

# EARTH TOMOGRAPHY WITH NEUTRINOS

*Sergio Palomares Ruíz*

IFIC, CSIC-U. Valencia



Based on **A. Donini, SPR** and J. Salvado, *Nature Physics* 15:37, 2019

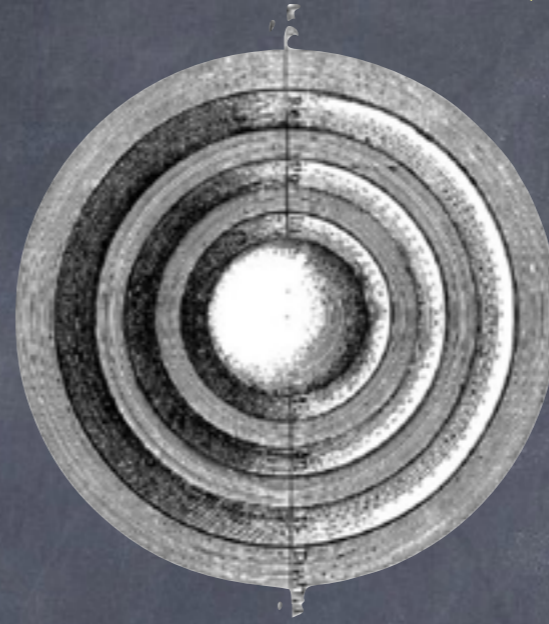
4th Uppsala workshop on  
Particle Physics with Neutrino Telescopes

October 9, 2019

# THE EARTH'S INTERIOR: EARLY (CRAZY) IDEAS

First hypothesis based on observations: Hollow Earth

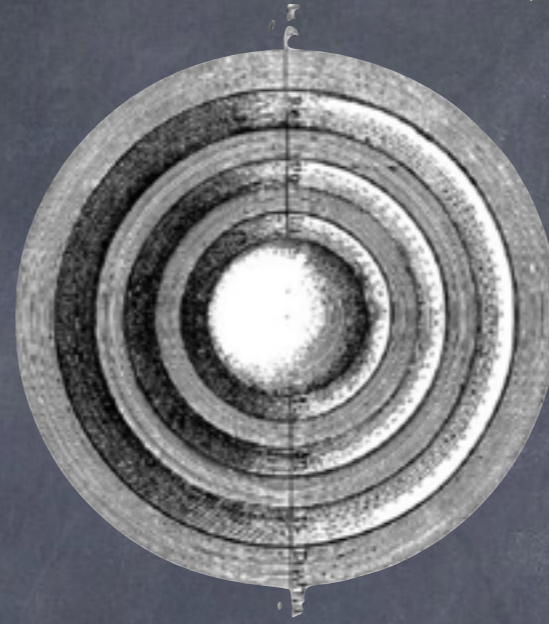
E. Halley, 1692



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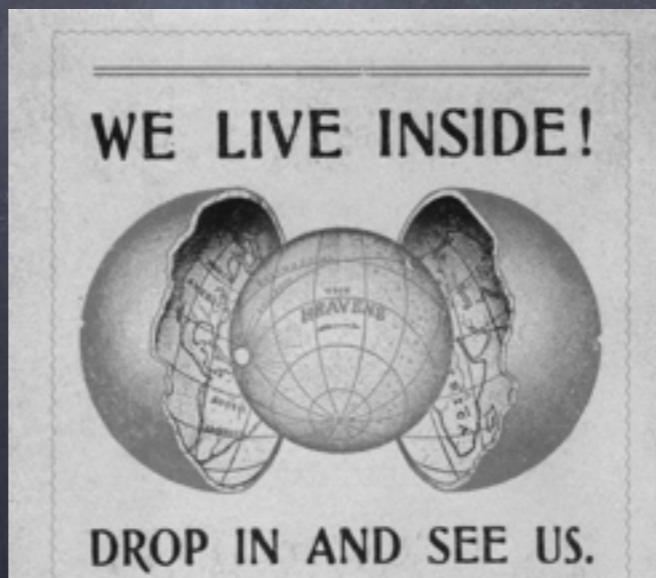
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... and then even crazier ideas...



