

# Global neutrino oscillation fits



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# Outline

## Introduction

**3-flavor fit**

**4-flavor fit**

## Conclusions

# Introduction

# Outstanding progress in $\nu$ physics in $\sim 20$ years

Discoveries	Interpretation	known knowns
<p><b>Zenith angle dependence (Multi-GeV)</b></p> <p><b>Fluxes</b></p> <p>+ many other ones: solar, KamLAND, <math>\theta_{13}</math> at reactors &amp; T2K ...</p>		$\delta m^2/eV^2 \sim 7.4 \times 10^{-5} \pm 2.3\%$ $\Delta m^2/eV^2 \sim 2.5 \times 10^{-3} \pm 1.6\%$ $\sin^2 \theta_{12} \sim 0.30 \pm 5.8\%$ $\sin^2 \theta_{13} \sim 0.022 \pm 4.0\%$ $\sin^2 \theta_{23} \sim 0.5 \pm 9.0\%$
		<b>known unknowns</b>
		$\delta(\text{CP})$ $\text{sign}(\Delta m^2)$ $\text{octant}(\theta_{23})$ absolute $\nu$ mass Dirac/Majorana
		<b>unknown unknowns</b>
		NSI, sterile states, PMNS non-unitarity, ...?

3-flavor scheme now established as the standard framework...

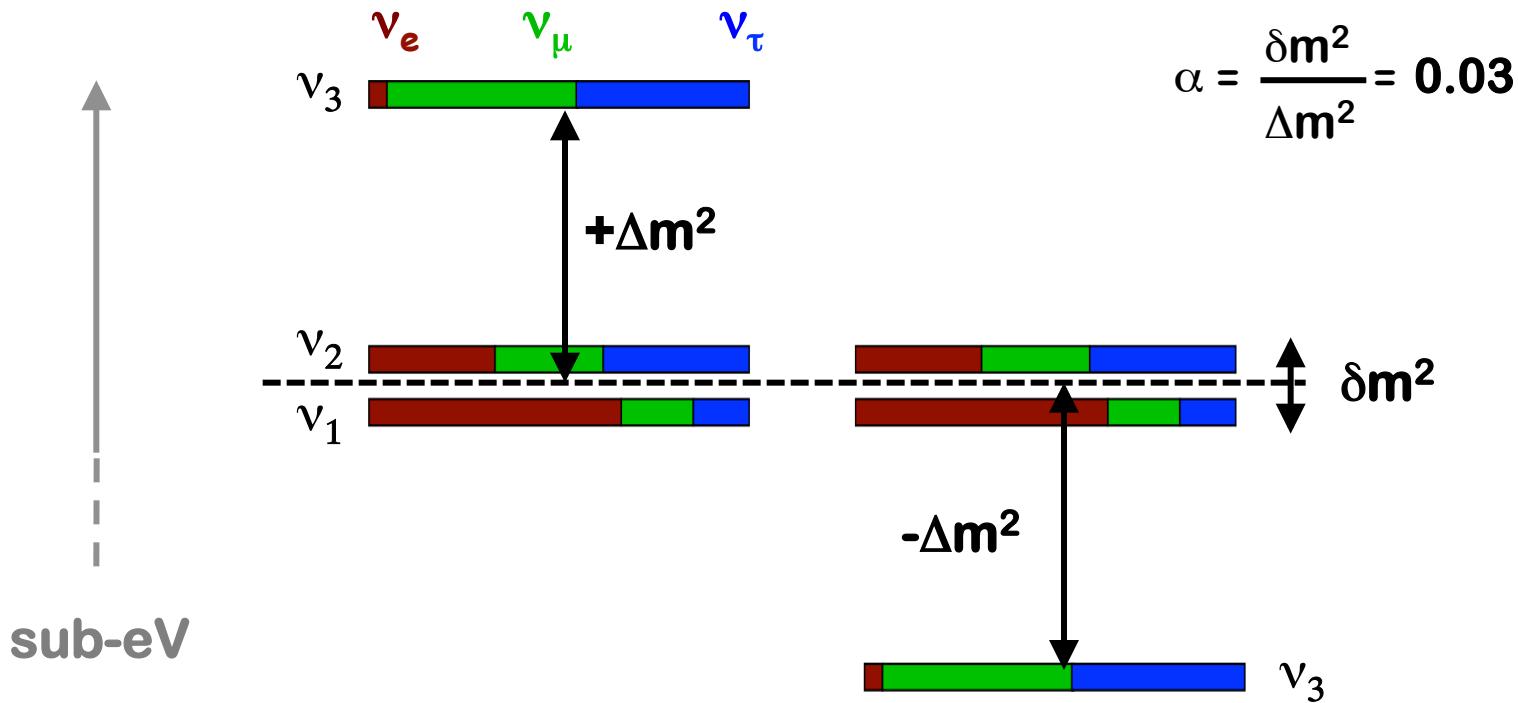
# The $3\nu$ mass spectrum

NO

or

IO ?

Unknown



# The 3ν mixing matrix

$$|\nu_\alpha\rangle = \sum_{i=1}^3 U_{\alpha i}^* |\nu_i\rangle \quad U = O_{23} \Gamma_\delta O_{13} \Gamma_\delta^\dagger O_{12}$$

$$\Gamma_\delta = \text{diag}(1, 1, e^{+i\delta})$$

$$\delta \in [0, 2\pi]$$

Dirac CP-violating phase  $\delta$

$U$  is non-real if  $\delta \neq (0, \pi)$

**Explicit  
form**

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\theta_{23} \sim 45^\circ \quad \theta_{13} \sim 9^\circ \quad \theta_{12} \sim 34^\circ$$

**Three non-zero  $\theta_{ij}$ : Way open to CPV searches...**

# CPV is a genuine 3-flavor effect

$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

$$A_{\alpha\beta}^{\text{CP}} \equiv P(\nu_\alpha \rightarrow \nu_\beta) - P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)$$

$$A_{\alpha\beta}^{\text{CP}} = -16 J_{\alpha\beta}^{12} \sin \Delta_{21} \sin \Delta_{13} \sin \Delta_{32}$$

$$J_{\alpha\beta}^{ij} \equiv \text{Im} [U_{\alpha i} U_{\beta j} U_{\alpha j}^* U_{\beta i}^*] \equiv J \sum_{\gamma=e,\mu,\tau} \epsilon_{\alpha\beta\gamma} \sum_{k=1,2,3} \epsilon_{ijk}$$

**J is parameterization independent (Jarlskog invariant)**

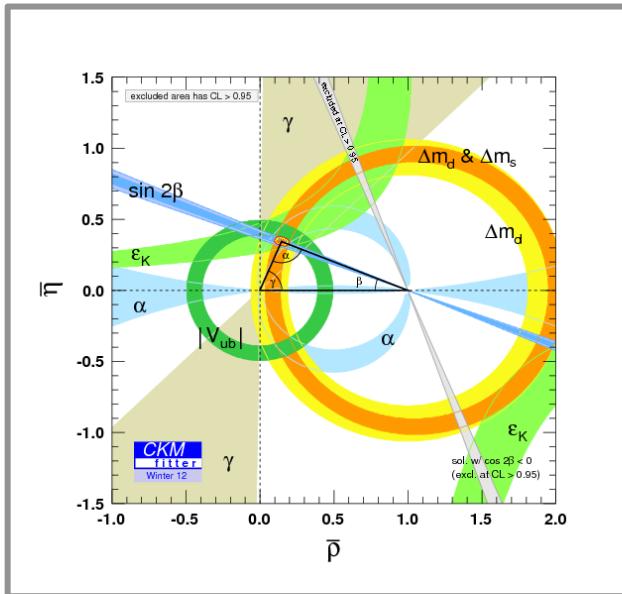
**In the standard parameterization:**

$$J = \frac{1}{8} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13} \cos \theta_{13} \sin \delta$$

**Conditions for CPV:**

- No degenerate ( $\nu_i, \nu_j$ ) ✓
- No  $\theta_{ij} = (0, \pi/2)$  ✓
- $\delta \neq (0, \pi)$  (hints)

# Quarks & Leptons vis-à-vis



In the neutrino sector the precision is much lower than that reached for quarks (albeit is quickly increasing!)

However, chances to discover a large CPV are much bigger...

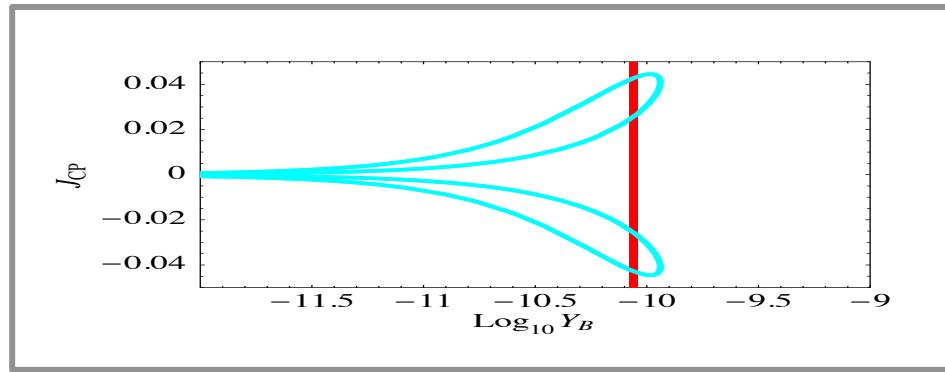
$$J = \frac{1}{8} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13} \cos \theta_{13} \sin \delta$$

-  $J_{CKM} \sim 3 \times 10^{-5}$

-  $J_{PMNS}$  may be as large as  $3 \times 10^{-2}$

# Implications of a large $J_{\text{PMNS}}$

While it would not prove the leptogenesis mechanism it may have an impact on it



Pascoli, Petcov, Riotto PRD 75 083511 (2007)

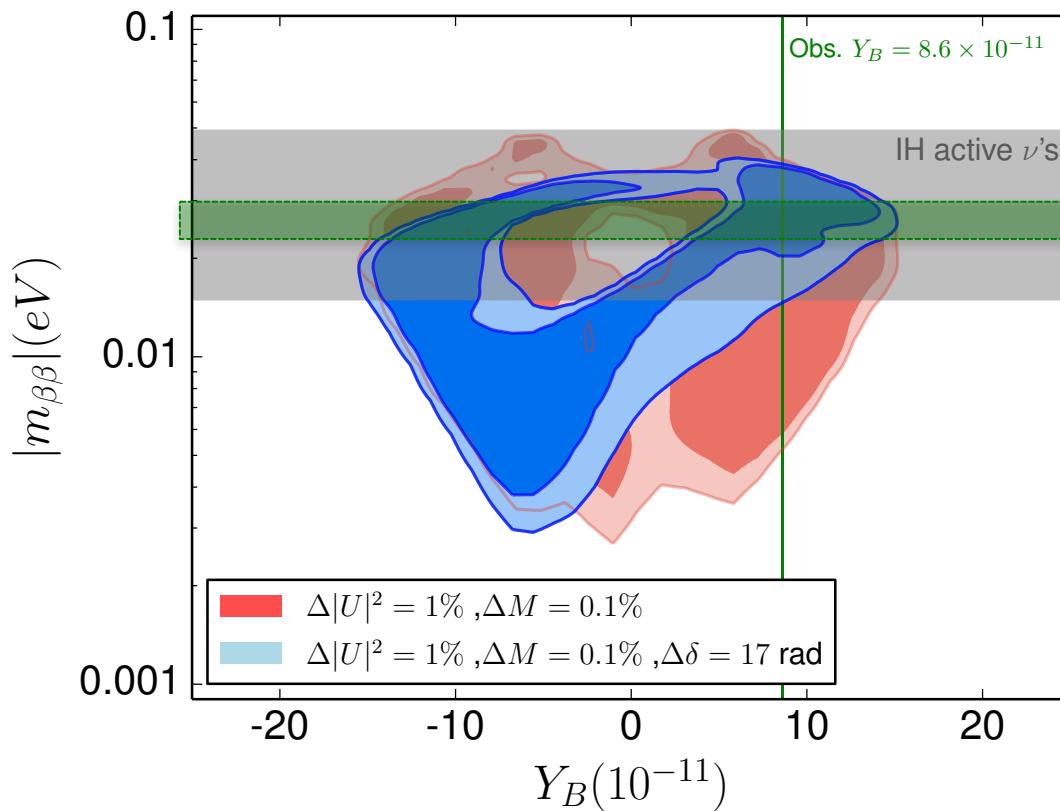
The sole  $\delta$  may suffice to produce the observed amount of baryon asymmetry provided

$$|\sin\theta_{13} \sin\delta| > 0.11$$

$\sim 0.15$

$\sim -1.0$  (see later)

# $Y_B$ in a minimal seesaw model ( $M \sim \text{GeV}$ )



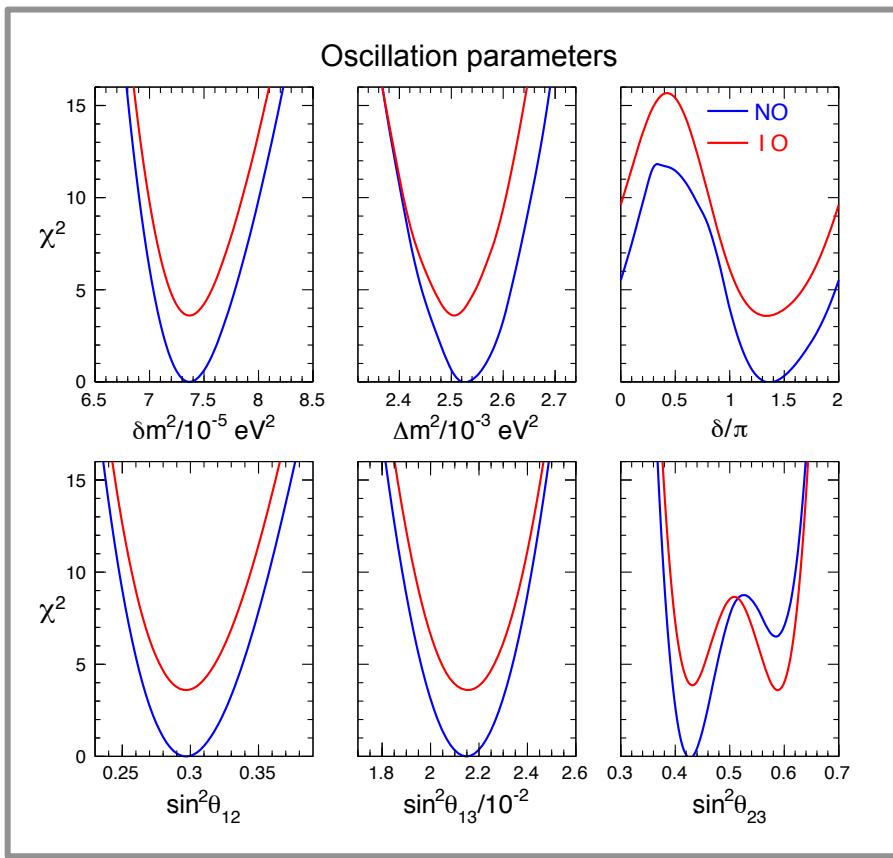
Talk by  
P. Hernandez

P. Hernandez et al.  
arXiv:1606.06719

**Prediction depends also on the value of  $\delta$**

# **3-flavor fit**

# Global 3ν oscillation analysis (2017)



NO: Normal Ordering  
IO: Inverted Ordering

~ **2 $\sigma$  preference for NO**

**Preference for  $\delta \in [\pi, 2\pi]$  ( $\sin \delta < 0$ )**

**Octant of  $\theta_{23}$**   
- lower in NO  
- no preference in IO

Capozzi, Di Valentino, Lisi, Marrone, Melchiorri, A.P,  
PRD 95, 096014 (2017) arXiv:1703.04471

