NuFACT 2017 @Uppsala, Sweden

Beyond Standard Neutrino Theory





I am expected to talk about "Exotics"...

...What kind of monster should I talk about?

eV sterile neutrinos → Pallavicini,

Heavy neutrinos \rightarrow Wynne,

Complementarity w. other exps \rightarrow Antusch, Tang, Teixeira





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...What kind of monster should I talk about?

- eV sterile neutrinos → Pallavicini,
- Heavy neutrinos \rightarrow Wynne,
- Complementarity w. other exps → Antusch, Tang, Teixeira
- Let me try to focus on the following items...
 - Nonstandard neutrino interactions,
 - Non-unitarity PMNS matrix,
 - Secret neutrino interactions (nu-nu, nu-invisible)
 - * Materials are mainly taken from the papers 2015-

NP in $0\nu\beta\beta$, cosmological bounds to m_{ν} ...

Back:Raccoon? Tail:Snake?





Non-standard neutrino interactions



NSIs – NP parametrized with four-Fermi interactions

$$\mathbf{e.g.}, -\mathscr{L} = 2\sqrt{2}G_F \epsilon^m_{\alpha\beta} [\overline{\nu}_{\alpha} \gamma^{\rho} \mathbf{P}_L \nu_{\beta}] [\overline{e} \gamma_{\rho} \mathbf{P}_L e] + \text{H.c.} \quad a = 2\sqrt{2}G_F N_e E$$

$$\mathbf{\downarrow} \mathbf{\downarrow} \mathbf{\downarrow} \langle \nu_{\alpha} | H | \nu_{\beta} \rangle = \frac{1}{2E} \left[U_{\alpha i} \Delta m_{i1}^2 U_{i\beta}^{\dagger} + a \begin{pmatrix} 1 + \epsilon^m_{ee} & \epsilon^m_{e\mu} & \epsilon^m_{e\tau} \\ (\epsilon^m_{e\mu})^* & \epsilon^m_{\mu\mu} & \epsilon^m_{\mu\tau} \\ (\epsilon^m_{e\tau})^* & (\epsilon^m_{\mu\tau})^* & \epsilon^m_{\tau\tau} \end{pmatrix} \right]$$



NSIs – NP parametrized with four-Fermi interactions



NSIs – NP parametrized with four-Fermi interactions

Current bounds at 90%CL, Choubey et al., JHEP 12 (2015) 126

$$\begin{split} |\epsilon_{ee}^{m} - \epsilon_{\mu\mu}^{m}| < 4.2 \quad |\epsilon_{\tau\tau}^{m} - \epsilon_{\mu\mu}^{m}| < 0.05 \quad |\epsilon_{e\mu}^{m}| < 0.3 \quad |\epsilon_{e\tau}^{m}| < 3.0 \quad |\epsilon_{\mu\tau}^{m}| < 0.01 \\ |\epsilon_{\mu\epsilon}^{s}| < 0.026 \quad |\epsilon_{\mu\mu}^{s}| < 0.078 \quad |\epsilon_{\mu\tau}^{s}| < 0.013 \end{split}$$
* see also the global fit by Gonzalez-Garcia Maltoni, JHEP1309 (2013)152 $\begin{aligned} |\epsilon_{\mu\tau}^{m}| < 0.005 \\ |\epsilon_{\mu\tau}^{m}| < 0.005 \end{aligned}$ From IceCube high *E* atmos, New Salvado, et al., JHEP1701 (2017) 141



*

NSIs – NP parametrized with four-Fermi interactions

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see also the global fit by Gonzalez-Garcia Maltoni, JHEP1309 (2013)152
$$\begin{aligned} |\epsilon_{\mu\tau}^{m}| < 0.005 \\ |\epsilon_{\mu\tau}^{m}| < 0.005 \end{aligned}$$

It is not easy to realize the NSIs with their upper limits (\rightarrow we will see), but we should keep the possibilities phenomenologically allowed in mind

Non-standard neutrino interactions

Impact of NSIs on the oscillation probability for $\nu_{\mu} \rightarrow \nu_{e}$

×

YACHAY TECH



NSI parameters are varied in their allowed regions

Non-standard neutrino interactions

Impact of NSIs on the oscillation probability for $u_{\mu} \rightarrow
u_{e}$

×

YACHAY

Blennow et al., JHEP 1608 (2016) 090



NSI parameters are varied in their allowed regions



* Check the talk by Raut



* Check the talk by Raut

NSIs as noise

NSIs in the context of the parameter determination in future experiments



* Check the talk by Raut

NSIs as noise

NSIs in the context of the parameter determination in future experiments

NSIs as signals

High precision experiments may also be sensitive to New Physics



* Check the talk by Raut

NSIs as noise

NSIs in the context of the parameter determination in future experiments



* Degeneracies with NSIs at LBL experiments, see e.g., Liao et al., PRD93 (2016) 093016

NSI- δ_{CP}

Masud et al., J. Phys. G43 (2016) 095005 Masud Mehta, PRD94 (2016) 013014 Rout et al., PRD95 (2017) 075035 Miranda et al., PRL (2017) 117 061804

NSI-Mass Hierarchy (MH)

Masud Mehta, PRD94 (2016) 053007 Dutta et al., NPB920 (2017) 385 Deepthi et al., 1612.00784

NSI- θ_{23} octant

Agarwalla et al., PLB762 (2016) 64 Dutta et al., PRD 95 (2017) 095007 Das et al., 1708.05182 de Gouvea Kelly 1605.099376 Ge Smirnov JHEP 10 (2016) 138 Dutta Ghoshal JHEP 09 (2016) 110

> * source/detection NSI effects in MH determination at JUNO, Ohlsson et al. PLB728 (2014) 148



NSI-MH at DUNE (L = 1300 km)



With NSIs, osc. probs. with NH overlaps with those with IH.