J. C. Symmes, 1818

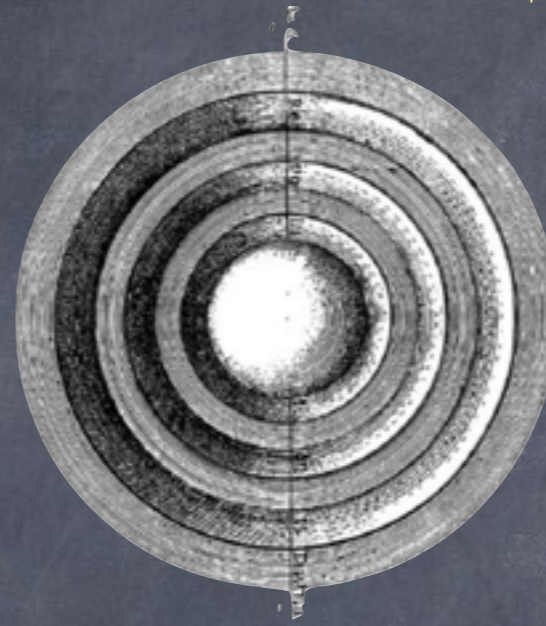


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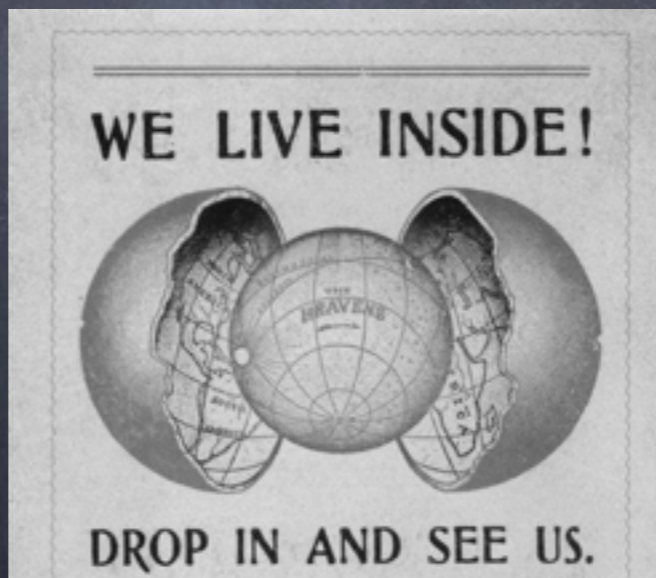
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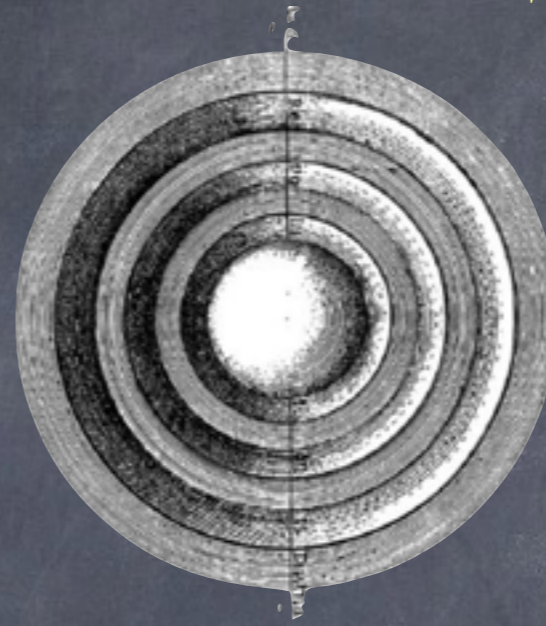
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Earth tomography with neutrinos

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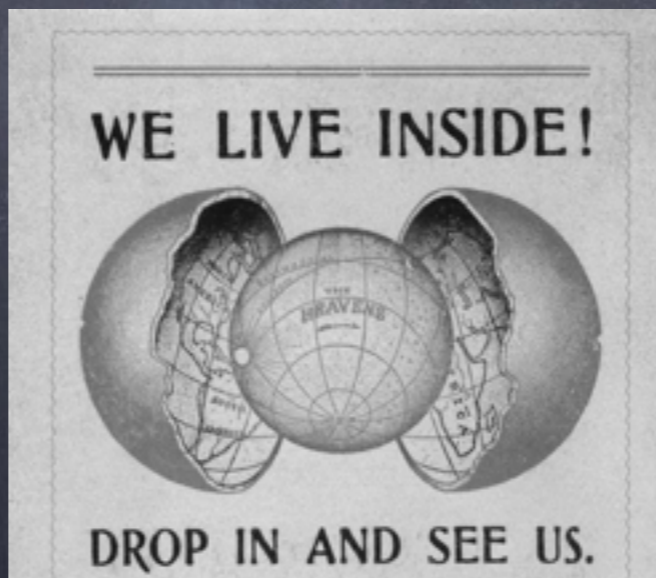
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GLOBE SHOWING SECTION OF THE EARTH'S INTERIOR