# Estimates of the 3-flavor parameters

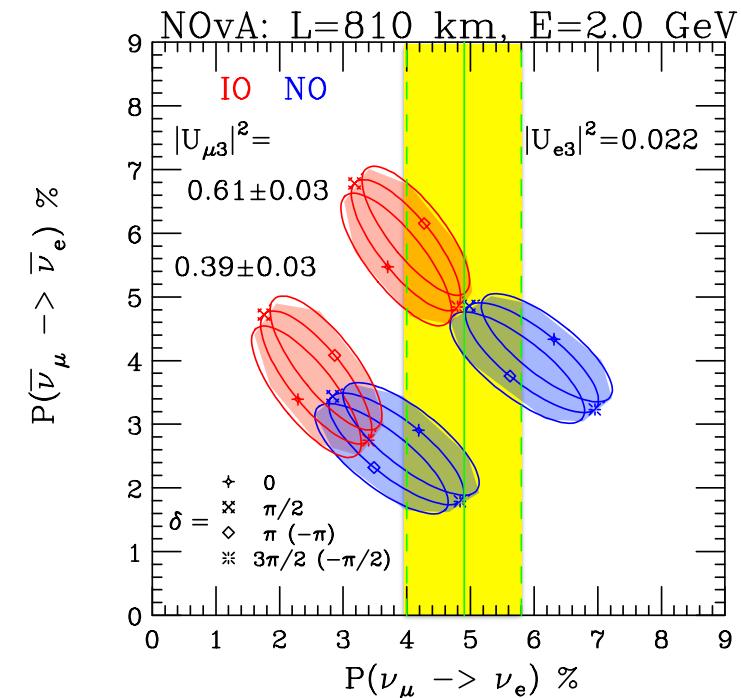
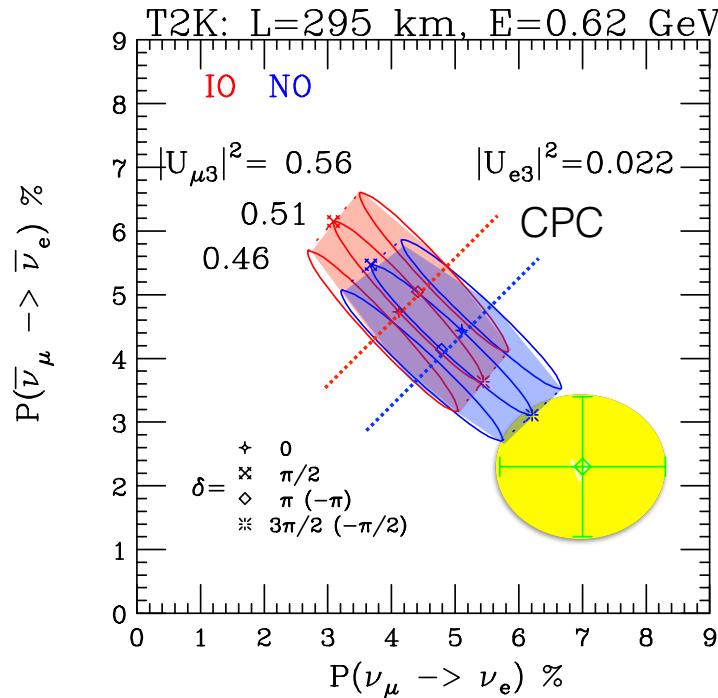
Parameter	Ordering	Best fit	$1\sigma$ range	$2\sigma$ range	$3\sigma$ range
$\delta m^2/10^{-5}$ eV $^2$	NO, IO, Any	7.37	7.21 – 7.54	7.07 – 7.73	6.93 – 7.96
$\sin^2 \theta_{12}/10^{-1}$	NO, IO, Any	2.97	2.81 – 3.14	2.65 – 3.34	2.50 – 3.54
$ \Delta m^2 /10^{-3}$ eV $^2$	NO	2.525	2.495 – 2.567	2.454 – 2.606	2.411 – 2.646
	IO	2.505	2.473 – 2.539	2.430 – 2.582	2.390 – 2.624
	Any	2.525	2.495 – 2.567	2.454 – 2.606	2.411 – 2.646
$\sin^2 \theta_{13}/10^{-2}$	NO	2.15	2.08 – 2.22	1.99 – 2.31	1.90 – 2.40
	IO	2.16	2.07 – 2.24	1.98 – 2.33	1.90 – 2.42
	Any	2.15	2.08 – 2.22	1.99 – 2.31	1.90 – 2.40
$\sin^2 \theta_{23}/10^{-1}$	NO	4.25	4.10 – 4.46	3.95 – 4.70	3.81 – 6.15
	IO	5.89	4.17 – 4.48 $\oplus$ 5.67 – 6.05	3.99 – 4.83 $\oplus$ 5.33 – 6.21	3.84 – 6.36
	Any	4.25	4.10 – 4.46	3.95 – 4.70 $\oplus$ 5.75 – 6.00	3.81 – 6.26
$\delta/\pi$	NO	1.38	1.18 – 1.61	1.00 – 1.90	0 – 0.17 $\oplus$ 0.76 – 2
	IO	1.31	1.12 – 1.62	0.92 – 1.88	0 – 0.15 $\oplus$ 0.69 – 2
	Any	1.38	1.18 – 1.61	1.00 – 1.90	0 – 0.17 $\oplus$ 0.76 – 2

Best estimates and fractional errors (defined as 1/6 of  $\pm 3\sigma$  ranges):

$$\begin{aligned}
 \delta m^2/\text{eV}^2 &\sim 7.4 \times 10^{-5} & \pm 2.3\% \\
 \Delta m^2/\text{eV}^2 &\sim 2.5 \times 10^{-3} & \pm 1.6\% \\
 \sin^2 \theta_{12} &\sim 0.30 & \pm 5.8\% \\
 \sin^2 \theta_{13} &\sim 0.022 & \pm 4.0\% \\
 \sin^2 \theta_{23} &\sim 0.5 & \pm 9.0\%
 \end{aligned}$$

# How the hints of CPV & MH arise (1)

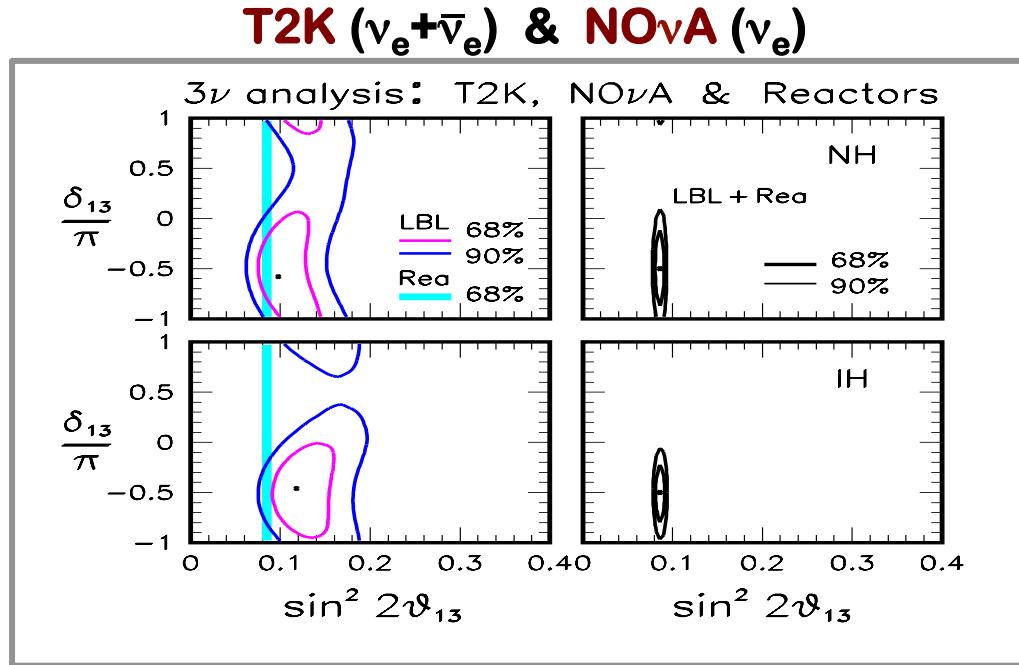
## T2K and NO $\nu$ A biprobability plots



S. Parke @ Invisibles 2016

Experimental data closer to  $\delta = -\pi/2$  and NO

# Numerical analysis of T2K and NO $\nu$ A

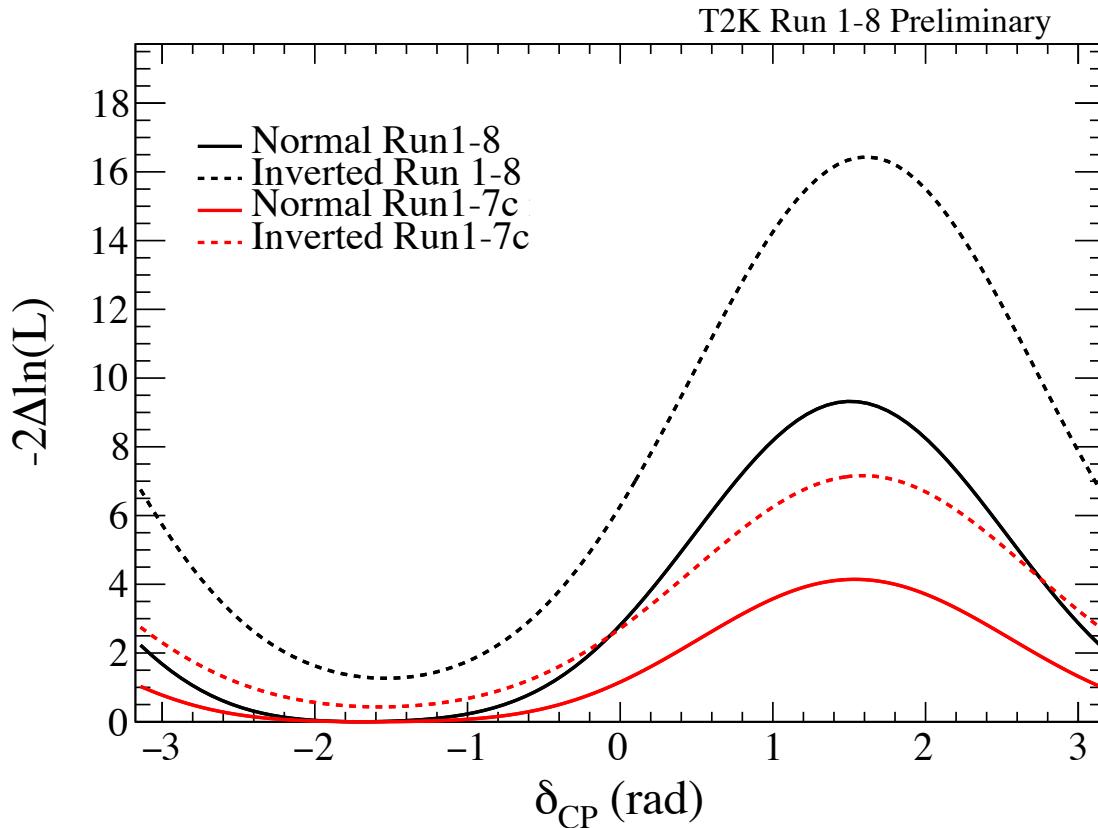


A.P., PLB 757 142-147 (2016) arXiv: 1509.03148

- Preference for CPV in T2K+NO $\nu$ A
- Reinforced when T2K+NO $\nu$ A are combined with Reactors
- IH slightly disfavored because of LBL-REA tension

# Latest T2K data confirm the trend

M. Hartz,  
KEK Colloquium,  
August 4, 2017

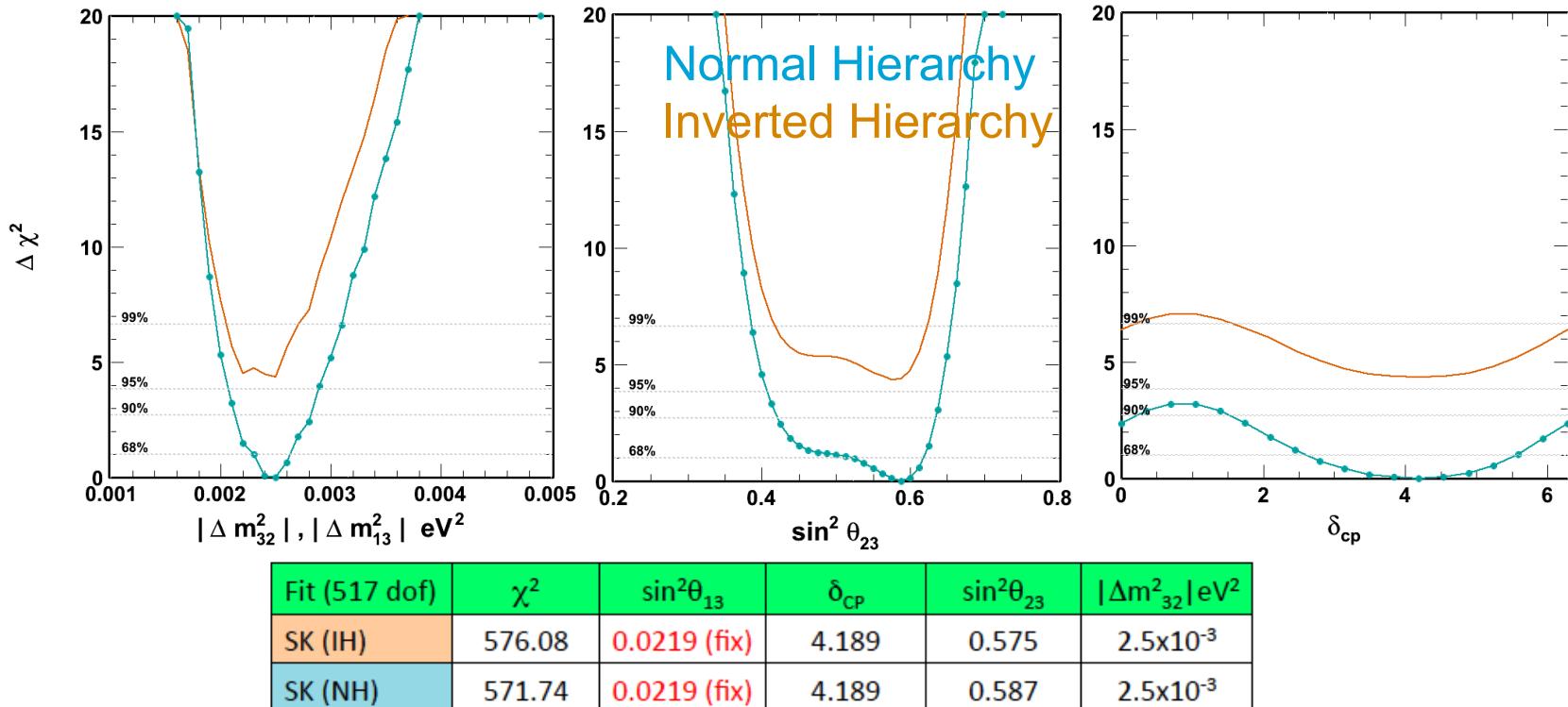


Summer 2017

Summer 2016  
(no CC1 $\pi$  sample)

# How the hints of CPV & MH arise (2)

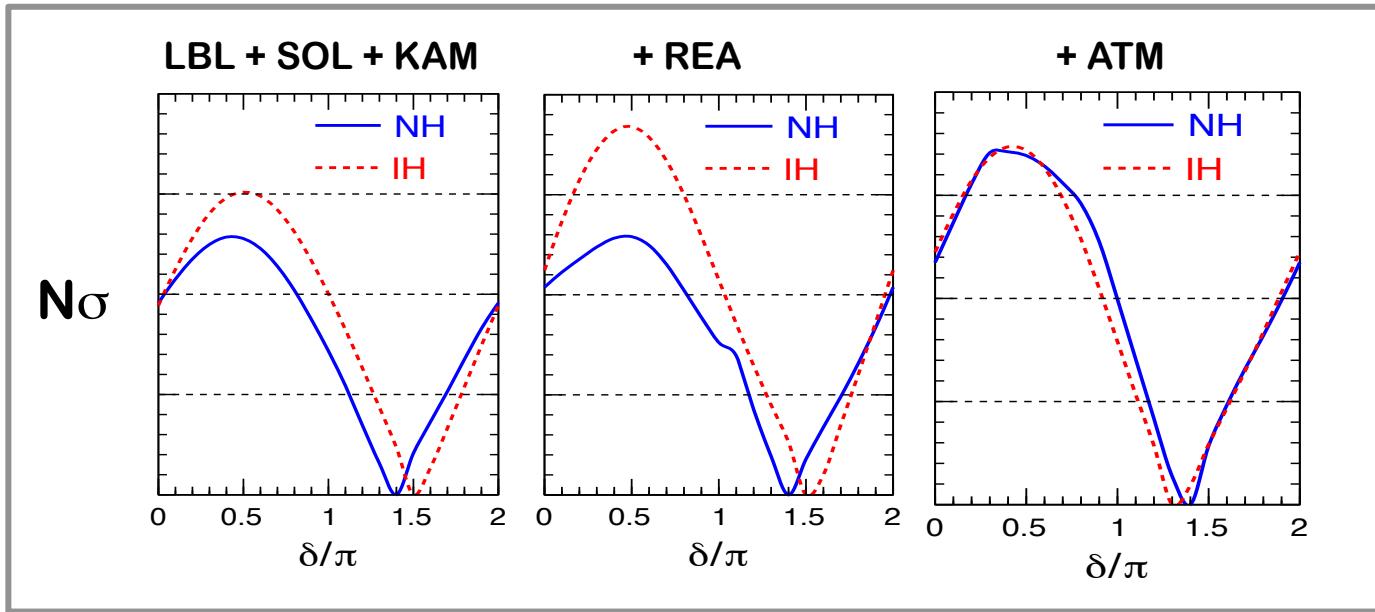
## SK atmospheric neutrinos



- Mass hierarchy:  $\Delta\chi^2 = \chi^2_{\text{NH}} - \chi^2_{\text{IH}} = -4.3$  (-3.1 expected)

M. Shiozawa @ NeuTel 2017

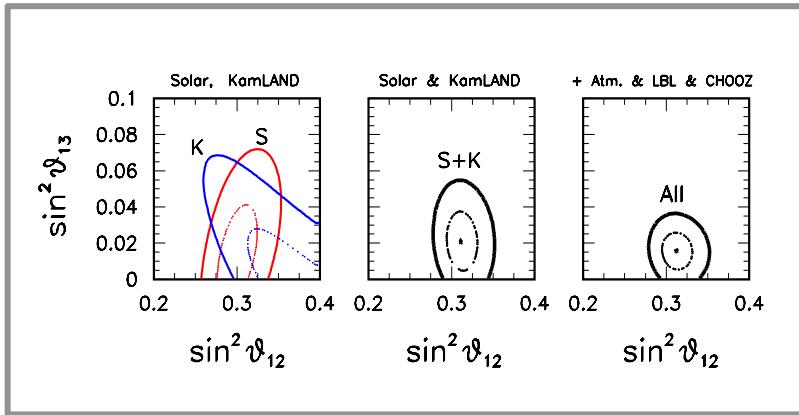
# CPV indication reinforced for increasingly rich data set



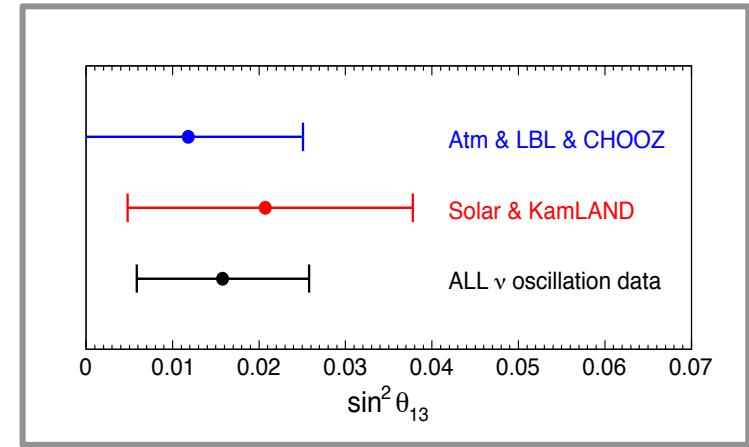
Supplementary to PRD 95, 096014 (2017) arXiv:1703.04471

This is a good sign!...