NSI-MH at DUNE (L = 1300 km)



With NSIs, osc. probs. with NH overlaps with those with IH.



NSI- δ_{CP} at DUNE



NSIs confuses the determination of δ

– Although the fit is good, the best-fit point suggests the wrong δ



NSI- θ_{23} octant at DUNE



With NSIs, the ellipses of LO overlap with those of HO.



NSIs as noise

NSIs in the context of the parameter determination in future experiments

To reduce the noise...



Synergy between DUNE and T2HK (clean from matter related effects)





de Gouvea Kelly 1605.099376

The best fit of δ at DUNE can be greatly shifted by matter NSI effects.

* For standard oscillation fit at DUNE+T2HK, see also Fukasawa Yasuda NPB918 (2017) 337



Synergy between DUNE and T2HK (clean from matter related effects)



* For standard oscillation fit at DUNE+T2HK, see also Fukasawa Yasuda NPB918 (2017) 337



Go shorter baseline (than T2(H)K) with a good profile/intense beam



No disturbance from matter NSIs

Future beams: ESSnSB (conventional high intensity beam, 0.2-0.6GeV) MOMENT (mu DIF), DAEdALUS (mu DAR), NuSTORM (mu storage ring)...



Ask for help to non-oscillation experiments

e.g., Dark solar solution (LMA-D) vs COHERENT Akimov et al., 1708.01294 Miranda et al., JHEP 10 (2006) 008





Ask for help to non-oscillation experiments

e.g., Dark solar solution (LMA-D) vs COHERENT Akimov et al., 1708.01294 Miranda et al., JHEP 10 (2006) 008 Coloma et al., 1708.02899



*For sensitivity to NSIs at COHERENT, see also, Lindner et al., JHEP 1703 (2017) 097 Shoemaker, PRD95 (2017) 115028



Energy dependence - Wide band, More channels

$$P(\nu_{\mu} \rightarrow \nu_{e}) = 4s_{13}^{2}s_{23}^{2}\mathcal{F}_{1}^{2} + 4\left[\frac{\Delta m_{21}^{2}}{\Delta m_{31}^{2}}\right]^{2}s_{12}^{2}c_{12}^{2}c_{23}^{2}\left[\frac{\Delta m_{31}^{2}}{a}\mathcal{F}_{2}\right]^{2} \quad \mathcal{F}_{1} \equiv \frac{\sin\frac{[\Delta m_{31}^{2} - a]L}{4E}}{1 - a/\Delta m_{31}^{2}} \\ + 8\left[\frac{\Delta m_{21}^{2}}{\Delta m_{31}^{2}}\right]s_{12}c_{12}s_{23}c_{23}s_{13}c_{\delta}\left[\frac{\Delta m_{31}^{2}}{a}\mathcal{F}_{1}\mathcal{F}_{2}\cos\frac{\Delta m_{31}^{2}L}{4E}\right] \quad \mathcal{F}_{2} \equiv \sin\frac{aL}{4E} \\ \text{Standard} \\ \text{Osc.} \qquad -8\left[\frac{\Delta m_{21}^{2}}{\Delta m_{31}^{2}}\right]s_{12}c_{12}s_{23}c_{23}s_{13}s_{\delta}\left[\frac{\Delta m_{31}^{2}}{a}\mathcal{F}_{1}\mathcal{F}_{2}\sin\frac{\Delta m_{31}^{2}L}{4E}\right] \\ \text{NSI} \\ + 8s_{23}c_{23}s_{13}\left[|\epsilon_{e\mu}^{m}|c_{23}c_{\delta+\phi_{e\mu}^{m}} - |\epsilon_{e\tau}^{m}|s_{23}c_{\delta+\phi_{e\tau}^{m}}\right]\left[\mathcal{F}_{1}\mathcal{F}_{2}\cos\frac{\Delta m_{31}^{2}L}{4E}\right] \\ - 8s_{23}c_{23}s_{13}\left[|\epsilon_{e\mu}^{m}|s_{23}c_{\delta+\phi_{e\mu}^{m}} - |\epsilon_{e\tau}^{m}|s_{23}s_{\delta+\phi_{e\tau}^{m}}\right]\left[\mathcal{F}_{1}\mathcal{F}_{2}\sin\frac{\Delta m_{31}^{2}L}{4E}\right] \\ + 8s_{23}^{2}s_{13}\left[|\epsilon_{e\mu}^{m}|s_{23}c_{\delta+\phi_{e\mu}^{m}} + |\epsilon_{e\tau}^{m}|c_{23}c_{\delta+\phi_{e\tau}^{m}}\right]\left[\frac{a}{\Delta m_{31}^{2}}\mathcal{F}_{1}^{2}\right] \\ + \mathcal{O}(\Delta m_{21}^{2}\epsilon) \end{aligned}$$