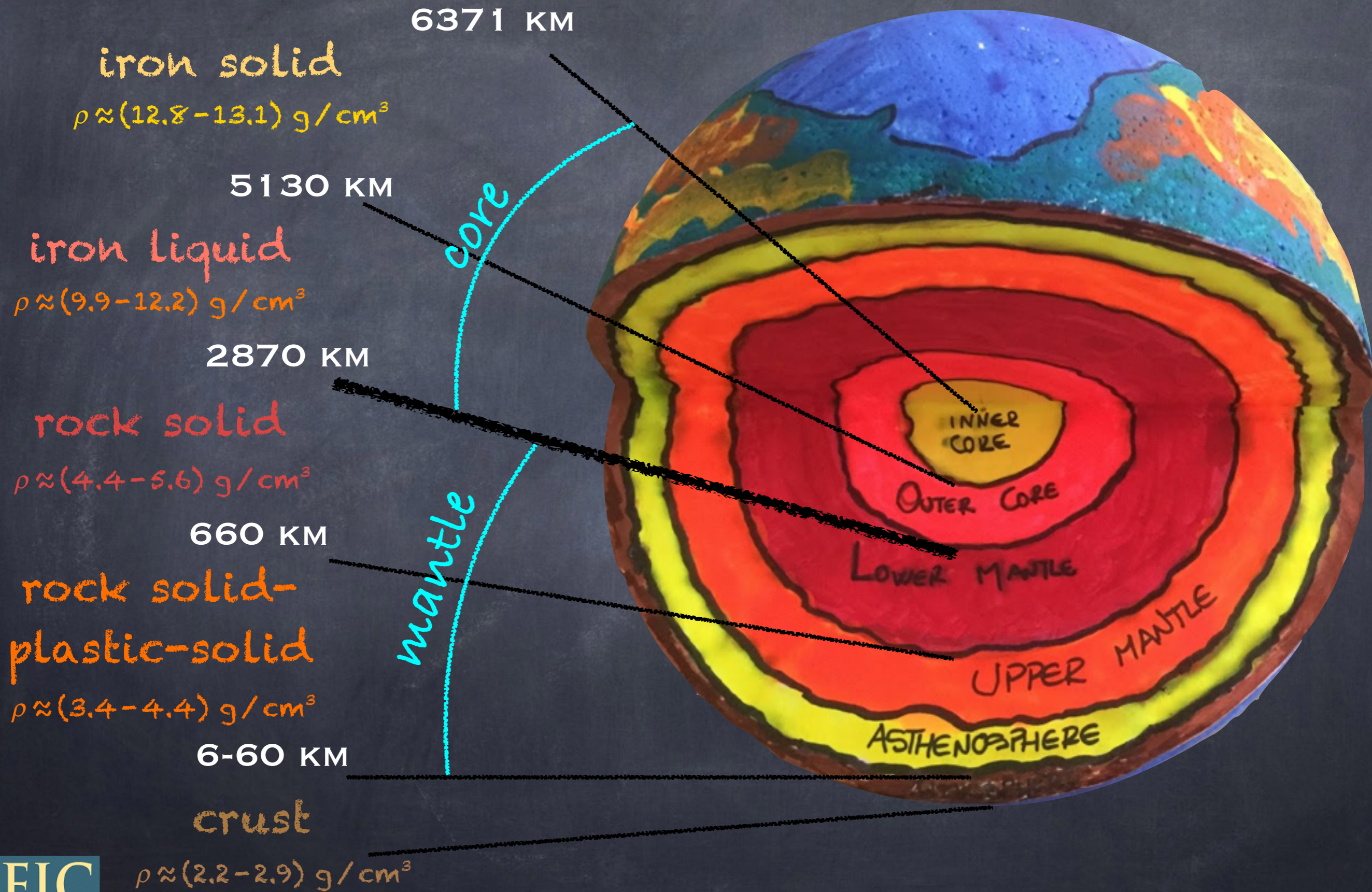
The earth is hollow. The poles so long sought are but phantoms. There are openings at the northern and southern extremities. In the interior are vast continents, oceans, mountains and rivers. Vegetable and animal life are evident in this new world, and it is probably peopled by races yet unknown to the dwellers upon the earth's exterior.

THE AUTHOR.