# A déjà vu: First hints of $\theta_{13} > 0$



Fogli, Lisi, Marrone, A.P., Rotunno,  
Phys. Rev. Lett. (2008)



Also in that case we had two weak but converging hints

The same story may be repeated with  $\delta$  !

# 4-flavor fit

# Beyond the standard picture

**Many extensions of the Standard Model predict  
new effects in neutrino oscillations**

**An incomplete list:**

- ✓ • Light sterile neutrinos
- Non standard neutrino interactions (NSI)
- Non unitarity of the PMNS matrix
- Long-range forces
- Lorentz and CPT violations
- Quantum decoherence ...

# Light sterile neutrinos

Wide interest in the scientific community

26/09/17

Antonio Palazzo, UNIBA & INFN

22

arXiv:1204.5379v1 [hep-ph] 18 Apr 2012

## Light Sterile Neutrinos: A White Paper

- K. N. Abazajian<sup>a,1</sup> M. A. Acero,<sup>2</sup> S. K. Agarwalla,<sup>3</sup> A. A. Aguilar-Arevalo,<sup>2</sup> C. H. Albright,<sup>4,5</sup> S. Antusch,<sup>6</sup> C. A. Argüelles,<sup>7</sup> A. B. Balantekin,<sup>8</sup> G. Barenboim<sup>a,3</sup> V. Barger,<sup>8</sup> P. Bernardini,<sup>9</sup> F. Bezrukov,<sup>10</sup> O. E. Bjaelde,<sup>11</sup> S. A. Bogacz,<sup>12</sup> N. S. Bowden,<sup>13</sup> A. Boyarsky,<sup>14</sup> A. Bravar,<sup>15</sup> D. Bravo Berguño,<sup>16</sup> S. J. Brice,<sup>5</sup> A. D. Bross,<sup>5</sup> B. Caccianiga,<sup>17</sup> F. Cavanna,<sup>18,19</sup> E. J. Chun,<sup>20</sup> B. T. Cleveland,<sup>21</sup> A. P. Collin,<sup>22</sup> P. Coloma,<sup>16</sup> J. M. Conrad,<sup>23</sup> M. Cribier,<sup>22</sup> A. S. Cucoanes,<sup>24</sup> J. C. D'Olivo,<sup>2</sup> S. Das,<sup>25</sup> A. de Gouvea,<sup>26</sup> A. V. Derbin,<sup>27</sup> R. Dharmapalan,<sup>28</sup> J. S. Diaz,<sup>29</sup> X. J. Ding,<sup>16</sup> Z. Djurcic,<sup>30</sup> A. Donini,<sup>31,3</sup> D. Duchesneau,<sup>32</sup> H. Ejiri,<sup>33</sup> S. R. Elliott,<sup>34</sup> D. J. Ernst,<sup>35</sup> A. Esmaili,<sup>36</sup> J. J. Evans,<sup>37,38</sup> E. Fernandez-Martinez,<sup>39</sup> E. Figueroa-Feliciano,<sup>23</sup> B. T. Fleming<sup>a,18</sup> J. A. Formaggio<sup>a,23</sup> D. Franco,<sup>40</sup> J. Gaffiot,<sup>22</sup> R. Gandhi,<sup>41</sup> Y. Gao,<sup>42</sup> G. T. Garvey,<sup>34</sup> V. N. Gavrin,<sup>43</sup> P. Ghoshal,<sup>41</sup> D. Gibin,<sup>44</sup> C. Giunti,<sup>45</sup> S. N. Gninenko,<sup>43</sup> V. V. Gorbachev,<sup>43</sup> D. S. Gorburunov,<sup>43</sup> R. Guenette,<sup>18</sup> A. Guglielmi,<sup>44</sup> F. Halzen,<sup>46,8</sup> J. Hamann,<sup>11</sup> S. Hannestad,<sup>11</sup> W. Haxton,<sup>47,48</sup> K. M. Heeger,<sup>8</sup> R. Henning,<sup>49,50</sup> P. Hernandez,<sup>3</sup> P. Huber,<sup>b,16</sup> W. Huelsnitz,<sup>34,51</sup> A. Ianni,<sup>52</sup> T. V. Ibragimova,<sup>43</sup> Y. Karadzhov,<sup>15</sup> G. Karagiorgi,<sup>53</sup> G. Keefer,<sup>13</sup> Y. D. Kim,<sup>54</sup> J. Kopp<sup>a,5</sup> V. N. Kornoukhov,<sup>55</sup> A. Kusenko,<sup>56,57</sup> P. Kyberd,<sup>58</sup> P. Langacker,<sup>59</sup> Th. Lasserre<sup>a,22,40</sup> M. Laveder,<sup>60</sup> A. Letourneau,<sup>22</sup> D. Lhuillier,<sup>22</sup> Y. F. Li,<sup>61</sup> M. Lindner,<sup>62</sup> J. M. Link<sup>b,16</sup> B. L. Littlejohn,<sup>8</sup> P. Lombardi,<sup>17</sup> K. Long,<sup>63</sup> J. Lopez-Pavon,<sup>64</sup> W. C. Louis<sup>a,34</sup> L. Ludhova,<sup>17</sup> J. D. Lykken,<sup>5</sup> P. A. N. Machado,<sup>65,66</sup> M. Maltoni,<sup>31</sup> W. A. Mann,<sup>67</sup> D. Marfatia,<sup>68</sup> C. Mariani,<sup>53,16</sup> V. A. Matveev,<sup>43,69</sup> N. E. Mavromatos,<sup>70,39</sup> A. Melchiorri,<sup>71</sup> D. Meloni,<sup>72</sup> O. Mena,<sup>3</sup> G. Mention,<sup>22</sup> A. Merle,<sup>73</sup> E. Meroni,<sup>17</sup> M. Mezzetto,<sup>44</sup> G. B. Mills,<sup>34</sup> D. Minic,<sup>16</sup> L. Miramonti,<sup>17</sup> D. Mohapatra,<sup>16</sup> R. N. Mohapatra,<sup>51</sup> C. Montanari,<sup>74</sup> Y. Mori,<sup>75</sup> Th. A. Mueller,<sup>76</sup> H. P. Mumm,<sup>77</sup> V. Muratova,<sup>27</sup> A. E. Nelson,<sup>78</sup> J. S. Nico,<sup>77</sup> E. Noah,<sup>15</sup> J. Nowak,<sup>79</sup> O. Yu. Smirnov,<sup>69</sup> M. Obolensky,<sup>40</sup> S. Pakvasa,<sup>80</sup> O. Palamara,<sup>18,52</sup> M. Pallavicini,<sup>81</sup> S. Pascoli,<sup>82</sup> L. Patrizii,<sup>83</sup> Z. Pavlovic,<sup>34</sup> O. L. G. Peres,<sup>36</sup> H. Pessard,<sup>32</sup> F. Pietropaolo,<sup>44</sup> M. L. Pitt,<sup>16</sup> M. Popovic,<sup>5</sup> J. Pradler,<sup>84</sup> G. Ranucci,<sup>17</sup> H. Ray,<sup>85</sup> S. Razzaque,<sup>86</sup> B. Rebel,<sup>5</sup> R. G. H. Robertson,<sup>87,78</sup> W. Rodejohann<sup>a,62</sup> S. D. Rountree,<sup>16</sup> C. Rubbia,<sup>39,52</sup> O. Ruchayskiy,<sup>39</sup> P. R. Sala,<sup>17</sup> K. Scholberg,<sup>88</sup> T. Schwetz<sup>a,62</sup> M. H. Shaevitz,<sup>53</sup> M. Shaposhnikov,<sup>89</sup> R. Shrock,<sup>90</sup> S. Simone,<sup>91</sup> M. Skorokhvatov,<sup>92</sup> M. Sorel,<sup>3</sup> A. Sousa,<sup>93</sup> D. N. Spergel,<sup>94</sup> J. Spitz,<sup>23</sup> L. Stanco,<sup>44</sup> I. Stancu,<sup>28</sup> A. Suzuki,<sup>95</sup> T. Takeuchi,<sup>16</sup> I. Tamborra,<sup>96</sup> J. Tang,<sup>97,98</sup> G. Testera,<sup>81</sup> X. C. Tian,<sup>99</sup> A. Tonazzo,<sup>40</sup> C. D. Tunnell,<sup>100</sup> R. G. Van de Water,<sup>34</sup> L. Verde,<sup>101</sup> E. P. Veretenkin,<sup>43</sup> C. Vignoli,<sup>52</sup> M. Vivier,<sup>22</sup> R. B. Vogelaar,<sup>16</sup> M. O. Wascko,<sup>63</sup> J. F. Wilkerson,<sup>49,102</sup> W. Winter,<sup>97</sup> Y. Y. Wong<sup>a,25</sup> T. T. Yanagida,<sup>57</sup> O. Yasuda,<sup>103</sup> M. Yeh,<sup>104</sup> F. Yermia,<sup>24</sup> Z. W. Yokley,<sup>16</sup> G. P. Zeller,<sup>5</sup> L. Zhan,<sup>61</sup> and H. Zhang<sup>62</sup>

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<sup>3</sup>Instituto de Física Corpuscular, CSIC and Universidad de Valencia

<sup>4</sup>Northern Illinois University

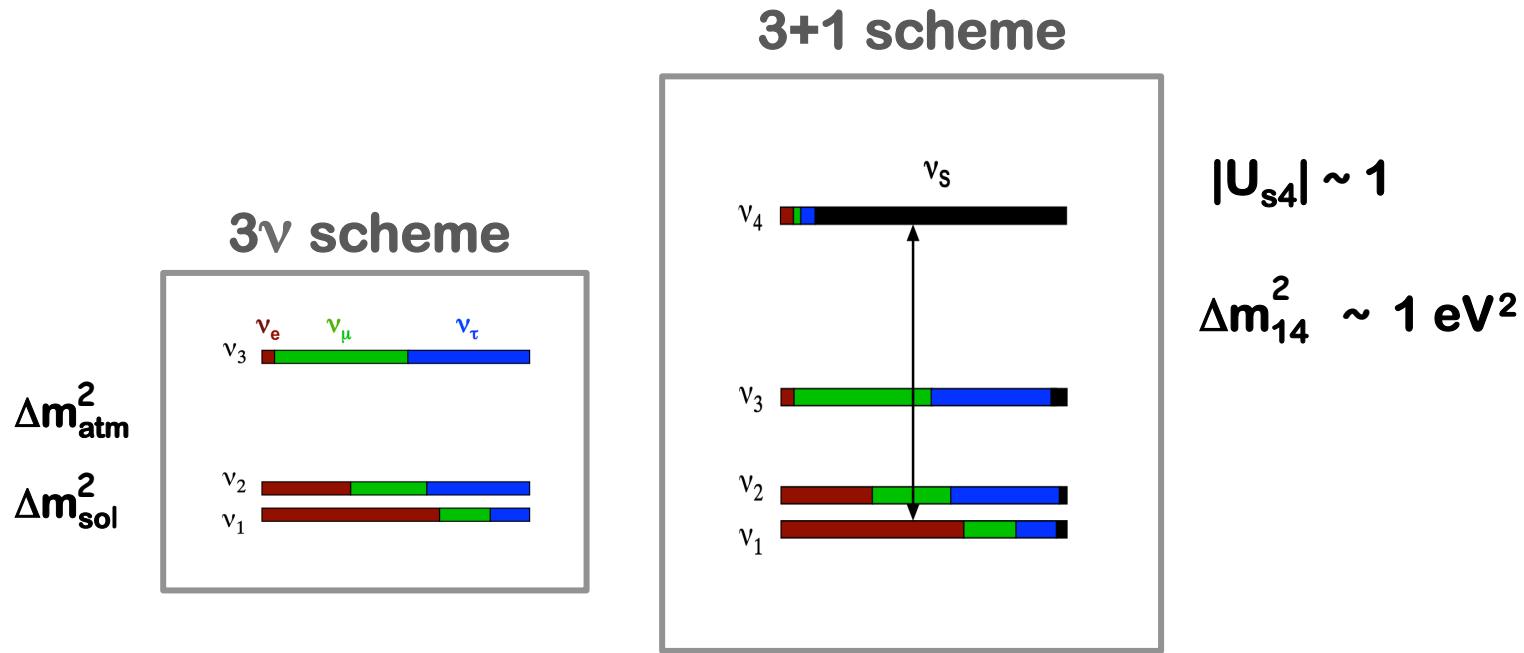
<sup>5</sup>Fermi National Accelerator Laboratory

<sup>6</sup>University of Basel

<sup>a</sup>Section editor

<sup>b</sup>Editor and corresponding author (pahuber@vt.edu and jmlink@vt.edu)

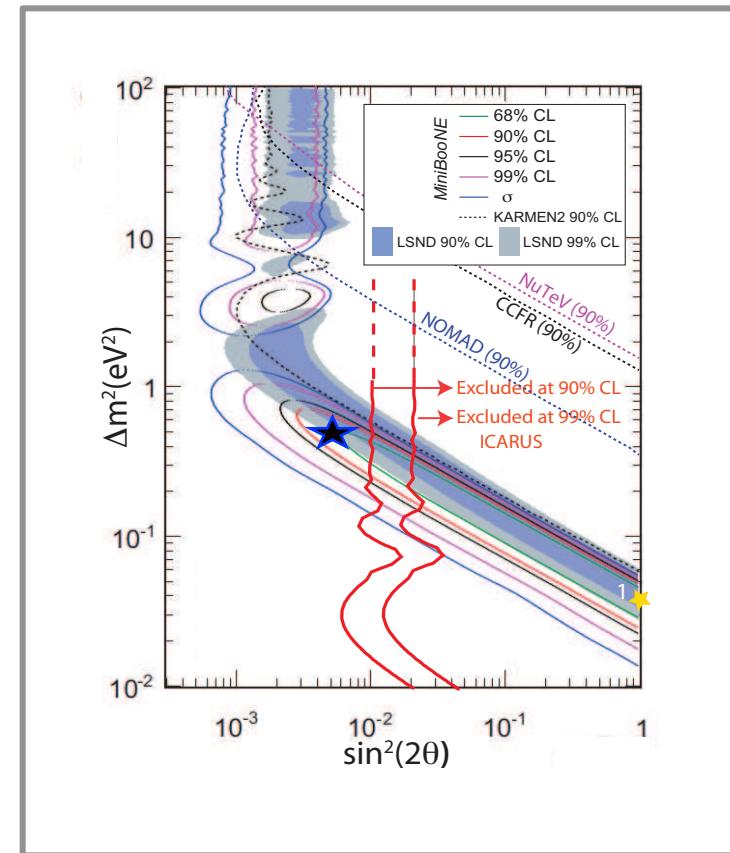
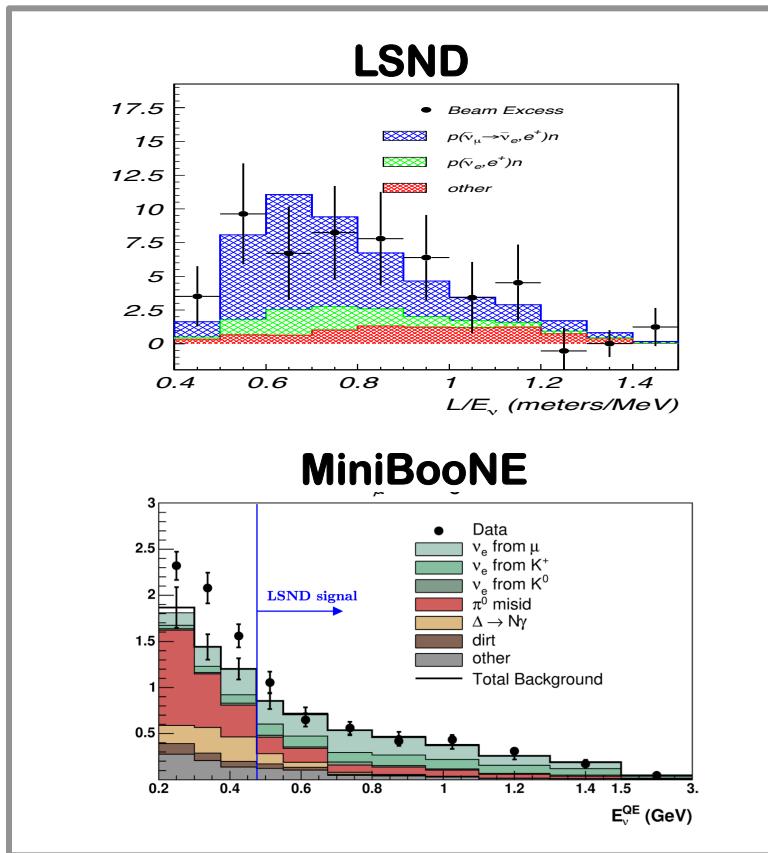
# How to enlarge the 3-flavor scheme