Energy dependence - Wide band, More channels

$$\begin{split} P(\nu_{\mu} \rightarrow \nu_{e}) &= 4s_{13}^{2}s_{23}^{2}\mathcal{F}_{1}^{2} + 4\left[\frac{\Delta m_{21}^{2}}{\Delta m_{31}^{2}}\right]^{2}s_{12}^{2}c_{12}^{2}c_{23}^{2}\left[\frac{\Delta m_{31}^{2}}{a}\mathcal{F}_{2}\right]^{2} \quad \mathcal{F}_{1} \equiv \frac{\sin\frac{|\Delta m_{31}^{2} - a|L}{4E}}{1 - a/\Delta m_{31}^{2}} \quad 1/E^{2} \\ &+ 8\left[\frac{\Delta m_{21}^{2}}{\Delta m_{31}^{2}}\right]s_{12}c_{12}s_{23}c_{23}s_{13}c_{\delta}\left[\frac{\Delta m_{31}^{2}}{a}\mathcal{F}_{1}\mathcal{F}_{2}\cos\frac{\Delta m_{31}^{2}L}{4E}\right] \quad \mathcal{F}_{2} \equiv \sin\frac{aL}{4E} \quad 1/E^{2} \\ \\ &\text{Standard} \\ &\text{Osc.} \qquad -8\left[\frac{\Delta m_{21}^{2}}{\Delta m_{31}^{2}}\right]s_{12}c_{12}s_{23}c_{23}s_{13}s_{\delta}\left[\frac{\Delta m_{31}^{2}}{a}\mathcal{F}_{1}\mathcal{F}_{2}\sin\frac{\Delta m_{31}^{2}L}{4E}\right] \qquad 1/E^{3} \\ &\text{NSI} \qquad +8s_{23}c_{23}s_{13}\left[|\epsilon_{e\mu}^{m}|c_{23}c_{\delta+\phi_{e\mu}^{m}} - |\epsilon_{e\tau}^{m}|s_{23}c_{\delta+\phi_{e\tau}^{m}}\right]\left[\mathcal{F}_{1}\mathcal{F}_{2}\cos\frac{\Delta m_{31}^{2}L}{4E}\right] \qquad 1/E^{3} \\ &-8s_{23}c_{23}s_{13}\left[|\epsilon_{e\mu}^{m}|c_{23}s_{\delta+\phi_{e\mu}^{m}} - |\epsilon_{e\tau}^{m}|s_{23}s_{\delta+\phi_{e\tau}^{m}}\right]\left[\mathcal{F}_{1}\mathcal{F}_{2}\sin\frac{\Delta m_{31}^{2}L}{4E}\right] \qquad 1/E^{2} \\ &+8s_{23}^{2}s_{13}\left[|\epsilon_{e\mu}^{m}|s_{23}c_{\delta+\phi_{e\mu}^{m}} + |\epsilon_{e\tau}^{m}|c_{23}c_{\delta+\phi_{e\tau}^{m}}\right]\left[\frac{a}{\Delta m_{31}^{2}}\mathcal{F}_{1}^{2}\right] \qquad 1/E^{2} \\ &+0(\Delta m_{21}^{2}\epsilon) \qquad \text{In high energy limit} \end{split}$$



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NSIs as signals

High precision experiments may also be sensitive to New Physics



Sensitivities to NSIs at the forthcoming experiments.

DUNE

Blennow et al., JHEP 08 (2016) 090 Coloma, JHEP 03 (2016) 016 de Gouvea Kelly, NPB908 (2016) 318 Liao et al., JHEP 01 (2017) 071

T2HK

Fukasawa et al., PRD95 (2017) 055005 Kelly, PRD95 (2017) 115009 Liao et al., JHEP 01 (2017) 071

* source/detection NSIs at ESSvSB Blennow et al., JHEP 1412 (2014) 120

Atmospheric neutrinos

at IceCube

Salvado et al., JHEP 01 (2017) 141 Mocioiu Wright, NPB893 (2015) 376 Choubey Ohlsson PLB739 (2014) 357 Esmaili Smirnov, JHEP 06 (2013) 026 Ohlsson et al., PRD88 (2013) 013001

SK official

set the bounds i Mitsuka et al., PRD84 (2011) 113008

Cosmic neutrinos at IceCube

Rasmussen et al., 1707.07684 Gonzalez-Garcia et al., Astropart Phys. 84 (2016) 15 Bustamante et al., PRL 115 (2015) 161302 Shoemaker Murase PRD 93 (2016) 085004

Cosmology

Archidiacono Hannestad, JCAP 1407 (2014) 046

* source/detection NSIs at MOMENT Tang Zhang, 1705.09500

at HK

Kelly, PRD95 (2017) 115009 Fukasawa Yasuda, NPB914 (2017) 99

at KM3NeT

Coelho 1702.04508

at INO

real data

Choubey et al., JHEP 12 (2015) 126



Sensitivities to NSIs at DUNE + T2HK

Synergy between DUNE + T2HK

Degeneracies in $\tilde{\epsilon}^m_{\mu\mu}$ at DUNE is solved with T2HK

Inclusion of the priors improves the sensitivity to $\epsilon^m_{e\tau}$ (solve the degeneracy with $\tilde{\epsilon}^m_{ee}$)

Determinations of the standard osc. parameters are also important

Typical sensitivities ~0.1-0.05

Sensitivities to matter NSIs at NuFACT ~ O(0.001)



0.4

 $\epsilon^m_{e au}$

0.6

0.8

Credible Intervals at 90%

0.2

DUNE

T2HK

0.0

T2HK+DUNE



Large NSIs in theory

* Check the talk by Rius

How to get large NSIs?

$$|\epsilon| \sim \mathcal{O}(1) - \mathcal{O}(10^{-2})$$

Currently allowed \rightarrow Sensitivity reach at the forthcoming experiments



O(1) NSIs are currently allowed and phenomenologically motivated by...

Weak tension between...



see also Fukasawa et al., 1609.04204, Ghosh Yasuda 1709.08264

To test the robustness of the standard oscillation fits

– e.g., Dark solar solution –

Miranda et al., JHEP 10 (2006) 008 Maltoni Smirnov, EPJ A52 (2016) 87 Coloma et al., JHEP 04 (2017) 116

$$\epsilon_{\mu\mu}^{\odot} \sim 2$$
$$s_{12}^2 \sim 0.7$$

vs COHERENT

Rate: Coloma et al., 1708.02899 Shape: Liao Marfatia, 1708.04255

We should not exclude the possibilities allowed phenomenologically...



It is not easy to accommodate with such a large NSI in a model...