W. Reed, The phantom of the poles, 1906

Earth tomography with neutrinos

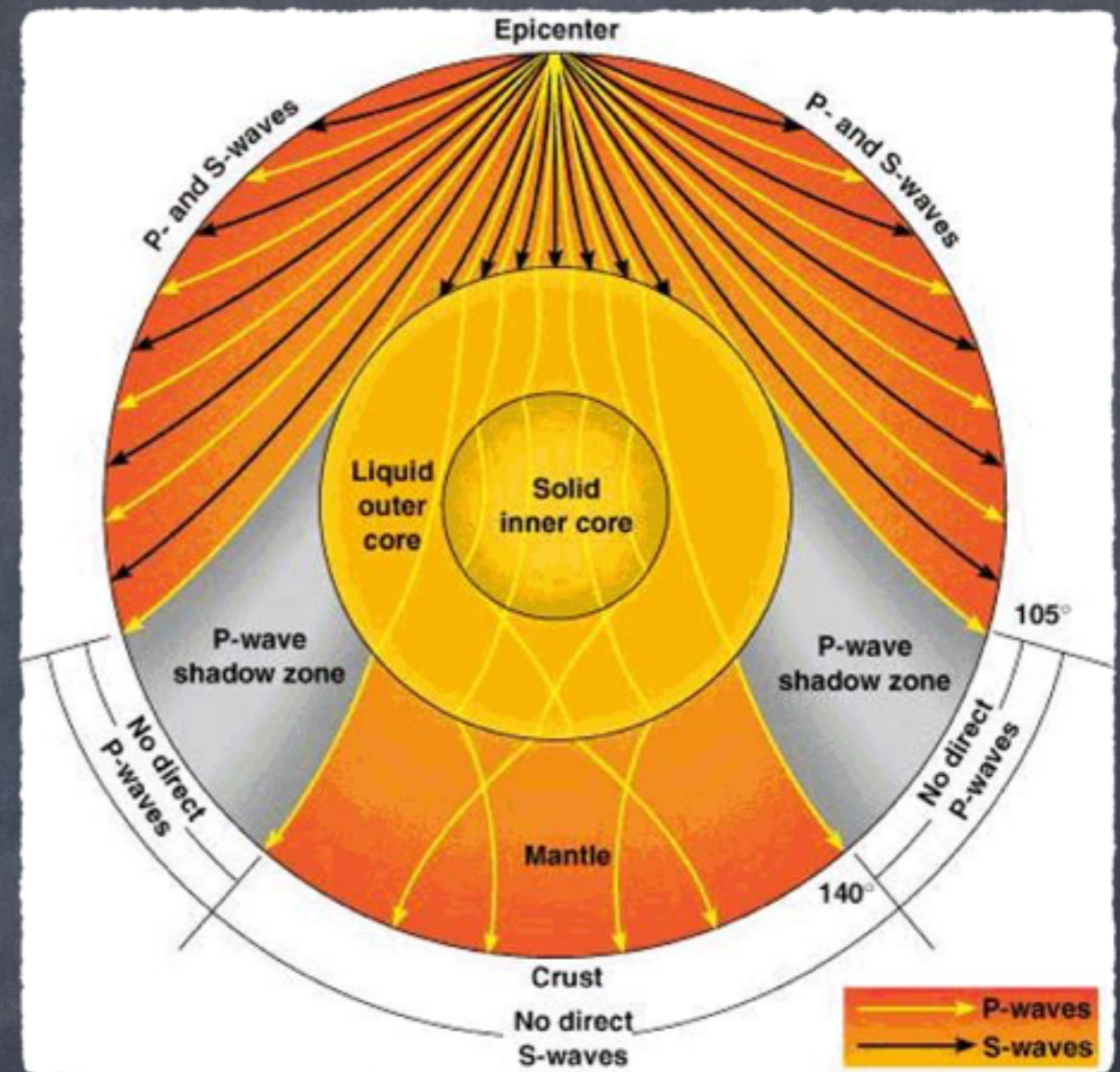
# THE EARTH'S INTERIOR: THE MODERN VIEW



# THE EARTH'S INTERIOR: HOW IS IT INFERRED?

## Earthquakes:

O(100/yr) with magnitude > 6  
Shaking and trembling of Earth's surface caused by sudden release of stress within the crust



## Seismic waves:

**P-waves** -> compressional: travel through liquids and solids

**S-waves** -> shear: travel through solids only

propagation depends on composition, temperature and pressure

# THE EARTH'S MASS AND MOMENT OF INERTIA: GRAVITATIONAL MEASUREMENTS

GM: satellite laser ranging (SLR)

Measures the gravity field

$$GM = 3.986004418(4) \times 10^{14} \text{ m}^3 \text{ s}^{-2}$$

J. C. Ries, Geophys. Res. Abs. 9:10809, 2007



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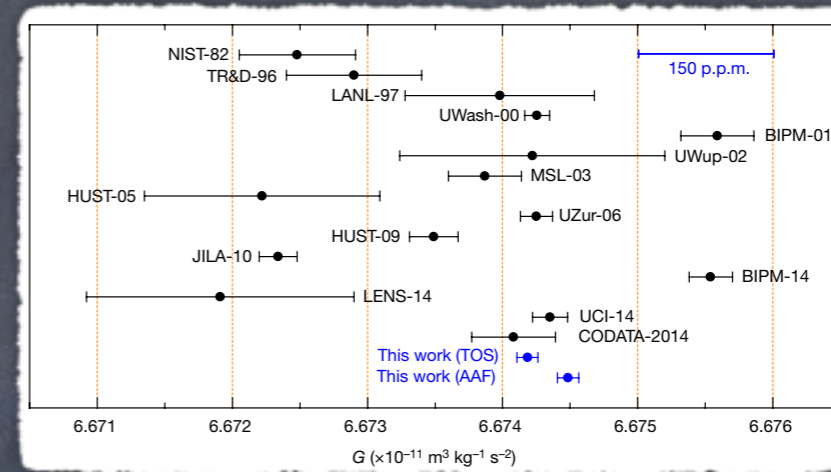
G: variations of the  
Cavendish experiment