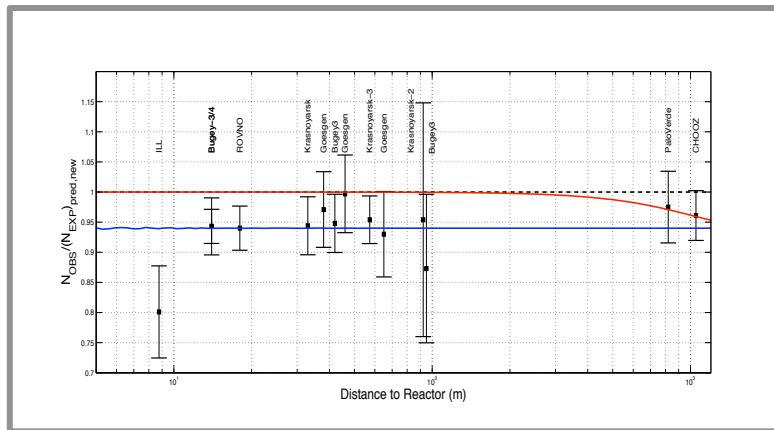
At LBL the effective 2-flavor SBL description is no more valid and calculations should be done in the 3+1 (or 3+N<sub>s</sub>) scheme

# 1) The SBL accelerator anomalies

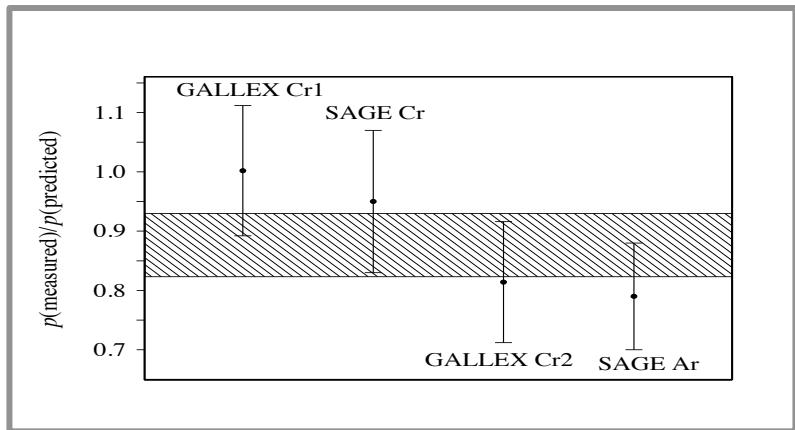
(unexplained  $\nu_e$  appearance in a  $\nu_\mu$  beam)



## 2) The reactor and gallium anomalies (unexplained $\nu_e$ disappearance)



Mention et al. arXiv:1101:2755 [hep-ex]

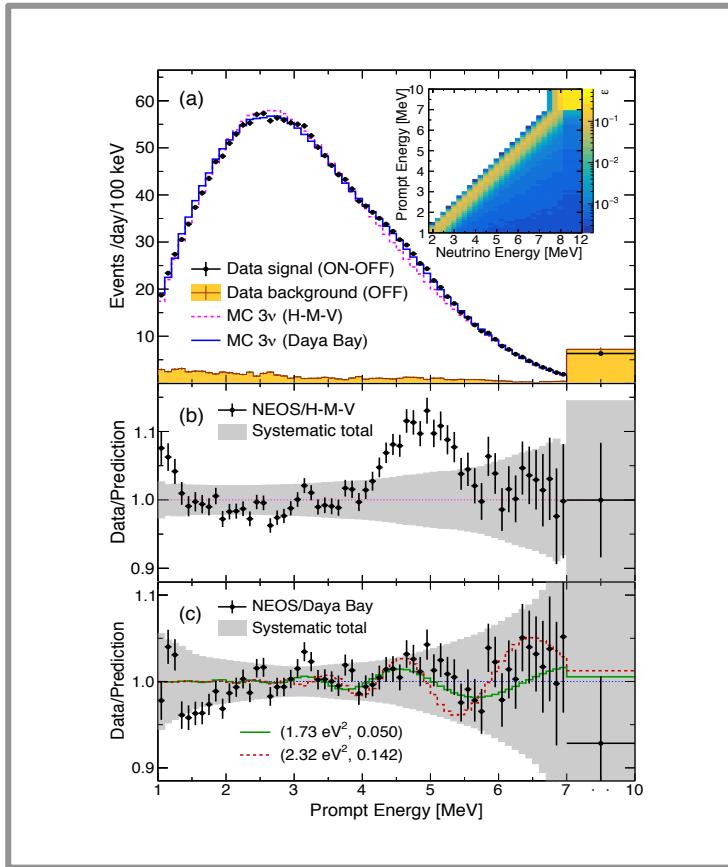


SAGE coll., PRC 73 (2006) 045805

**Warning: both are mere normalization issues**

**The culprit may be hidden in unknown systematics**

# 3) NEOS: a new hint of sterile neutrinos?



NEOS arXiv:1610:05134

**Hanbit Nuclear Power Complex, Korea**

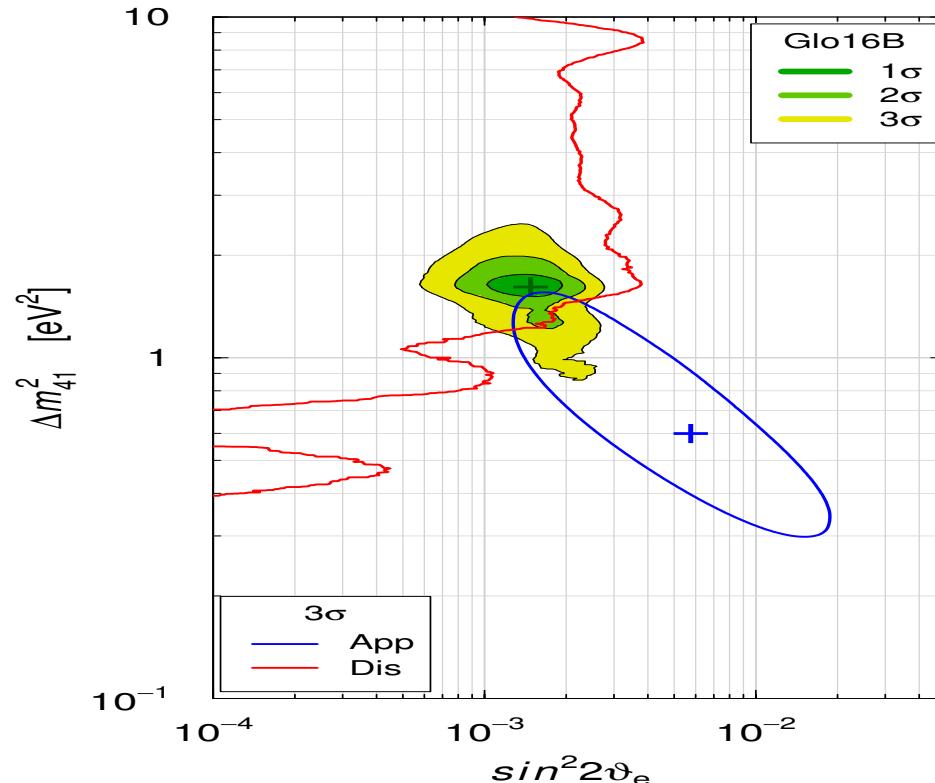
**Detector: 1 ton  
Gd-loaded liquid scintillator 24 m from the reactor core**

**Daya-Bay absolute spectrum used as a normalization**

**Oscillating pattern visible after normalization**

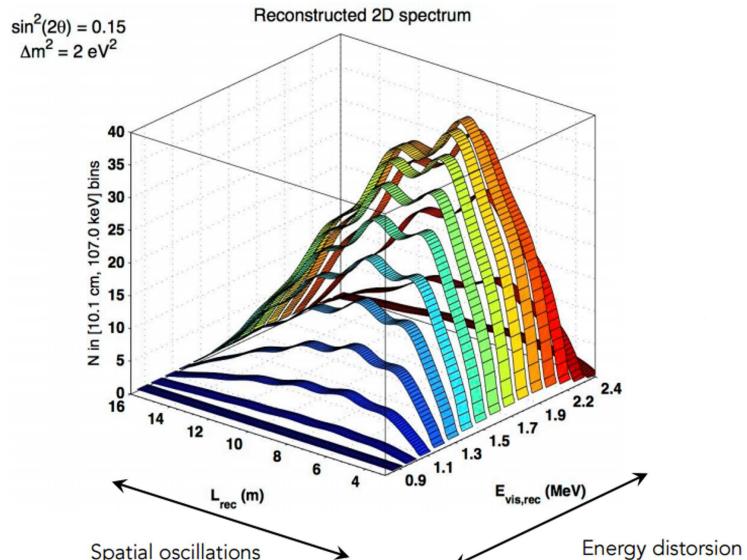
# Global SBL data fit in the 3+1 scheme

Gariazzo et al. arXiv:1703.00860

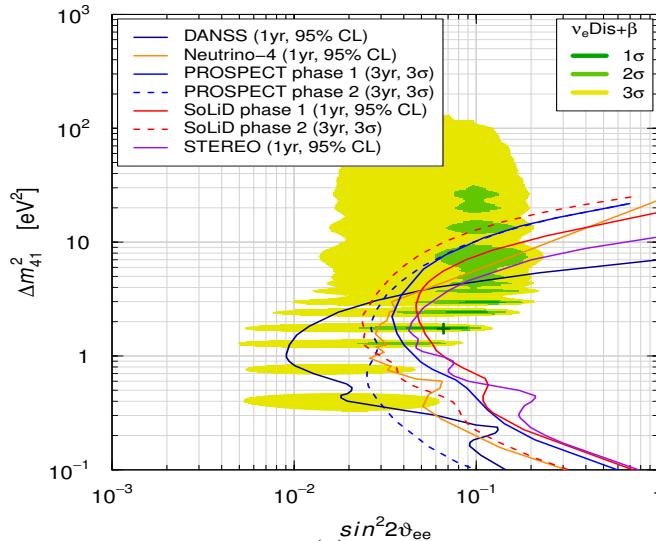


# The smoking gun

SOX experiment @ LNGS



Gariazzo et al., 1703.00860



**Observation of the oscillation pattern at SBL experiments**

**Many projects are under consideration**

**But sterile neutrinos are not just a SBL “affair”...**

# An intrinsic limitation of SBL

At SBL atm/sol oscillations are negligible

$$\frac{L}{E} \sim \frac{m}{\text{MeV}}$$

$$\begin{aligned}\Delta_{12} &\simeq 0 \\ \Delta_{13} &\simeq 0\end{aligned}$$

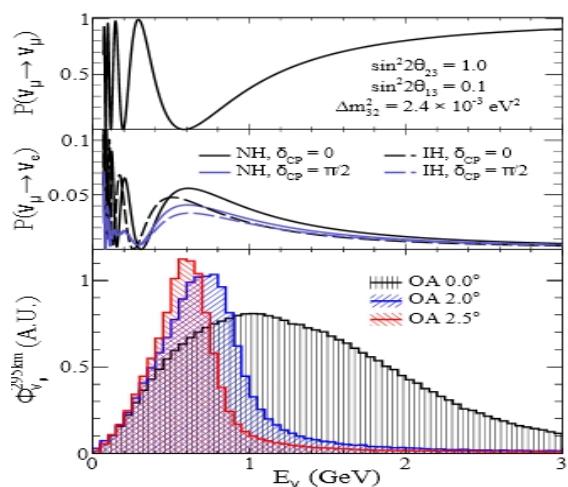
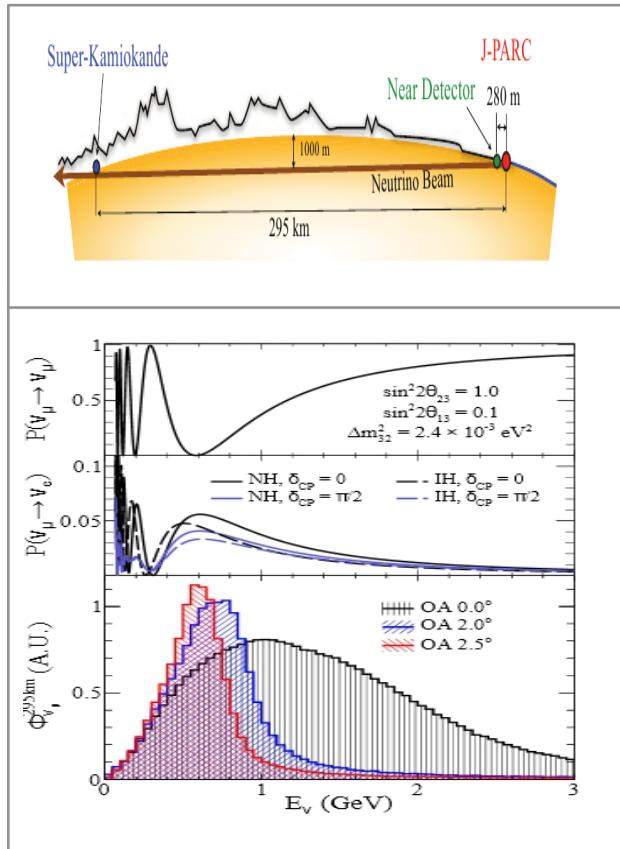
$$\Delta_{ij} = \frac{\Delta m^2_{ij} L}{4E}$$

Impossible to observe phenomena of interference between the new frequency ( $\Delta_{14} \sim 1$ ) and atm/sol ones

This is relevant because we need to observe such phenomena in order to measure the new CP-phases induced by sterile neutrinos

But we have LBL, which are sensitive interferometers

# LBL Experiments: T2K & NO $\nu$ A

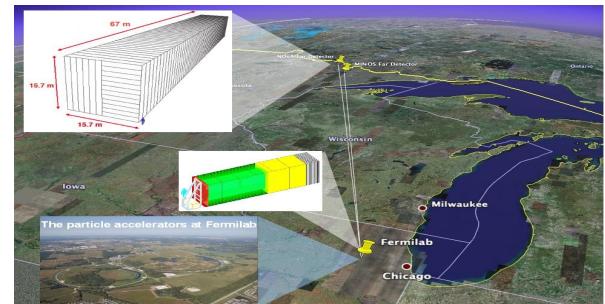


$E = 0.6 \text{ GeV}$   
 $L = 295 \text{ km}$

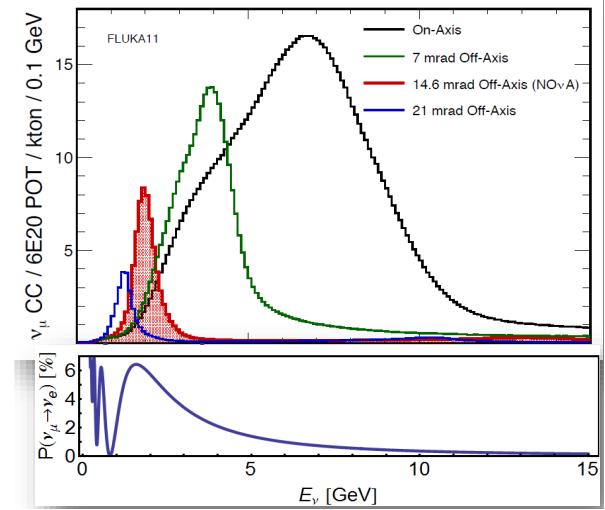
off-axis  
beam

$$\Delta = \frac{\Delta m_{13}^2 L}{4E} \gtrsim \frac{\pi}{2}$$

First  
oscillation  
maximum



Far Detector flux   NOvA Simulation



$E = 2 \text{ GeV}$   
 $L = 810 \text{ km}$

# LBL transition probability in 3-flavor

$$P_{\nu_\mu \rightarrow \nu_e}^{3\nu} = P^{\text{ATM}} + P^{\text{SOL}} + P^{\text{INT}}$$