Naive expectation...

$$\epsilon = \frac{g_{\rm NSI}^2}{2\sqrt{2}G_F\Lambda^2} = 3 \cdot 10^{-2} \left[\frac{g_{\rm NSI}}{1.0}\right]^2 \left[\frac{1.0[{\rm TeV}]}{\Lambda}\right]^2$$

e.g.,
$$\nu$$
 $g_{\rm NSI}$ ν
 $f_{g_{\rm NSI}}$ f

...suggests New Physics (Leptoquarks, Z' etc.) at LHC.



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...suggests New Physics (Leptoquarks, Z' etc.) at LHC.

e.g., ν $g_{\rm NSI}$ ν f $g_{\rm NSI}$ f

NSIs appears with charged lepton SU(2) counter processes.

$$\mathscr{L} = 2\sqrt{2}G_F\epsilon \left[\overline{L}\gamma^{\rho}L\right] \left[\overline{f}\gamma_{\rho}f\right] = 2\sqrt{2}G_F\epsilon \left[\overline{\nu}\gamma^{\rho}P_L\nu + \frac{\overline{\ell}\gamma^{\rho}P_L\ell}{\overline{\ell}\gamma^{\rho}P_L\ell}\right] \left[\overline{f}\gamma_{\rho}f\right]$$

 $f_{g_{\rm NSI}} = f_{g_{\rm NSI}$



 $+(2\sqrt{2}G_F)^2\epsilon(\overline{\ell}\ell\overline{f}fH^+H^-)+\cdots$

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 $\begin{array}{ccc} g_{\mathrm{NSI}} & L & \mathrm{Bound\ from\ counter\ processes} & \mathrm{Grossman,\ PLB359\ (1995)\ 141} \\ & & \\ & & \\ g_{\mathrm{NSI}} & f & \epsilon \lesssim \mathcal{O}(10^{-3}) \end{array} \\ \begin{array}{c} & & \\ & & & \\ & & \\ & & & \\ & & & \\ & & \\ & &$

To avoid the counter, use of d=8 operators with Higgs fields. e.g.,

$$\mathscr{L} = (2\sqrt{2}G_F)^2 \epsilon \left[\overline{L}i\tau^2 H^* \gamma^{\rho} H^{\mathsf{T}}i\tau^2 L\right] \left[\overline{f}\gamma_{\rho}f\right] = 2\sqrt{2}G_F \epsilon \left[\overline{\nu}\gamma^{\rho}\mathcal{P}_L\nu\right] \left[\overline{f}\gamma_{\rho}f\right]$$

Berezhiani Rossi, PLB535 (2002) 207 Davidson et al., JHEP 03 (2003) 011



Tree-level decompositions of d=8 ops are accompanied by...

d=6 ops of NSIs + counter processes

Antusch et al., NPB810 (2009) 369 Gavela et al., PRD79 (2009) 013007











Tree-level decompositions of d=8 ops are accompanied by...

d=6 ops of NSIs + counter processes

d=6 ops of the non-Unitarity (MUV)

Antusch et al., NPB810 (2009) 369 Gavela et al., PRD79 (2009) 013007

→ d=6 NSI/non-Uni models

At the loop level...

They are quadratical divergent.

Biggio et al., JHEP 03 (2009) 139 Biggio et al., JHEP 08 (2009) 090





Tree-level decompositions of d=8 ops are accompanied by...

d=6 ops of NSIs + counter processes

d=6 ops of the non-Unitarity (MUV)

Antusch et al., NPB810 (2009) 369 Gavela et al., PRD79 (2009) 013007

→ d=6 NSI/non-Uni models

At the loop level...

They are quadratical divergent.

Biggio et al., JHEP 03 (2009) 139 Biggio et al., JHEP 08 (2009) 090

To cancel/regularize them, d=6 ops (counter terms) are necessary.

→ d=6 NSI models

It may be possible, but cancellations/fine-tunings are necessary

"Pure NSIs from d=8" require the dedicated construction at the d=6 level.

- A new trend
 - → NSIs mediated by a light mediator



NSIs mediated by light fields

Forward scattering \rightarrow mediator is not necessarily heavier than EW

$$\epsilon = \frac{g_{\rm NSI}^2}{2\sqrt{2}G_F\Lambda^2} = 3 \cdot 10^{-2} \left[\frac{g_{\rm NSI}}{10^{-5}}\right]^2 \left[\frac{10[{\rm MeV}]}{\Lambda}\right]^2$$

→ Faint interactions mediated by a MeV mediator

GeV right-hand nus + New U(1) with MeV scale breaking \rightarrow O(1) NSI

$$\begin{aligned} \mathscr{L} &= y\overline{L}i\tau^{2}H'^{*}P_{R}\Psi + M_{\Psi}\overline{\Psi}\Psi \\ \blacktriangleright \mathscr{L}_{NSI} &= \frac{g_{f}g_{\Psi}\kappa_{\alpha}^{*}\kappa_{\beta}}{M_{Z'}^{2}} [\overline{\nu}_{\alpha}\gamma^{\rho}P_{L}\nu_{\beta}][\overline{f}\gamma_{\rho}f] \\ &\equiv 2\sqrt{2}G_{F}\epsilon_{\alpha\beta} \end{aligned}$$

$$\begin{aligned} M_{Z'} &\simeq 10[\text{MeV}] \quad M_{\Psi} \simeq 1[\text{GeV}] \\ g_{q} &\sim 10^{-4} \\ g_{\Psi} &\sim 0.05 \\ y &\sim 1 \end{aligned}$$

$$\begin{aligned} \min_{\kappa_{e}} &\simeq y_{e}^{*}\langle H'\rangle/M_{\Psi} \\ \langle H'\rangle &= M_{Z'}/(\sqrt{2}g_{\Psi}) \end{aligned}$$

$$\epsilon_{ee}^{m} \sim 1 \end{aligned}$$

$$\begin{aligned} \varepsilon_{ee}^{m} \sim 1 \end{aligned}$$

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$$\begin{aligned} \varepsilon_{ee}^{m} \sim 1 \end{aligned}$$

$$\begin{aligned} \omega_{ee}^{m} \sim 1 \end{aligned}$$

$$\begin{aligned} \omega_{ee}^{m} \sim 1 \end{aligned}$$

MeV mediator is a trend \rightarrow Cosmic Nu, muon g-2, LUV in B-phys. etc.