$$G = 6.67408(31) \times 10^{-11} \text{ kg}^{-1} \text{ m}^3 \text{ s}^{-2}$$

P. J. Mohr, D. B. Newell and B. N. Taylor, CODATA-2014,  
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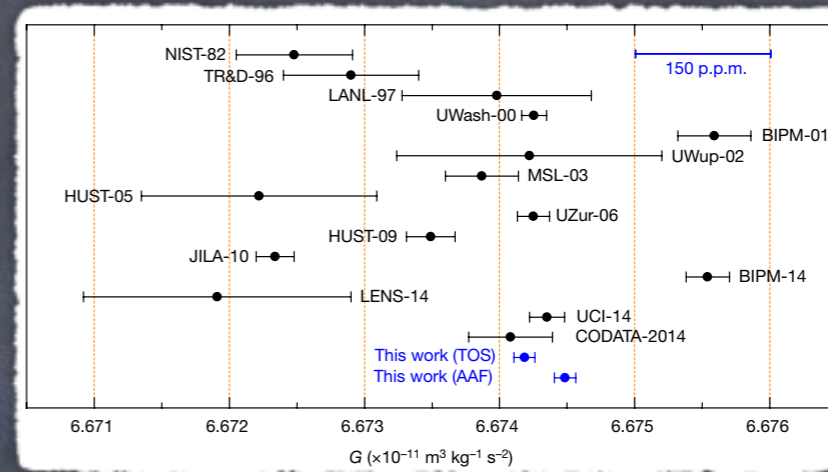
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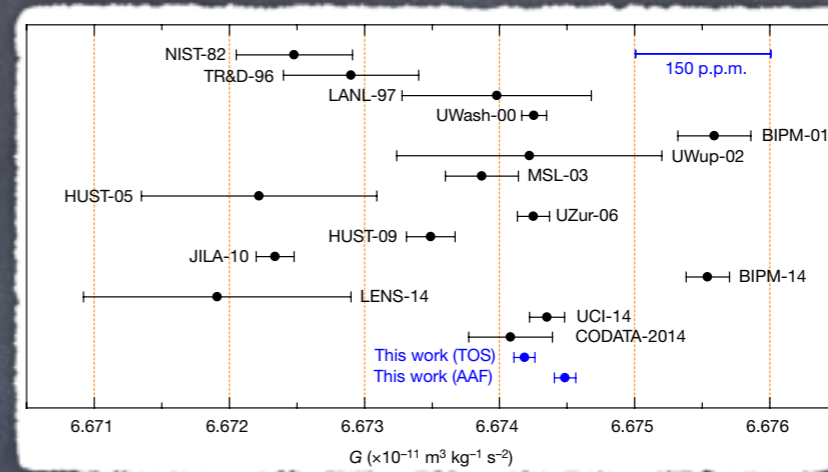
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Earth gravity model:  
terrestrial, altimetry-derived  
and airborne gravity data

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Q. Li et al., Nature 560:582, 2018