**in vacuum:**

$$P^{\text{ATM}} = 4s_{23}^2 s_{13}^2 \sin^2 \Delta$$

$$P^{\text{SOL}} = 4c_{12}^2 c_{23}^2 s_{12}^2 (\alpha \Delta)^2$$

$$P^{\text{INT}} = 8s_{23}s_{13}c_{12}c_{23}s_{12}(\alpha \Delta) \sin \Delta \cos(\Delta + \delta_{CP}).$$

$$\Delta = \frac{\Delta m_{31}^2 L}{4E}, \quad \alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2}$$

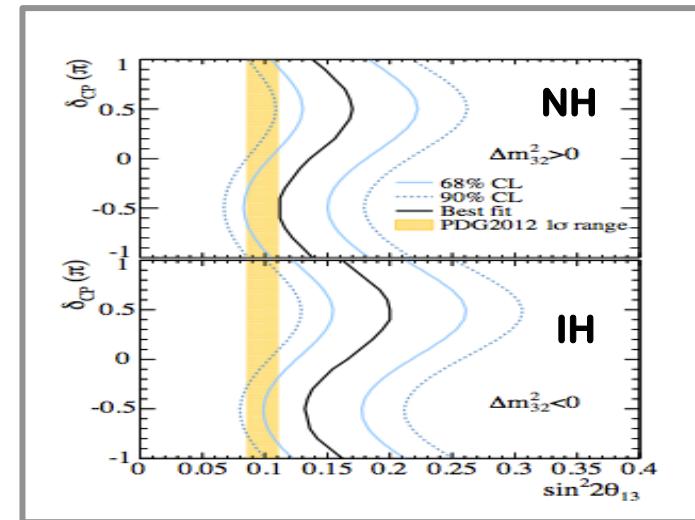
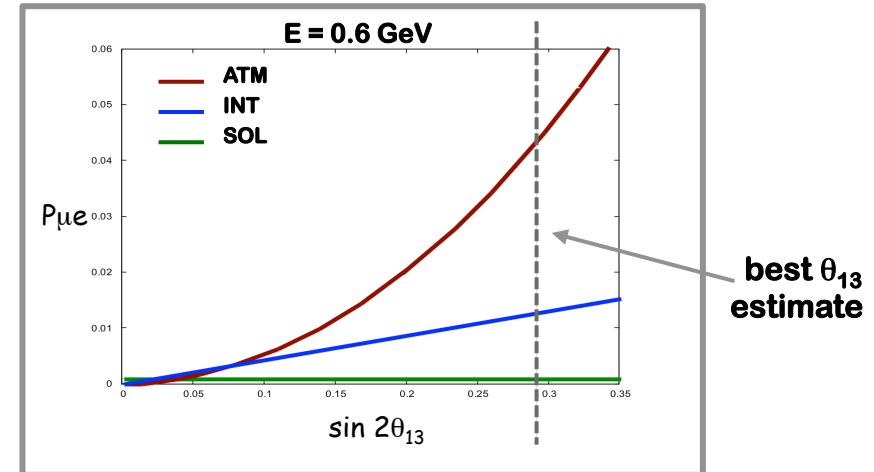
$$\begin{aligned} \Delta &\sim \pi/2 \\ \alpha &\sim 0.03 \end{aligned}$$

**P<sub>ATM</sub>** leading  $\rightarrow \theta_{13} > 0$

**P<sub>INT</sub>** subleading  $\rightarrow$  dependency on  $\delta$

**P<sub>SOL</sub>** negligible

Matter effects break  
NH-IH degeneracy



# Sterile vs bring new CPV sources

$$U = \tilde{R}_{34} \ R_{24} \ \tilde{R}_{14} \ R_{23} \ \underbrace{\tilde{R}_{13} \ R_{12}}_{3\nu}$$

$$R_{ij} = \begin{bmatrix} c_{ij} & s_{ij} \\ -s_{ij} & c_{ij} \end{bmatrix}$$

$$\tilde{R}_{ij} = \begin{bmatrix} c_{ij} & \tilde{s}_{ij} \\ -\tilde{s}_{ij}^* & c_{ij} \end{bmatrix}$$

$$\begin{aligned} s_{ij} &= \sin \theta_{ij} \\ c_{ij} &= \cos \theta_{ij} \\ \tilde{s}_{ij} &= s_{ij} e^{-i\delta_{ij}} \end{aligned}$$

$3\nu$   $\left\{ \begin{array}{l} \text{3 mixing angles} \\ \text{1 Dirac phases} \\ \text{2 Majorana phases} \end{array} \right.$

$3+1$   $\left\{ \begin{array}{l} 6 \\ 3 \\ 3 \end{array} \right.$

$3+N$   $\left\{ \begin{array}{l} 3+3N \\ 1+2N \\ 2+N \end{array} \right.$

Invisible at SBL but visible at LBL experiments...

# A new interference term in the 3+1 scheme

N. Klop & A.P., arXiv: 1412.7524 (PRD 2015)

- $\Delta_{14} \gg 1$  : fast oscillations are averaged out
- But interference of  $\Delta_{14}$  &  $\Delta_{13}$  survives and is observable

$$P_{\mu e}^{4\nu} \simeq P^{\text{ATM}} + P_I^{\text{INT}} + P_{II}^{\text{INT}}$$

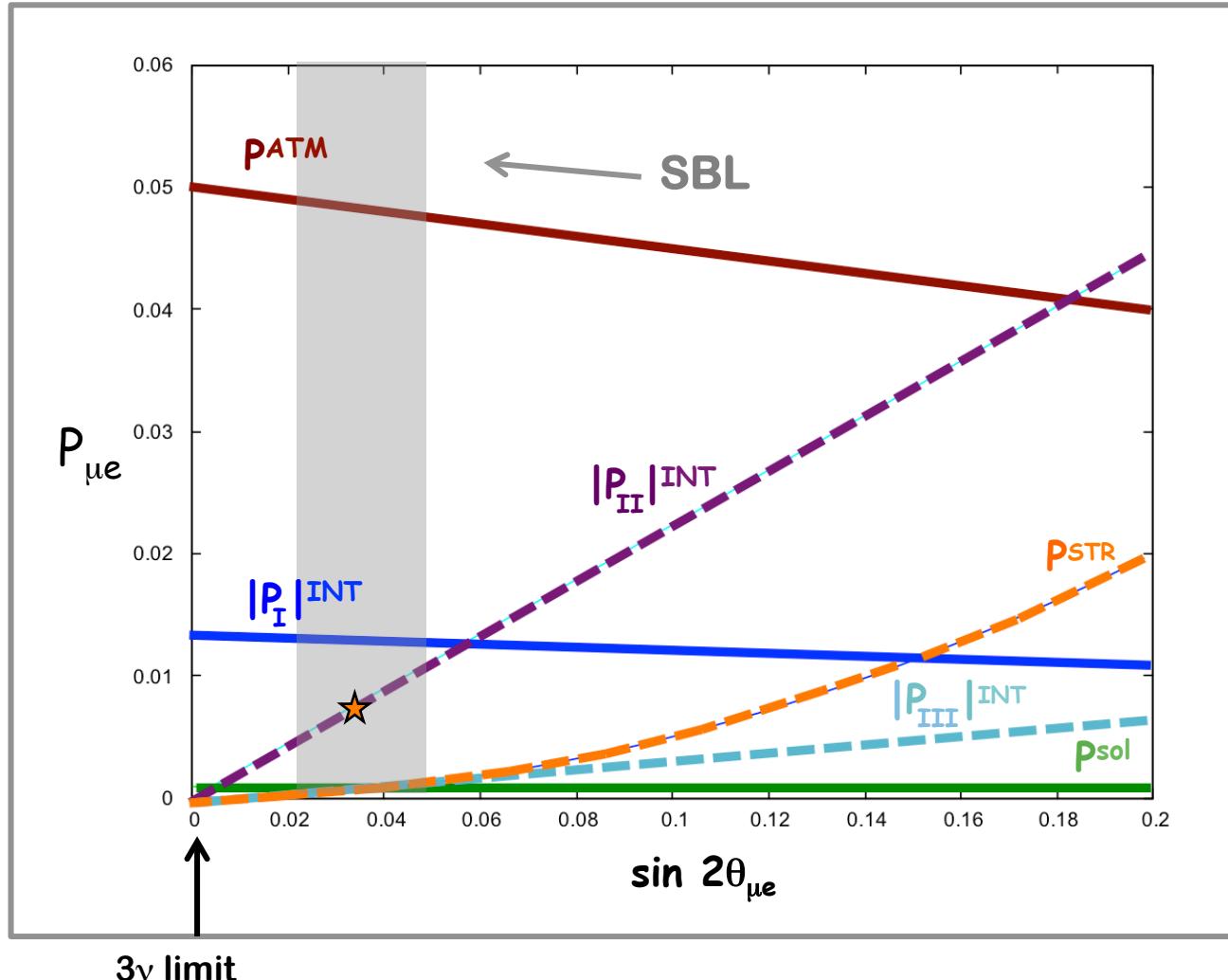
$$\begin{aligned} S_{13} &\sim S_{14} \sim S_{24} \sim 0.15 \sim \varepsilon \\ \alpha = \delta m^2 / \Delta m^2 &\sim 0.03 \sim \varepsilon^2 \end{aligned}$$

$$\left\{ \begin{array}{ll} P^{\text{ATM}} \simeq 4s_{23}^2 s_{13}^2 \sin^2 \Delta & \sim \varepsilon^2 \\ P_I^{\text{INT}} \simeq 8s_{13}s_{23}c_{23}s_{12}c_{12}(\underline{\alpha}\underline{\Delta}) \sin \Delta \cos(\Delta + \delta_{13}) & \sim \varepsilon^3 \\ P_{II}^{\text{INT}} \simeq 4s_{14}s_{24}s_{13}s_{23} \sin \Delta \sin(\Delta + \delta_{13} - \delta_{14}) & \sim \varepsilon^3 \end{array} \right.$$

**Sensitivity to the new CP-phase  $\delta_{14}$**

# Amplitude of the new interference term

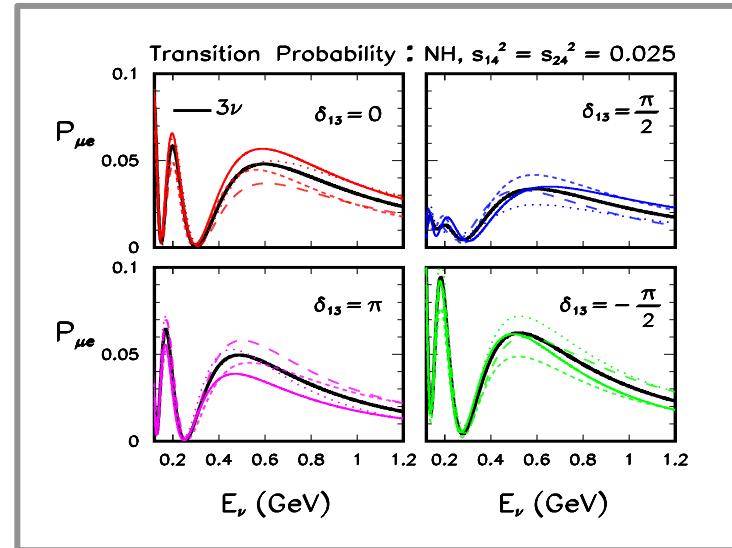
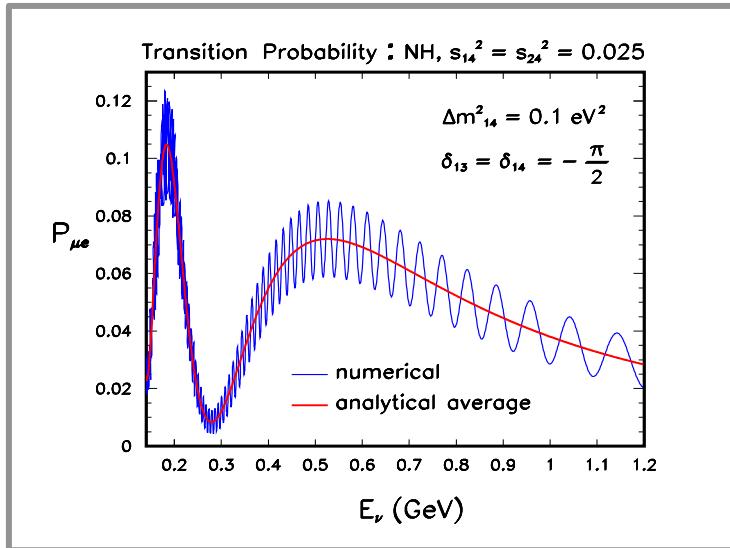
N. Klop & A.P., PRD (2015)



T2K  
 $\theta_{13} = 9^\circ$   
 $E = 0.6 \text{ GeV}$

$$\sin^2 2\theta_{\mu e} = 4|U_{e4}|^2 |U_{\mu 4}|^2$$

# Numerical examples of $4\nu$ probability



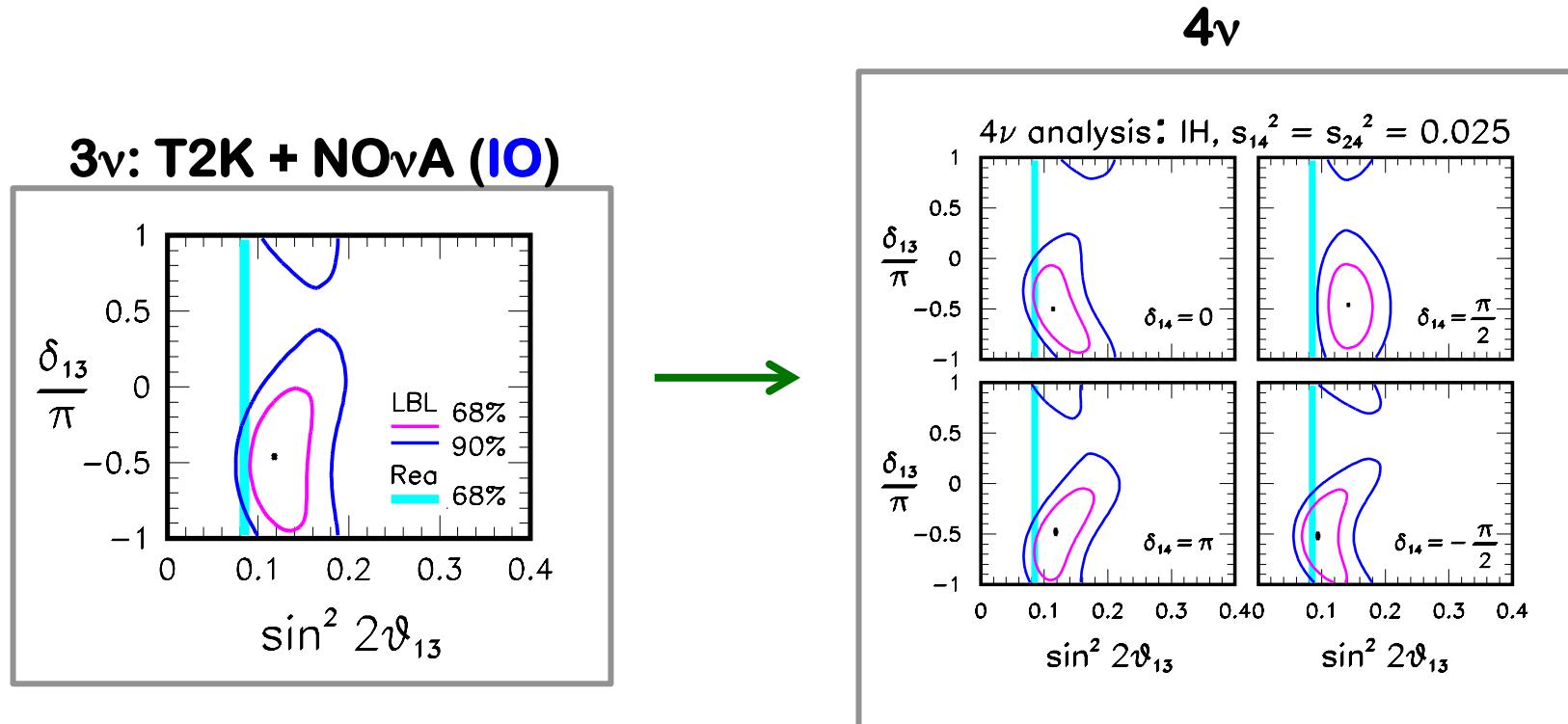
The fast oscillations get averaged out due to the finite energy resolution

Different line styles  
 $\Leftrightarrow$   
Different values of  $\delta_{14}$

The modifications induced by  $\delta_{14}$  are almost as large as those induced by the standard CP-phase  $\delta_{13}$