Non-unitary PMNS matrix

Unitarity violation

Violation of the conservation of

probability and energy





Unitarity is violated in effective theories in general. For example,...

$\begin{array}{|c|c|c|c|c|c|c|c|} \hline \text{Mix with light sterile neutrinos} & \rightarrow \text{Talk by Pallavicini, Ko, Aurisano, Blake, Ghosh, Vanegas Forero} \\ \hline \text{Mix with light sterile neutrinos} & & & & \\ \hline \text{Ghosh, Vanegas Forero} \\ \hline \text{Ghosh, Vanegas Forero} \\ \hline \text{Holdson } P(\nu_{\alpha} \rightarrow \nu_{\beta}) = \delta_{\alpha\beta} - 4\sum_{i < j}^{N} \text{Re} \left[U_{\beta i} U_{\alpha i}^{*} U_{\beta j}^{*} U_{\alpha j} \right] \sin^{2} \frac{\Delta m_{ji}^{2} L}{4E} \\ \hline \text{Extra osc. driven} \\ \text{by } \Delta m_{41}^{2} \text{ etc.} & + 2\sum_{i < j}^{N} \text{Im} \left[U_{\beta i} U_{\alpha i}^{*} U_{\beta j}^{*} U_{\alpha j} \right] \sin \frac{\Delta m_{ji}^{2} L}{2E} \\ \hline \end{array}$

Mix with heavy neutral fields = "Minimal Unitarity Violation"

see e.g., Antusch et al., JHEP10 (2006) 84 $\langle \nu_4 | \nu_{\alpha} \rangle \neq 0 \quad | \nu_4 \rangle$ Too heavy to participate in the propagation non-unitary

$$P(\nu_{\alpha} \to \nu_{\beta}) = \left| \sum_{i,j=1}^{3} \langle \nu_{\beta} | \nu_{j} \rangle \langle \nu_{j} | \mathrm{e}^{-\mathrm{i}HL} | \nu_{i} \rangle \langle \nu_{i} | \nu_{\alpha} \rangle \right|^{2} = \left| \sum_{i=1}^{3} N_{\beta i} \mathrm{e}^{-\mathrm{i}\frac{\Delta m_{i1}^{2}L}{2E}} N_{i\alpha}^{\dagger} \right|^{2}$$

* One must be further careful about the normalization factor, cf., Langacker London, PRD38 (1988) 907

Neutrino decaySee e.g., Berryman et al., PLB742 (2015) 74Non-hermitian Hamiltonian
 $\langle \nu_i | H_{\text{vac}} | \nu_i \rangle = \frac{m_i^2}{2E} - i\frac{\Gamma_i}{2}$ Coloma Peres, 1705.03599 Choubey et al., 1705.05820 $\langle \nu_i | H_{\text{vac}} | \nu_i \rangle = \frac{m_i^2}{2E} - i\frac{\Gamma_i}{2}$ $|\nu_{\alpha}\rangle = \sum_{i=1}^{3} |\nu_i\rangle\langle\nu_i | \nu_{\alpha}\rangle = \sum_{i=1}^{3} |\nu_i\rangle N_{i\alpha}^{\dagger}$

Non-unitary PMNS matrix

Fitting the PMNS to oscillation experiments without assuming unitarity

×

YACHAY TECH





Current bounds in MUV (Mix with heavy neutrals)