$$I = 8.01736(96) \times 10^{37} \text{ kg m}^2$$

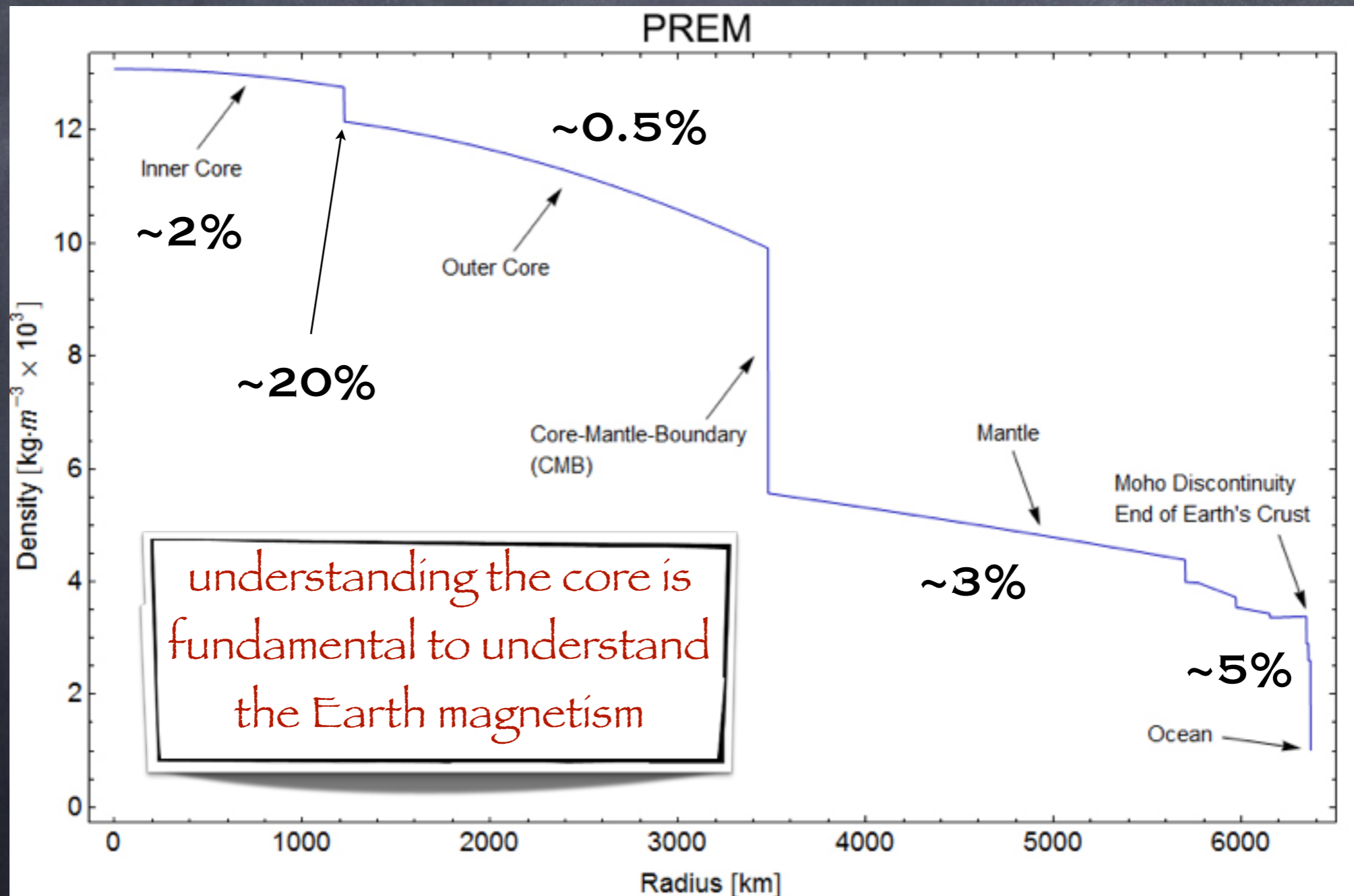
W. Chen et al., J. Geod. 89:179, 2015

# PRELIMINARY REFERENCE EARTH MODEL (PREM)

A. M. Dziewonski and D. L. Anderson, Phys, Earth Planet. Inter. 25:297, 1981

## 1-D density profile

From seismic wave data and imposing the Earth's radius, mass and moment of inertia as additional constraints



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Yes!

Weak interactions: Neutrinos!

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Old idea: First mentioned in...

a 1973 CERN report

A. Placci and E. Zavattini, submitted in October 1973 to Nuovo Cimento... but never published

and a 1974 talk

L. V. Volkova and G. T. Zatsepin, Izv. Akad. Nauk. Ser. Fiz. 38N5:1060, 1974

Using man-made neutrino beams

# oscillation tomography

## Man-made beams

V. K. Ermilova, V. A. Tsarev and V. A. Chechin, JETP Lett. 43:453, 1986

## Solar neutrinos

A. N. Ioanissian and A. Smirnov, hep-ph/0201012

## Supernova neutrinos

E. K. Akhmedov, M. A. Tortola and J. W. F. Valle, JHEP 0506:053, 2005

## Atmospheric neutrinos

S. K. Agarwalla, T. Li, O. Mena and SPR, arXiv:1212.2238

## Coherent effect in neutrino propagation

$$\frac{d\phi_\nu(E_\nu, x)}{dx} = -i \left( U H_{vac} U^\dagger + V_m \right) \phi_\nu(E_\nu, x)$$

$$P_{2\nu}(v_\alpha \rightarrow v_\beta) = \sin^2 2\theta^m \sin^2 \left( \frac{\Delta^m L}{4E} \right)$$

$$\Delta^m = \sqrt{(\Delta m^2 \cos 2\theta \mp 2EV)^2 + (\Delta m^2 \sin 2\theta)^2}$$

