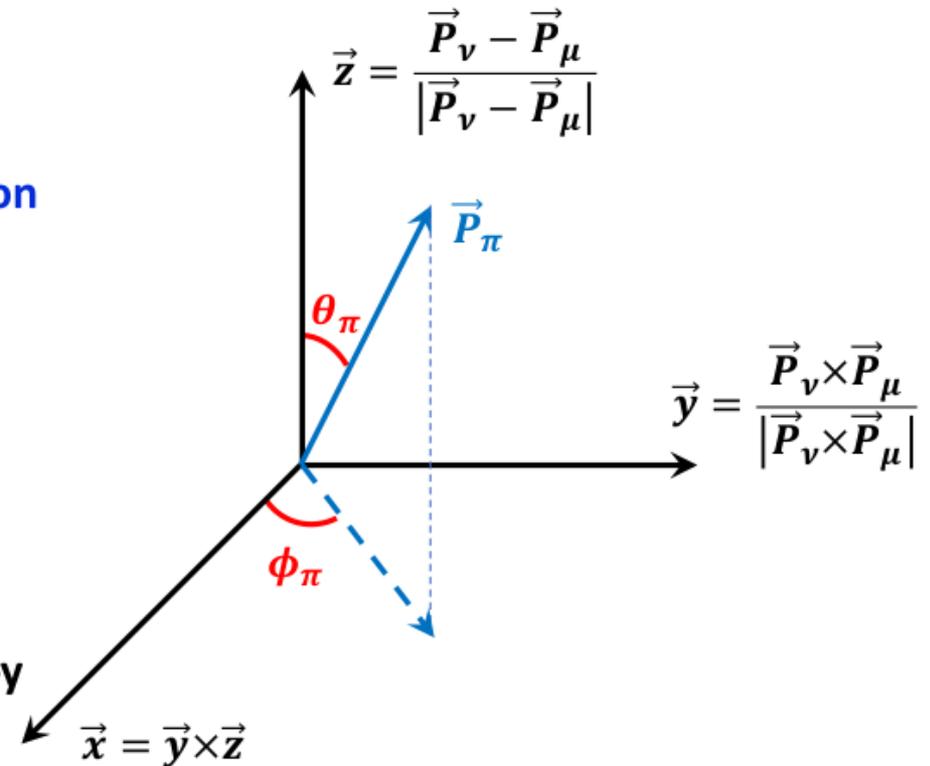


- Adding in models of RPA (a charge screening effect) and 2p2h improves agreement in some regions, but not in others.



## $\Delta^+(1232)$ Polarization – Coordinate Axes

1. Boost all particles to  $\Delta$  rest frame
2. Form z-axis along the momentum transfer direction
3. Form y-axis along the production plane normal
4. Form x-axis assuming the system is Right-Handed
5. Angle  $\theta$  is between z-axis and  $\vec{P}_\pi$
6. Angle  $\phi$  is between x-axis and  $\vec{P}_\pi$  projection on x-y plane



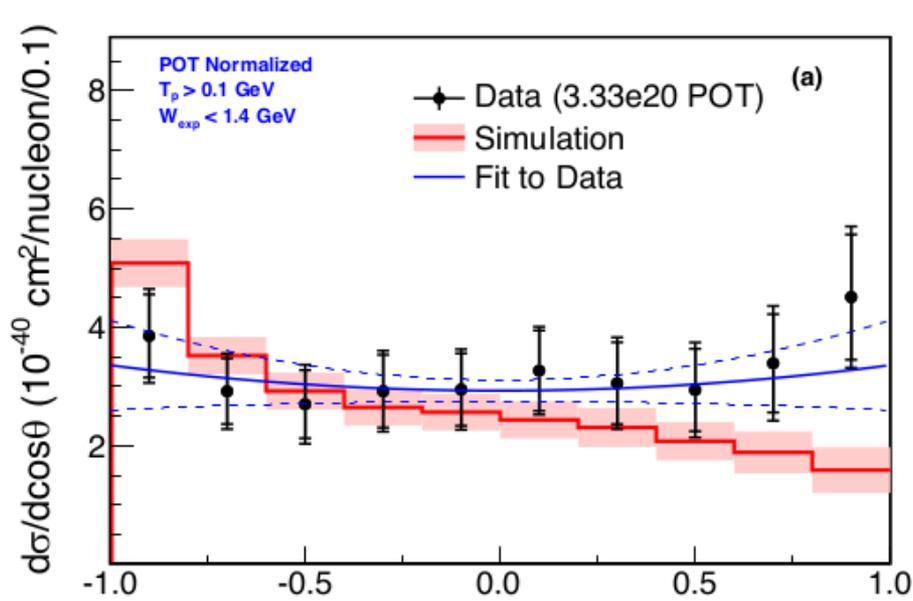


# $\nu_\mu$ CC Single $\pi^0$ Production

arXiv:1708.03723



## $\Delta^+(1232)$ Polarization – $\cos(\theta)$ and $\phi$

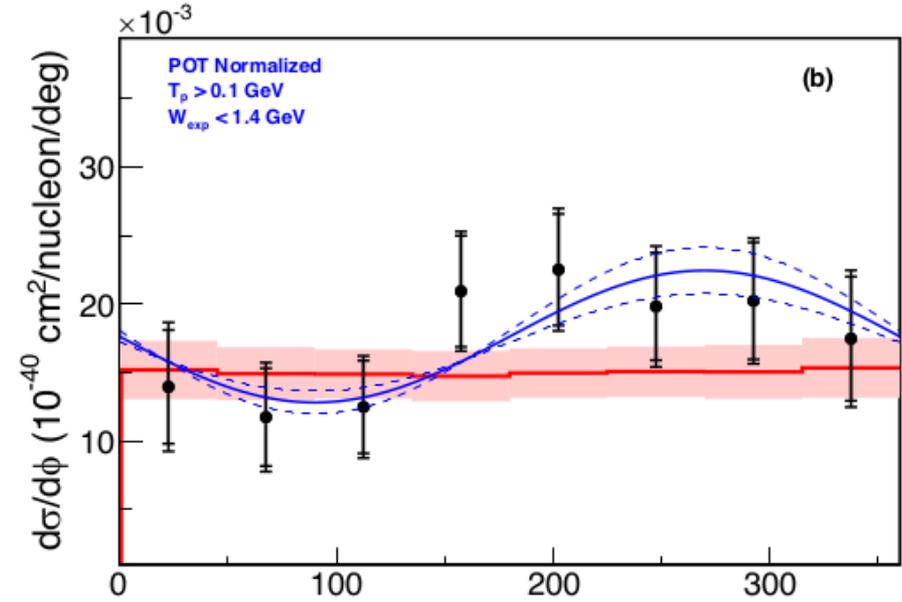


$$y = A + B(\cos \theta)^2$$

$$A = 2.93 \pm 0.18, B = 0.43 \pm 0.58$$

$$\frac{\chi_{MC}^2}{dof} = \frac{20.1}{9} = 2.3$$

$$\frac{\chi_{fit}^2}{dof} = \frac{2.9}{8} = 0.4$$



$$y = A + B \sin \phi$$

$$A = 17.54 \pm 0.43, B = -4.81 \pm 1.26$$

$$\frac{\chi_{MC}^2}{dof} = \frac{10.3}{7} = 1.5$$

$$\frac{\chi_{fit}^2}{dof} = \frac{3.3}{6} = 0.6$$