Fernandez-Martinez et al., JHEP 03 (2016) 033

Observable	SM prediction	Experimental value	
$M_W \simeq M_W^{SM} (1 + 0.20 (\eta_{ee} + \eta_{\mu\mu}))$	$(80.363 \pm 0.006)~{\rm GeV}$	$(80.385\pm 0.015)~{\rm GeV}$	
$s_{\mathrm{W~eff}}^{2 \text{ lep}} \simeq s_{\mathrm{W~eff}}^{2 \text{ lep} SM} \left(1 - 1.30 \left(\eta_{ee} + \eta_{\mu\mu}\right)\right)$	0.23152 ± 0.00010	0.23113 ± 0.00021	
$s_{\mathrm{W~eff}}^{2\mathrm{had}} \simeq s_{\mathrm{W~eff}}^{2\mathrm{had}}$ SM $(1 - 1.30 \left(\eta_{\mathrm{ee}} + \eta_{\mu\mu}\right))$	0.23152 ± 0.00010	0.23222 ± 0.00027	
$R_l \simeq R_l^{\rm SM} \left(1 + 0.18 \left(\eta_{ee} + \eta_{\mu\mu}\right)\right)$	20.740 ± 0.010	20.804 ± 0.050	
$R_{e}\simeq R_{e}^{\rm SM}\left(1+0.11\left(\eta_{\rm ee}+\eta_{\mu\mu}\right)\right)$	0.17226 ± 0.00003	0.1721 ± 0.0030	
$R_b \simeq R_b^{\rm SM} \left(1 - 0.06 \left(\eta_{ee} + \eta_{\mu\mu} \right) \right)$	0.21576 ± 0.00003	0.21629 ± 0.00066	
$\sigma_{\text{had}}^0 \simeq \sigma_{\text{had}}^{0 \text{ SM}} \left(1 + 0.55 \left(\eta_{\text{ee}} + \eta_{\mu\mu}\right) + 0.53 \eta_{\tau\tau}\right)$	$(41.479 \pm 0.008)~\rm{nb}$	(41.541 ± 0.037) nb	
$\Gamma_{\rm inv}\simeq\Gamma_{\rm inv}^{\rm SM}\left(1-0.33\left(\eta_{\rm ee}+\eta_{\mu\mu}\right)-1.32\eta_{\tau\tau}\right)$	(0.50166 ± 0.00005) GeV	(0.4990 ± 0.0015) GeV	
$R^{\pi}_{\mu e} \simeq (1 - (\eta_{\mu\mu} - \eta_{ee}))$	1	1.0042 ± 0.0022	
$R^{\pi}_{\tau\mu} \simeq (1 - (\eta_{\tau\tau} - \eta_{\mu\mu}))$	1	0.9941 ± 0.0059	
$R_{\mu e}^W \simeq (1 - (\eta_{\mu\mu} - \eta_{ee}))$	1	0.992 ± 0.020	
$R^W_{\tau\mu} \simeq (1 - (\eta_{\tau\tau} - \eta_{\mu\mu}))$	1	1.071 ± 0.025	
$R_{\mu e}^{K} \simeq (1 - (\eta_{\mu\mu} - \eta_{ee}))$	1	0.9956 ± 0.0040	
$R^K_{\tau\mu} \simeq (1 - (\eta_{\tau\tau} - \eta_{\mu\mu}))$	1	0.978 ± 0.014	
$R^l_{\mu e} \simeq (1 - (\eta_{\mu\mu} - \eta_{ee}))$	1	1.0040 ± 0.0032	
$R^l_{\tau\mu} \simeq (1 - (\eta_{\tau\tau} - \eta_{\mu\mu}))$	1	1.0029 ± 0.0029	
$V_{ud}^{\beta} \simeq \sqrt{1 - V_{us} ^2}(1 + \eta_{\mu\mu})$	$\sqrt{1- V_{us} ^2}$	0.97417 ± 0.00021	
$\left V_{us}^{\tau \rightarrow K \nu \tau}\right \simeq \left V_{us}\right \left(1 + \eta_{ee} + \eta_{\mu\mu} - \eta_{\tau\tau}\right)$	$ V_{us} $	0.2212 ± 0.0020	
$\left V_{us}^{\tau \to K,\pi}\right \simeq \left V_{us}\right (1 + \eta_{\mu\mu})$	$ V_{us} $	0.2232 ± 0.0019	
$\left V_{us}^{K_L \to \pi e \overline{\nu}_s}\right \simeq \left V_{us}\right (1 + \eta_{\mu\mu})$	$ V_{us} $	0.2237 ± 0.0011	
$\left V_{us}^{K_L \to \pi \mu \overline{\nu}_{\mu}}\right \simeq \left V_{us}\right (1 + \eta_{ee})$	$ V_{us} $	0.2240 ± 0.0011	
$\left V_{us}^{K_S \to \pi e \overline{\nu}_s} \right \simeq \left V_{us} \right \left(1 + \eta_{\mu\mu} \right)$	$ V_{us} $	0.2229 ± 0.0016	
$\left V_{us}^{K\pm \to \pi e \nabla_s}\right \simeq \left V_{us}\right (1 + \eta_{\mu\mu})$	$ V_{us} $	0.2247 ± 0.0012	
$\left V_{us}^{K \pm \to \pi \mu \overline{\nu}_{\mu}} \right \simeq \left V_{us} \right (1 + \eta_{ee})$	$ V_{us} $	0.2245 ± 0.0014	
$\left V_{us}^{K,\pi \to \mu \nu}\right \simeq \left V_{us}\right \left(1 + \eta_{\mu \mu}\right)$	$ V_{us} $	0.2315 ± 0.0010	

See also, Antusch Fischer, JHEP 10 (2014) 094 Escrihuela et al., 1612.07377 Blennow et al., JHEP 04 (2017) 153

The PMNS matrix *N* is parametrized as

$$N_{\alpha i} \equiv \left[\delta_{\alpha\beta} - \eta_{\alpha\beta}\right] \mathcal{U}_{\beta i}$$

3*3 unitary matrix

Deviation from unitarity is parametrized with a 3*3 hermitian matrix

* Unitarity condition of the full mixing matrix

$$U = \begin{pmatrix} N_{3\times3} & \Theta \\ R & S \end{pmatrix} \xrightarrow{UU^{\dagger} = 1} \eta = \frac{1}{2} \Theta \Theta^{\dagger}$$

* Parametrization with a 3*3 lower triangular matrix Escrihuela et al., PRD92 (2015) 053009 Blennow et al., JHEP 04 (2017) 153

 $\eta_{\alpha\beta}$ in non-oscillation observables



Non-unitary PMNS matrix

Current bounds in MUV (Mix with heavy neutrals)

		G-SS	
		LFC	m LFV
$\sqrt{2\eta_{ee}}, \theta_e $	1σ	$0.031\substack{+0.010\\-0.020}$	_
	2σ	< 0.050	_
$\sqrt{2\eta_{\mu\mu}}, \theta_{\mu} $	1σ	< 0.011	_
	2σ	< 0.021	_
$\sqrt{2\eta_{\tau\tau}}, \theta_{\mu} $	1σ	$0.044\substack{+0.019\\-0.027}$	_
	2σ	< 0.075	—
$\sqrt{2\eta_{e\mu}}, \sqrt{ \theta_e\theta_\mu }$	1σ	< 0.018	$< 4.1\cdot 10^{-3}$
	2σ	< 0.026	$<4.9\cdot10^{-3}$
$\sqrt{2\eta_{e\tau}}, \sqrt{ \theta_e \theta_\tau }$	1σ	< 0.045	< 0.107
	2σ	< 0.052	< 0.127
$\sqrt{2\eta_{\mu\tau}}, \sqrt{ \theta_{\mu}\theta_{\tau} }$	1σ	< 0.024	< 0.115
	2σ	< 0.035	< 0.137



The PMNS matrix *N* is parametrized as

$$N_{\alpha i} \equiv \left[\delta_{\alpha\beta} - \eta_{\alpha\beta}\right] \mathcal{U}_{\beta i}$$

3^{*}3 unitary matrix

Deviation from unitarity is parametrized with a 3*3 hermitian matrix

Current bounds $\eta < \mathcal{O}(10^{-3})$

We can constrain the deviation from unitarity, but...