## Consequences...

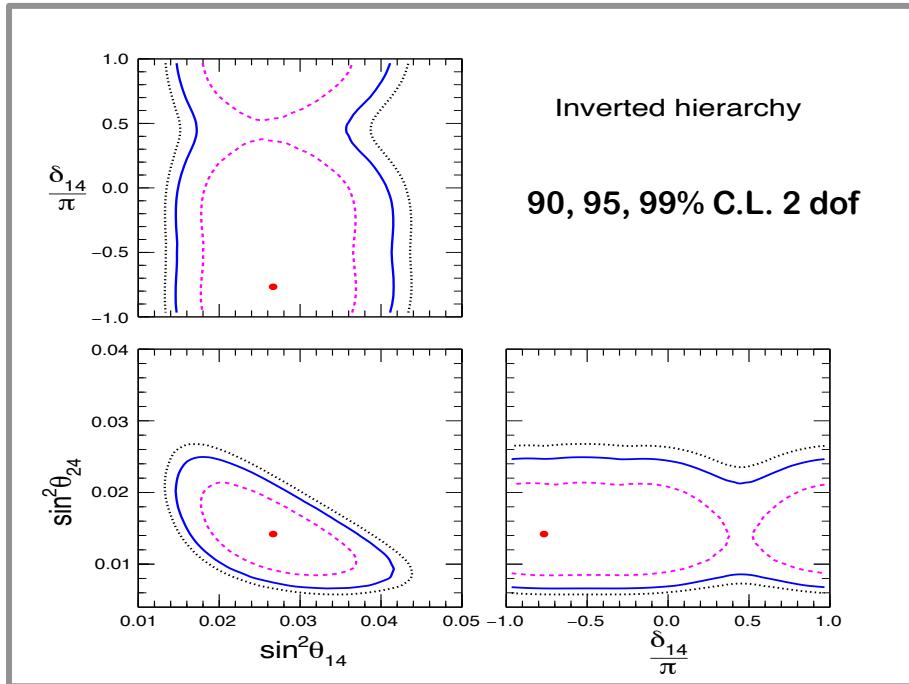
# LBL constraints change in the 3+1 scheme



A.P., PLB 757, 142 (2016) arXiv:1509.03148

# Joint SBL and LBL constraints on $[\theta_{14}, \theta_{24}, \delta_{14}]$

**SBL + LBL**



**SBL (all available data)**

**(Icecube and NEOS not included in this analysis)**

**LBL  $\equiv$  T2K + NO $\nu$ A**

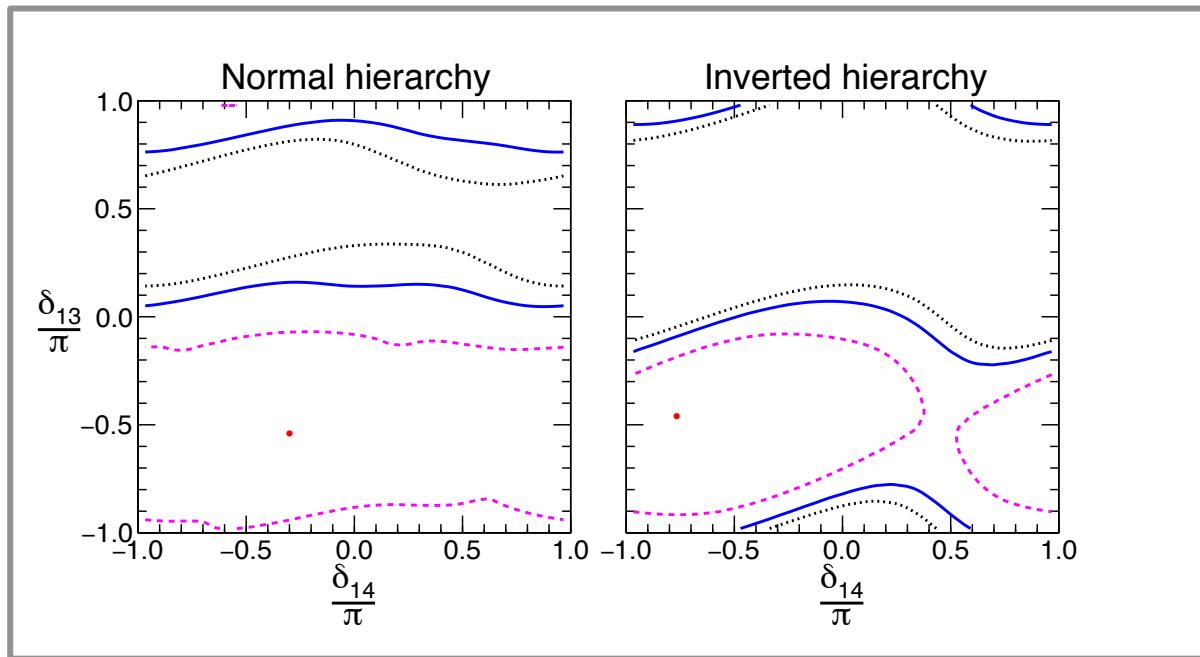
**(Neutrino 2016 data)**

Capozzi, Giunti, Laveder & A.P.,  
arXiv:1612.07764 (PRD 2017)

- $[\theta_{14}, \theta_{24}]$  determined by SBL experiments
- $\delta_{14}$  constrained by LBL experiments

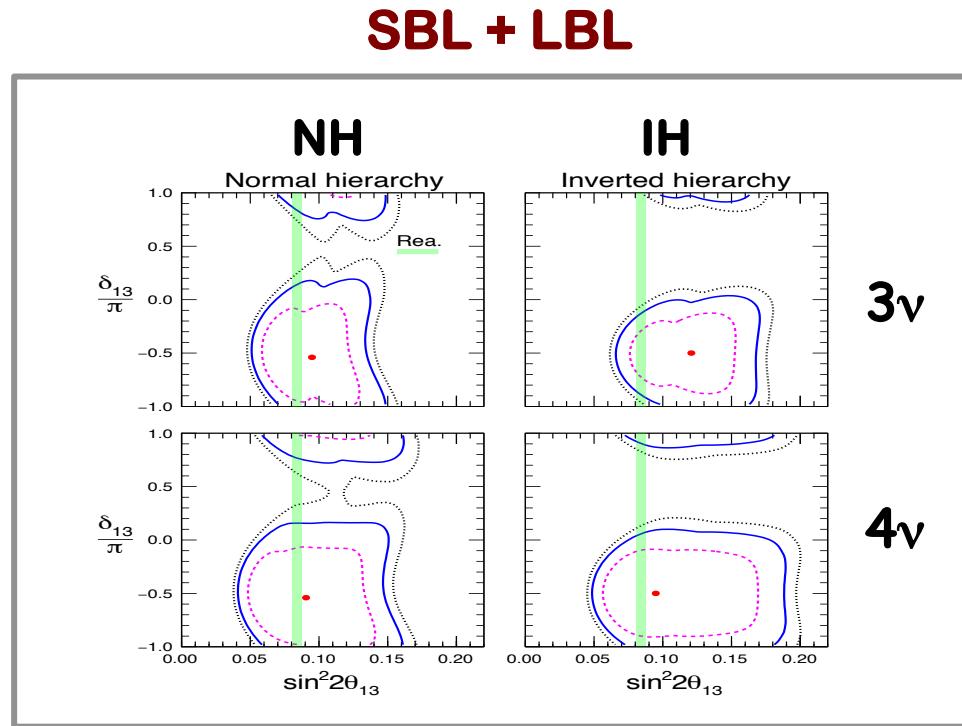
# Constraints on the two CP-phases

SBL + LBL



- $\delta_{13}$  is more constrained than  $\delta_{14}$
- Best fit values:  $\delta_{13} \sim \delta_{14} \sim -\pi/2$
- This information cannot be extracted from SBL alone !

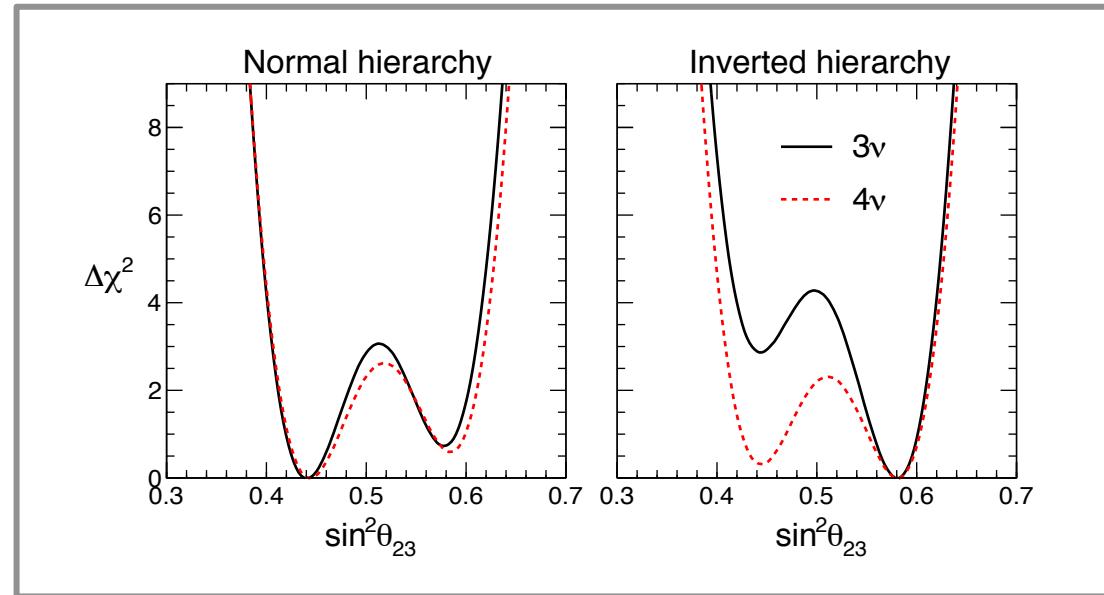
# Impact on the standard parameters $[\theta_{13}, \delta_{13}]$



- Allowed range for  $\theta_{13}$  from LBL alone gets enlarged
- Values preferred for  $\delta_{13} \equiv \delta$  basically unaltered
- Mismatch (in IH) of LBL and Reactors decreases in 3+1

# Impact of sterile neutrinos on $\theta_{23}$

SBL + LBL



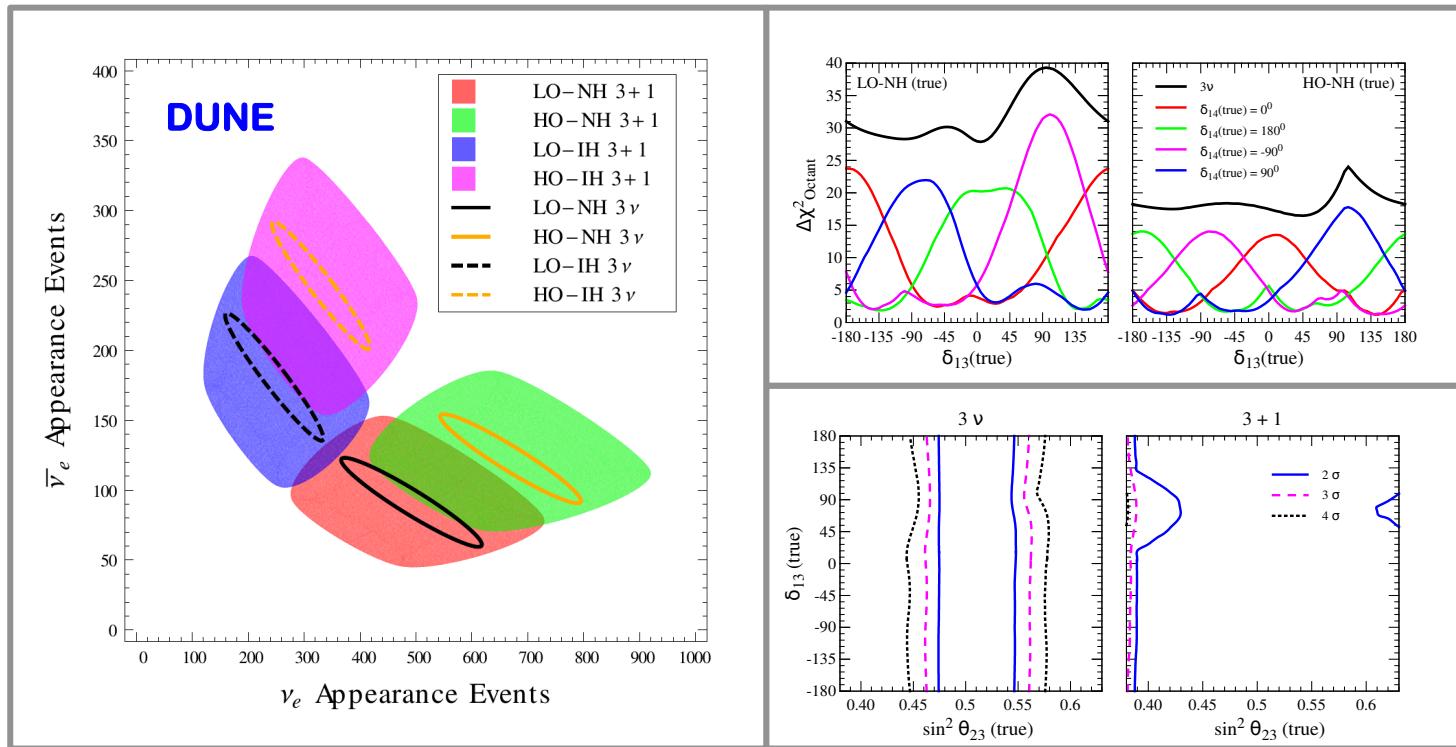
Indication for non-maximal  $\theta_{23}$  persists in 3+1 scheme

Preference for  $\theta_{23}$  octant disappears in 3+1 scheme

Octant fragility seems to be a general feature...

# Octant of $\theta_{23}$ in danger with a sterile neutrino

Agarwalla, Chatterjee, A.P., arXiv: 1605.04299 (PRL 2017)