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## Cosmic neutrinos

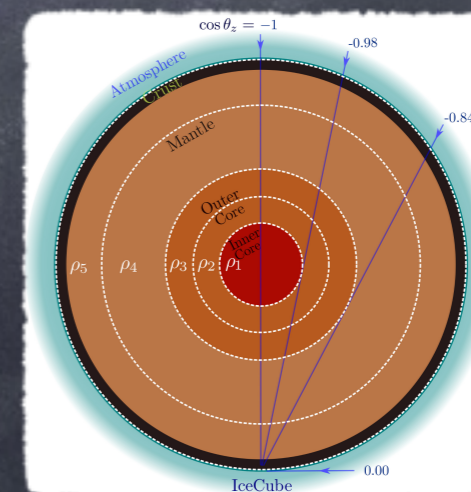
T. L. Wilson, Nature 309:38, 1984

## Atmospheric neutrinos

M. C. González-García, F. Halzen, M. Maltoni and H. K. M. Tanaka, Phys. Rev. Lett. 100:061802, 2008

## Incoherent effect in neutrino propagation

$$\frac{d\phi_\nu(E_\nu, x)}{dx} \approx -n(x) \sigma(E_\nu) \phi_\nu(E_\nu, x)$$



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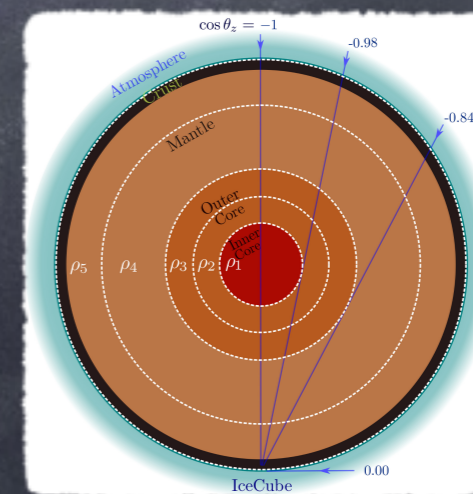
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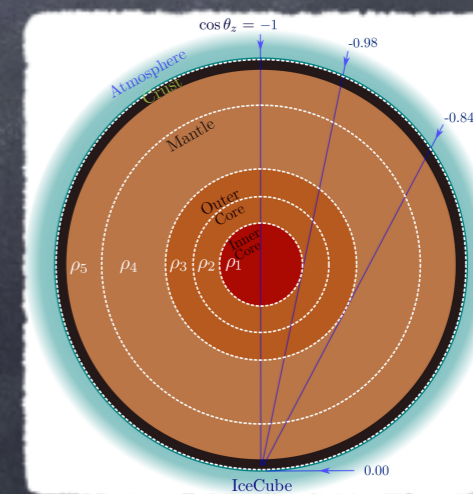
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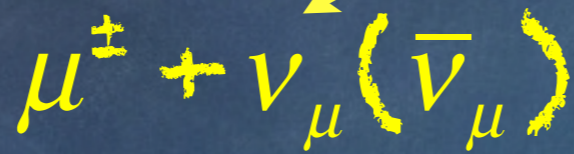
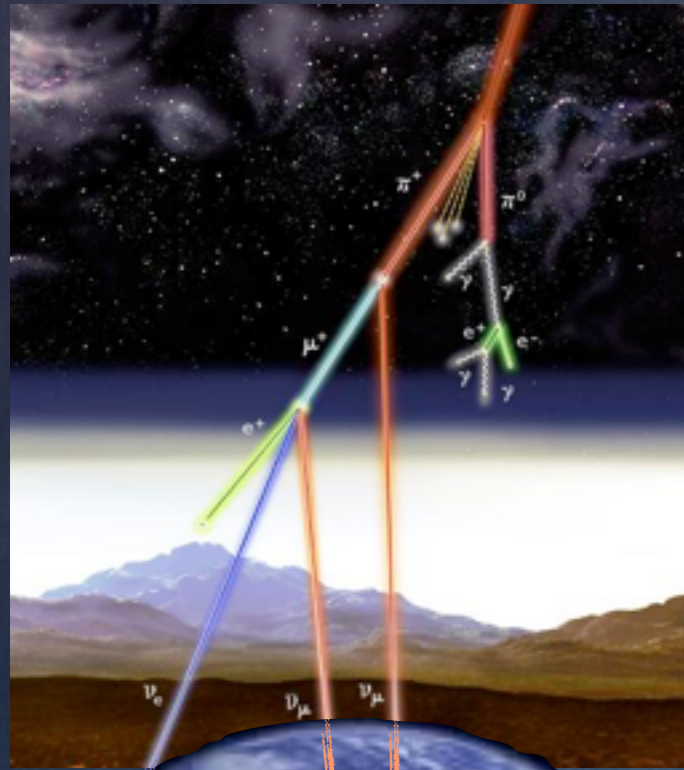