Can we "test" the unitarity in oscillations? – In principle, Yes.



Sato, hep-ph/0008056, proc. of NuFACT00 Unitarity check in $\nu_{\mu} \rightarrow \nu_{e}$ Paes Sicking, PRD95 (2017) 075004 Oscillation probability at $(\Delta m_{21}^2)^2$, $\Delta m_{21}^2 |U_{e3}|$, $|U_{e3}|^2$, $P_{\nu_{\mu} \to \nu_{e}} = 4|U_{\mu3}U_{e3}^{*}|^{2} \frac{\Delta m_{31}^{2}L}{4E} \qquad \begin{array}{c} \text{Different } E \text{ dependences} \\ \text{They can be separated, in principle} \\ +4\text{Re} \left[U_{\mu2}U_{e2}^{*}U_{\mu3}^{*}U_{e3} \right] \left[\frac{\Delta m_{21}^{2}L}{4E} \right] \sin \frac{\Delta m_{31}^{2}L}{2E} \end{array}$ $-8\mathrm{Im}\left[U_{\mu 2}U_{e 2}^{*}U_{\mu 3}^{*}U_{e 3}\right]\left[\frac{\Delta m_{21}^{2}L}{4E}\right]\sin^{2}\frac{\Delta m_{31}^{2}L}{4E}$ $+4\left|U_{\mu 2}U_{e 2}^{*}\right|^{2}\left[\frac{\Delta m_{21}^{2}L}{4E}\right]^{2}+\mathcal{O}\left[(\Delta m_{21}^{2})^{2}|U_{e 3}|\right]$





If U is unitary, we can determine a triangle only with A, B, and D





If U is unitary, we can determine a triangle only with A, B, and D
 Jarlskog, PRL55 (1985) 1039,
 C is Jarlskog's invariant = Area of the triangle
 PRD36 (1987) 2127

Unitarity of U is tested by checking...

Area of the triangle suggested by A, B, and D $\stackrel{?}{=}$ C/2





Interactions between neutrinos and invisibles (incl. neutrinos)





Sterile matter effect to avoid the bound from $N_{
m eff}$

Chu et al., JCAP 1510 (2015) 011 Cherry et al., 1605.06506

MSW effect with thermal potential mediated by a new gauge boson with a mass around MeV

$$\sin^2 2\tilde{\theta}_{\text{a-s}} = \frac{\sin 2\theta_{\text{a-s}}}{(\cos 2\theta_{\text{a-s}} + \frac{2E}{\Delta m^2}V_{\text{eff}})^2 + \sin^2 2\theta_{\text{a-s}}}$$



Sterile decouples before/during BBN, if $V_{
m eff}\gg rac{\Delta m^2}{2E}$

Neutrino annihilation to avoid cosmological bound on $\sum m_{\nu}$

Farzan Hannestad, JCAP 1602 (2016) 058

Dark matter effect with sterile neutrino

Capozzi et al., JCAP 1707 (2017) 021

Fuzzy DM (very light DM)-nu interaction

Berlin, PRL 117 (2016) 231801 Krnjaic et al., 1705.06740 Brdar et al., 1705.09455



Cosmic neutrinos as a probe to secret neutrino interactions

Deviation from a power-law spectrum?





Cosmic neutrinos as a probe to secret neutrino interactions





Cosmic neutrinos as a probe to secret neutrino interactions



Resonant scattering in propagation, mediated by a secret nu-nu int.?

 Ioka Murase, PTEP 2014 (2014) 061E01
 Araki et al., PRD91 (2015) 037301

 Ng Beacom PRD90 (2014) 065035
 Kamada Yu,PRD92 (2015) 113004

 Ibe Kaneta PRD90 (2014) 053011
 DiFranzo Hooper PRD92 (2015) 095002

 Blum et al., 1408.3799
 Araki et al., PRD93 (2016) 013014





Secret neutrino interactions

Cosmic neutrino spectrum with the $L_{\mu} - L_{\tau}$ interaction



 $L_{\mu} - L_{\tau}$ gauge interaction

 $\mathcal{L} = g_{Z'} \left[\overline{\mu} \gamma^{\rho} \mu - \overline{\tau} \gamma^{\rho} \tau + \overline{\nu}_{\mu} \gamma^{\rho} \mathcal{P}_{L} \nu_{\mu} - \overline{\nu}_{\tau} \gamma^{\rho} \mathcal{P}_{L} \nu_{\tau} \right] Z'_{\rho} + (M_{Z'}^{2}/2) Z'_{\rho} Z'^{\rho}$ $+ \begin{array}{c} M_{Z'} = 11 \text{MeV} \\ g_{Z'} = 5 \cdot 10^{-4} \end{array} \quad \text{Contribution to muon g-2 is } a_{\mu}^{Z'} = 24.2 \cdot 10^{-10} \\ \text{Gap should not be deep} \rightarrow L_{\mu} - L_{\tau} \text{ will be tested} \end{array}$









NSIs with O(0.1-1) are phenomenologically allowed

It is possible for NSIs with O(0.01) to disturb the parameter determinations at the forthcoming experiments.