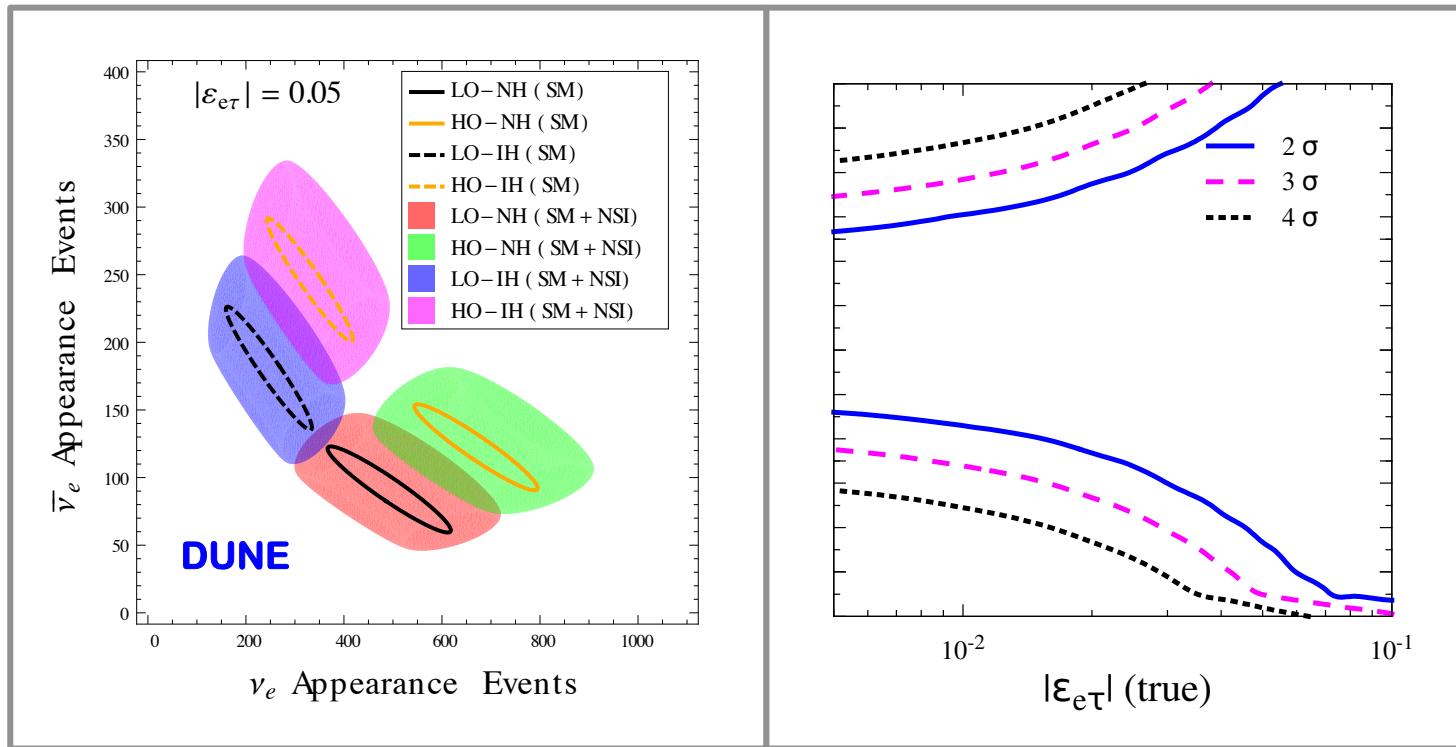


**Distinct ellipses (3ν) become overlapping blobs (3+1)**

**For unfavorable combinations of  $\delta_{13}$  &  $\delta_{14}$  sensitivity is lost**

# Striking analogy between steriles and NSIs

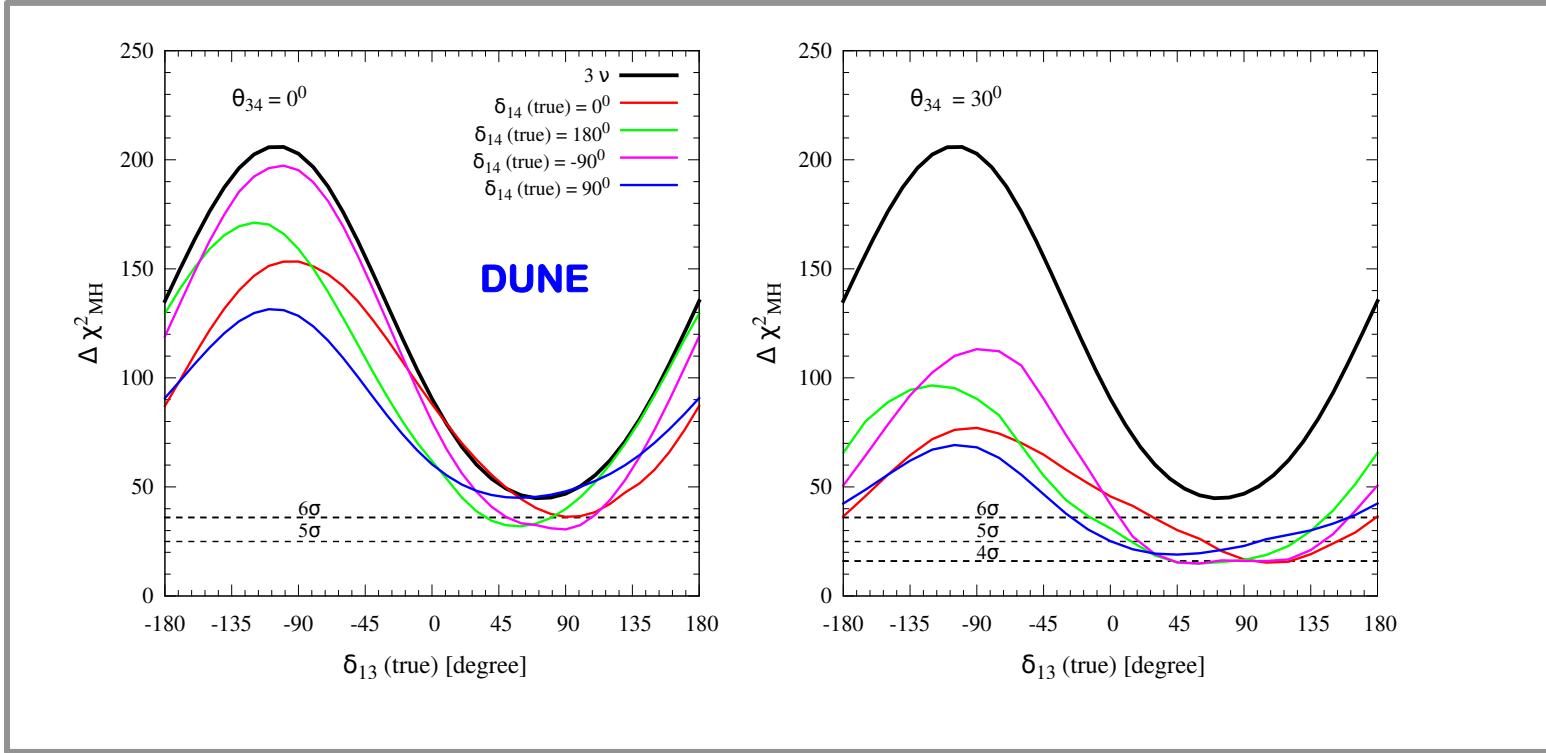
Agarwalla, Chatterjee, A.P., arXiv: 1607.01745 (PLB 2016)



Also in this case a new CP-phase introduces a degeneracy  
Very small values of the coupling may be harmful

# Discovery potential of mass hierarchy

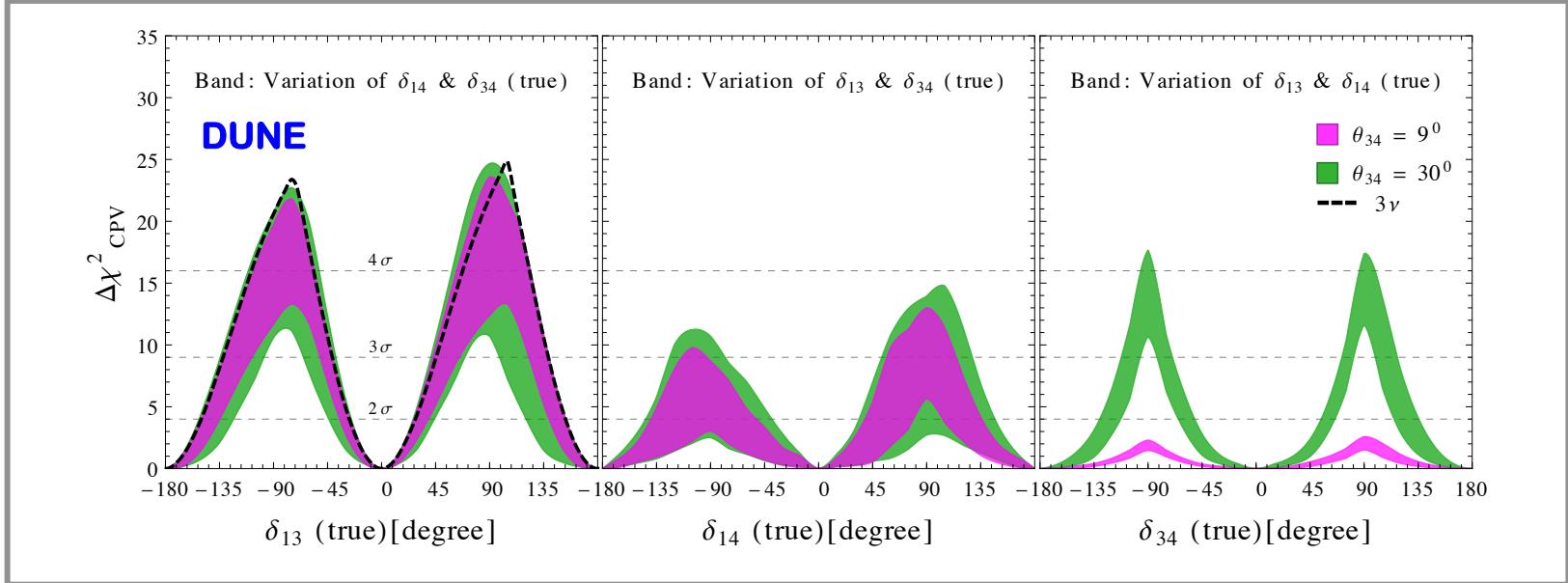
Agarwalla, Chatterjee, A.P., arXiv: 1603.03759 (JHEP 2016)



Degradation of sensitivity but  $4\sigma$  level preserved

# CPV discovery potential

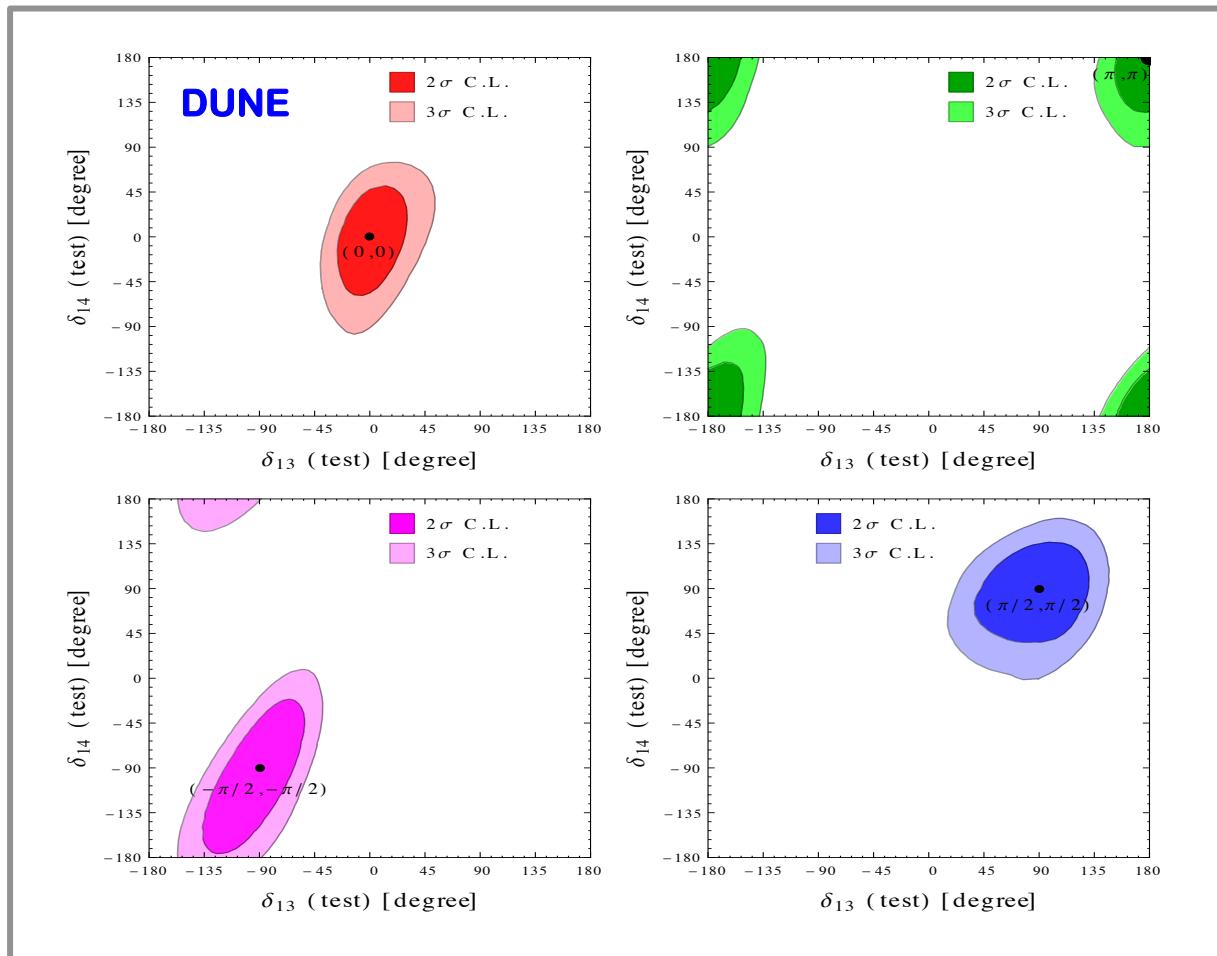
Agarwalla, Chatterjee, A.P., arXiv: 1603.03759 (JHEP 2016)



- Sensitivity to CPV induced by  $\delta_{13}$  reduced in 3+1 scheme
- Potential sensitivity also to the new CP-phases  $\delta_{14}$  e  $\delta_{34}$
- Clear hierarchy in the sensitivity:  $\delta_{13} > \delta_{14} > \delta_{34}$  for  $\theta_{14} = \theta_{24} = \theta_{34} = 9^\circ$

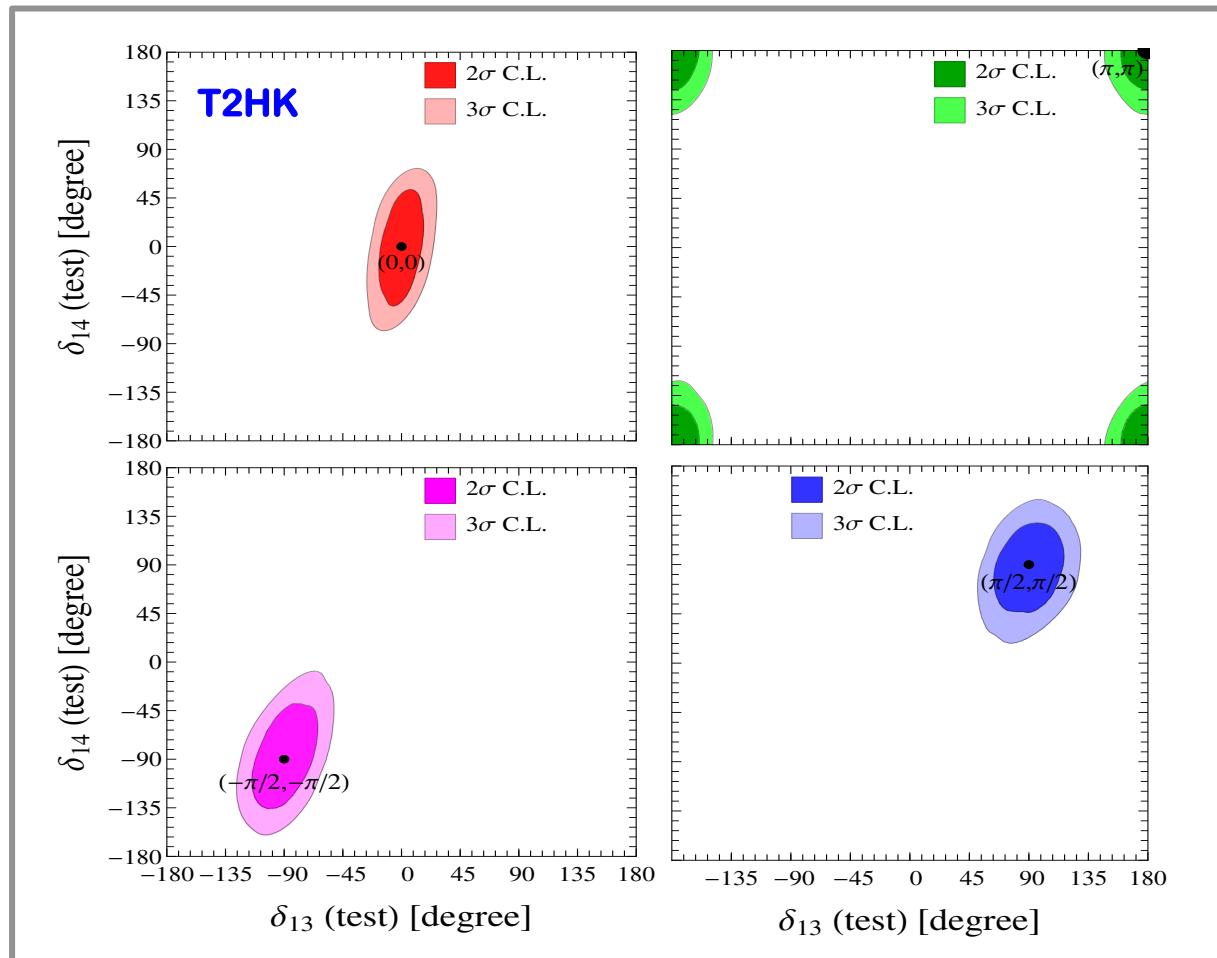
# We may be able to measure two CP phases

Agarwalla, Chatterjee, A.P., arXiv: 1603.03759 (JHEP 2016)



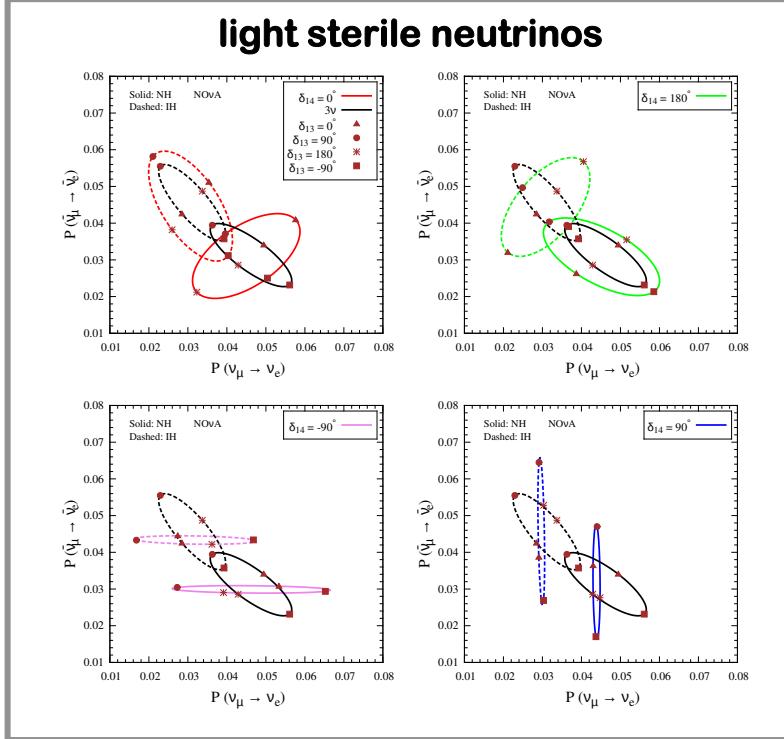
# Reconstruction of the CP phases in T2HK