It may be time to "think freely and rightly" on future plans...



→ Trace out the oscillation pattern over a wide energy range

→ Separate the standard osc. effects from exotics

A new trend – Secret neutrino interactions with light mediators



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Summary



other writings nothing is stated about its

torso, so it is sometimes depicted to have the

"Kyoto Taibi (The End)" (京 印都 鵺 大尾) (among The Sixty-nine Stations of the Kiso Kaidō one that is by Utagawa Kuniyoshi, in Kaei 5 (1852), October)



Summary



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From Wikipedia, the free encyclopedia

For other uses, see NUE (disambiguation).

The Nue (鵺, 鵼, 恠鳥, or 奴延鳥) is a legendary Japanese yōkai or mononoke.

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- 4 The Nue's Remains
- 5 Landmarks
- 6 Culture related to nue
- 7 References

Appearance [edit]



In the *Heike Monogatari*, it is described as having the face of a monkey, the legs of a tiger, the body of a tanuki (Japanese raccoon dog) and the front half of a snake for a tail. In other writings nothing is stated about its torso, so it is sometimes depicted to have the



"Kyoto Nue Taibi (The End)" (京 印都 鵺 大尾) (among The Sixty-nine Stations of the Kiso Kaidō one that is by Utagawa Kuniyoshi, in Kaei 5 (1852), October)



Summary









PMNS elements constrained from oscillation experiments





Relation between non-unitarity η and NSI ϵ

Non-unitarity appears in osc. as "correlated NSIs"

$$\begin{split} N_{\alpha i} &\equiv \left[\delta_{\alpha\beta} - \eta_{\alpha\beta}\right] \mathcal{U}_{\beta i} \\ \eta_{ee} &= -\epsilon^m_{ee} \ \eta_{\mu\mu} = \epsilon^m_{\mu\mu} \ \eta_{\tau\tau} = \epsilon^m_{\tau\tau} \ \eta_{\mu\tau} = \epsilon^m_{\mu\tau} \ \epsilon^m_{e\mu} = \epsilon^m_{e\tau} = 0 \ \eta_{\alpha\beta} = -\epsilon^{s,d}_{\beta\alpha} \end{split}$$

$$\end{split}$$

$$Meloni \text{ et al., JHEP1004 (2010) 041}$$

$$at the first order of \eta$$

$$Blennow \text{ et al., JHEP 04 (2017) 153}$$

Sensitivities to η at forthcoming LBLs are $\mathcal{O}(10^{-2})$ except $\eta_{e\mu}$ and $\eta_{e\tau}$

The other parametrization method of the non-unitary PMNS Escrihuela et al., 1612.07377 Blennow et al., JHEP 04 (2017) 153

$$N_{\alpha i} \equiv \begin{bmatrix} \delta_{\alpha\beta} - \alpha_{\alpha\beta} \end{bmatrix} \mathcal{V}_{\beta i}$$
$$\alpha = \begin{pmatrix} \alpha_{ee} & 0 & 0\\ \alpha_{\mu e} & \alpha_{\mu\mu} & 0\\ \alpha_{\tau e} & \alpha_{\tau\mu} & \alpha_{\tau\tau} \end{pmatrix}$$

	Non-Unitarity	Averaged-out sterile
α_{ee}	$1.3 \cdot 10^{-3}$	$2.6\cdot10^{-2}$
$\alpha_{\mu\mu}$	$2.0\cdot 10^{-4}$	$4.5 \cdot 10^{-2}$
$\alpha_{\tau\tau}$	$2.8\cdot 10^{-3}$	10^{-1}
$\alpha_{\mu e}$	$6.8\cdot 10^{-4}\; (2.4\cdot 10^{-5})$	$4.8\cdot 10^{-2}$
$\alpha_{\tau e}$	$2.7\cdot 10^{-3}$	$7.2\cdot 10^{-2}$
$\alpha_{\tau\mu}$	$1.2\cdot 10^{-3}$	$9.5\cdot10^{-2}$



Secret neutrino interactions

Gap in the spectrum – Secret interaction between Cosmic nu and CnuB?

Resonance condition



Condition to mean free path

 $\lambda \simeq 1/n_{\mathrm{C}\nu\mathrm{B}}\sigma_{\mathrm{@Res}} \stackrel{\cdot}{\lesssim} \mathrm{Gpc}$

 $\sigma_{\odot Res} \gtrsim 10^{-30} [cm^2]$

so that cosmic neutrinos from extra galactic sources get the scattering

 $n_{\rm C\nu B} = 56.8 [/\rm cm^3]$ for each dof $\gg n_{\rm Baryon}$

 $L_{\mu} - L_{\tau}$ model

$$\mathscr{L} = g_{Z'} \left[\overline{\mu} \gamma^{\rho} \mu - \overline{\tau} \gamma^{\rho} \tau + \overline{\nu}_{\mu} \gamma^{\rho} \mathcal{P}_{L} \nu_{\mu} - \overline{\nu}_{\tau} \gamma^{\rho} \mathcal{P}_{L} \nu_{\tau} \right] Z'_{\rho} \qquad g_{Z'} > 10^{-4}$$
$$\sigma(\nu_{i} \overline{\nu}_{j} \to \nu \overline{\nu}) = \frac{|g_{ji}|^{2} g_{Z'}^{2}}{6\pi} \frac{s}{(s - M_{Z'}^{2})^{2} + M_{Z'}^{2} \Gamma_{Z'}^{2}} \qquad g_{ji} = g_{Z'} \sum_{\alpha} U_{j\alpha}^{\dagger} \operatorname{diag}(0, 1, -1)_{\alpha} U_{\alpha i}$$