Preliminary plot realized by S.S. Chatterjee

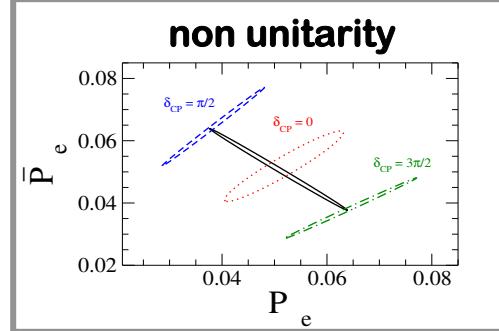


# The dance of the ellipses

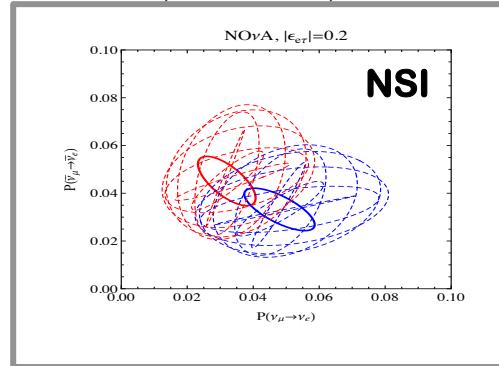
Agarwalla, Chatterjee, Dasgupta, A.P., 1601.05995



Miranda, Tortola, Valle, 1604:05690



Friedland, Shoemaker, 1207.6642



**Extensions of SM are often sources of extra CP-phases**  
**In all cases a new interference term appears in  $P_{\mu e}$  at LBL**  
**Bi-probability plots clearly represent this physical fact**

# Conclusions

- 3-flavor searches in evolution
- First indications about CPV and MO
- Intriguing hints of light sterile neutrinos
- New SBL experiments will shed light
- Full exploration of sterile vs possible with LBL only
- LBL program complementary to SBL one

# **Back up slides**

# CPV and averaged oscillations

$$A_{\alpha\beta}^{\text{CP}} \equiv P(\nu_\alpha \rightarrow \nu_\beta) - P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)$$

$$A_{\alpha\beta}^{\text{CP}} = -16 J_{\alpha\beta}^{12} \sin \Delta_{21} \underbrace{\sin \Delta_{13} \sin \Delta_{32}}$$

if  $\Delta \equiv \Delta_{13} \simeq \Delta_{23} \gg 1$  →  $\langle \sin^2 \Delta \rangle = 1/2$   
osc. averaged out by finite E resol.

It can be:

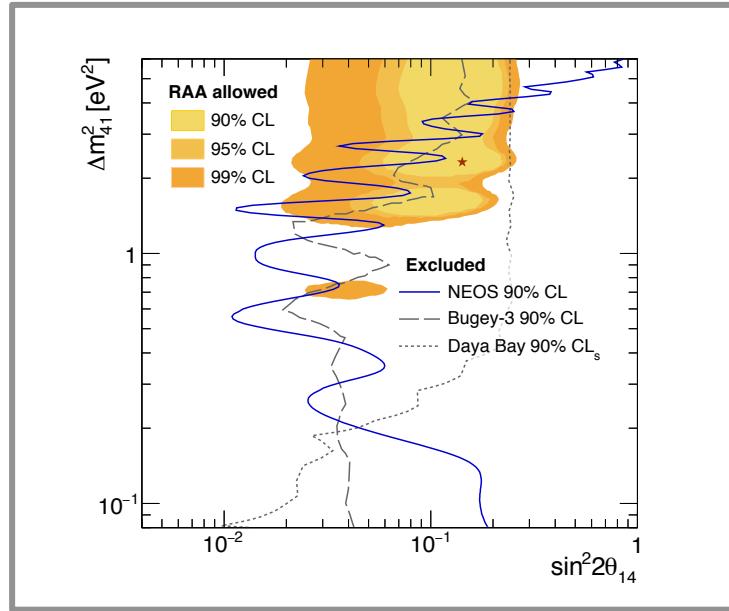
$$A_{\alpha\beta}^{\text{CP}} \neq 0$$

(if  $\sin \delta = 0$ )

The bottom line is that if one of the three  $\nu_i$  is  $\infty$  far from the other two ones this does not erase CPV  
(relevant for the  $4\nu$  case)

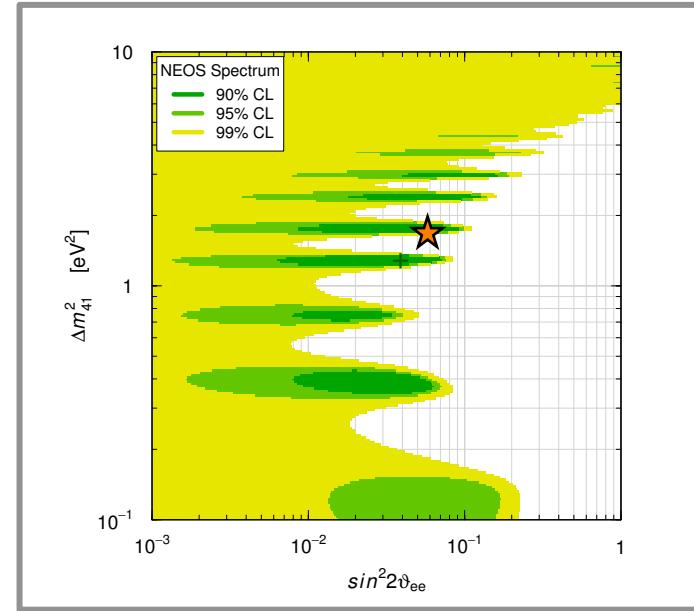
# Two different perspectives

negative view



NEOS, arXiv:1610:05134

positive view



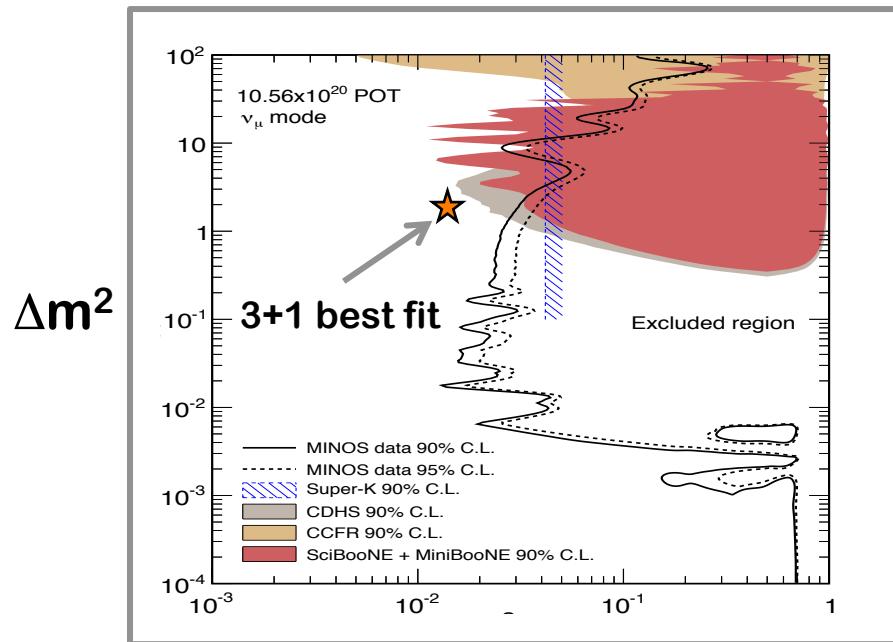
Gariazzo et al., arXiv: 1703.00860

**Best fit:  $\Delta m^2 = 1.73$  eV    $\sin^2 2\theta = 0.05$**

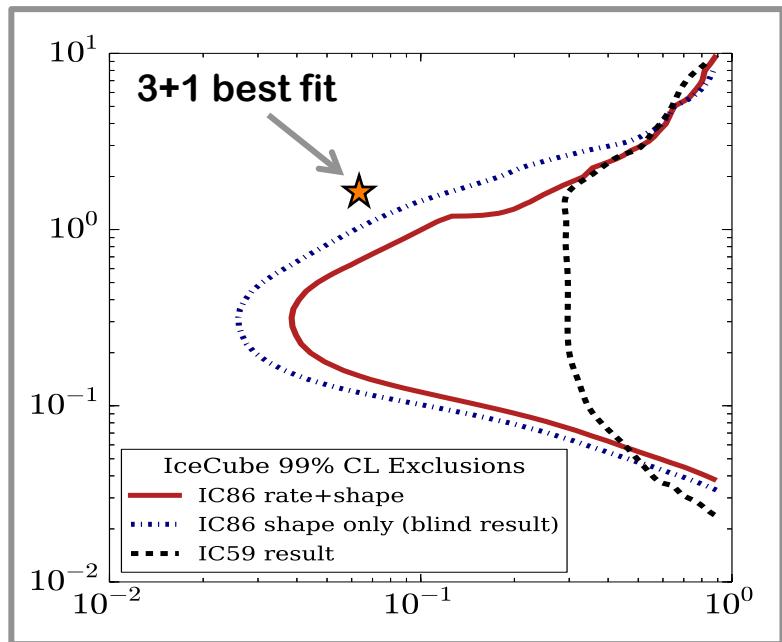
$\chi^2_{\text{no osc}} - \chi^2_{\min} = 6.5$    > 95% CL indication!

# No anomaly in $\nu_\mu$ disappearance

SBL & MINOS (NC)



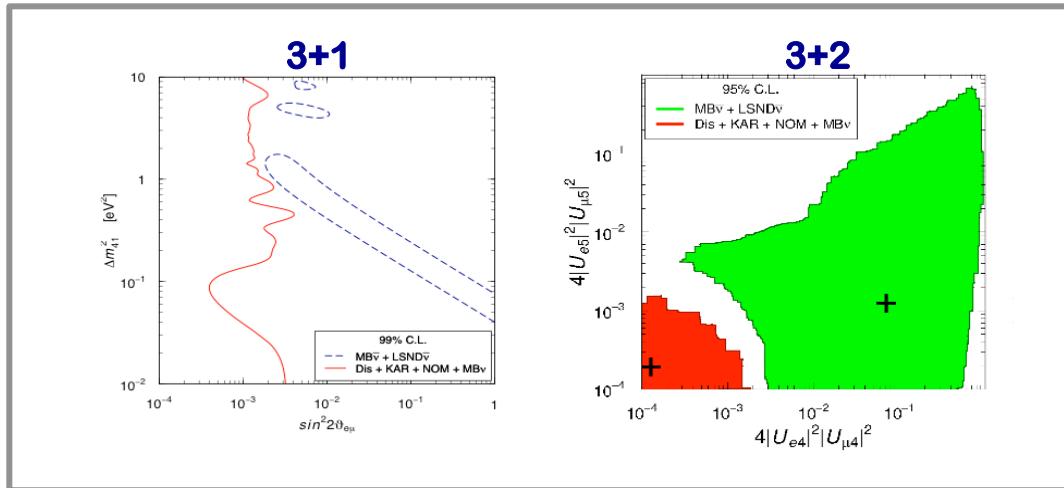
IceCube



$$\sin^2 \theta_{\mu\mu}$$

$$\sin^2 2\theta_{\mu\mu}$$

# Tension in all $\nu_s$ models



Giunti  
&  
Laveder

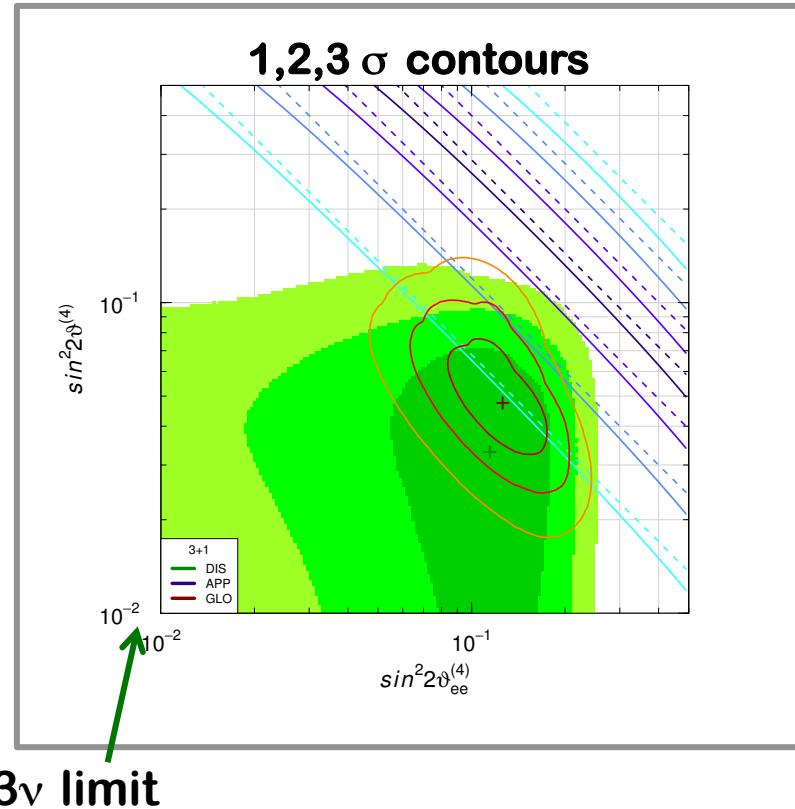
arXiv:1107.1452

$\nu_\mu \rightarrow \nu_e$  **positive**  
 $\nu_e \rightarrow \nu_e$  **positive**  
 $\nu_\mu \rightarrow \nu_\mu$  **negative**

$|U_{e4}| |U_{\mu 4}| > 0$   
 $|U_{e4}| > 0$   
 $|U_{\mu 4}| \sim 0$

$$\sin^2 2\theta_{e\mu} \simeq \frac{1}{4} \sin^2 2\theta_{ee} \sin^2 2\theta_{\mu\mu} \simeq 4|U_{e4}|^2|U_{\mu 4}|^2$$

# An “undecidable” problem



App. & Dis. barely overlap at  $2\sigma$  level

But their combination gives a  $6\sigma$  improvement with respect to the 3v case

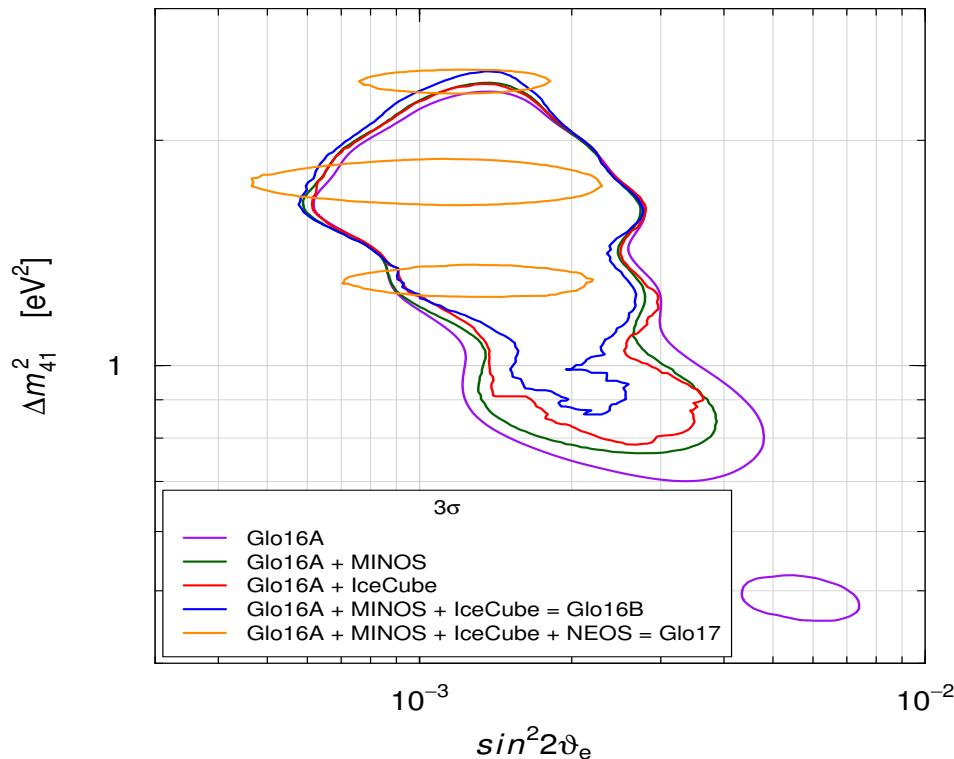
Difficult to take a decision on sterile vs !

Only new more sensitive experiments can decide

Figure from Giunti & Zavanin, arXiv:1508:03172  
(tension slightly increased after NEOS, MINOS, IceCube)

# Impact of the latest measurements

Gariazzo et al. arXiv:1703.00860



**NEOS selects a subregion of the region allowed by all the other data : very intriguing!**