# diffraction

Coherent effect: Unfeasible

A. D. Fortes, I. G. Wood and L. Oberauer, Astron. Geophys, 47:5.31, 2006

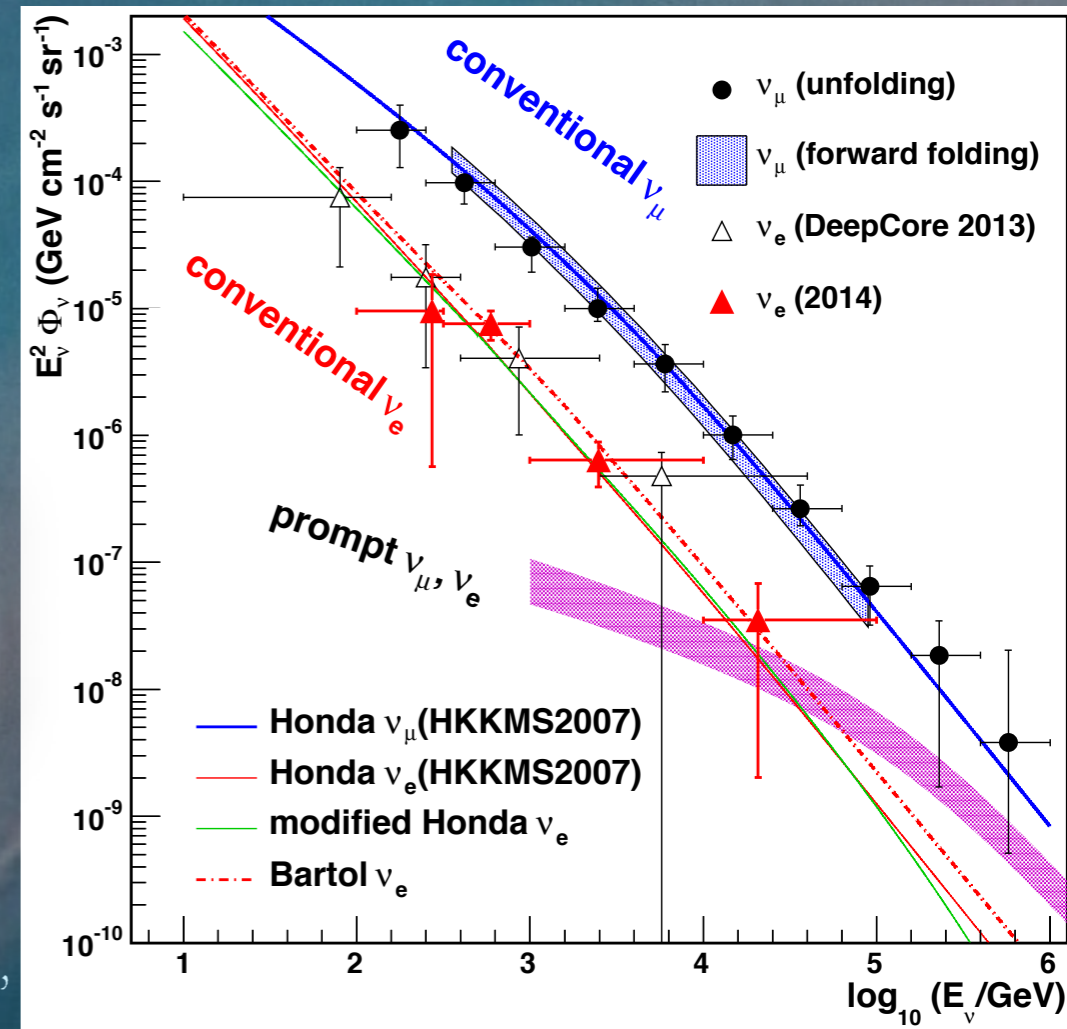
# ATMOSPHERIC NEUTRINOS



Huge range of energies and baselines

$E < 100 \text{ TeV}$

$$n\sigma \sim \left( \frac{E}{40 \text{ TeV}} \right) R_\oplus^{-1}$$

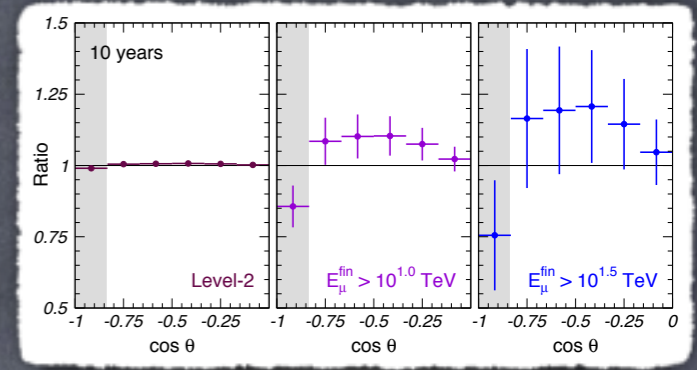


M. G. Aartsen et al. [IceCube Collaboration],  
Phys. Rev. D91:122004, 2015

# PREVIOUS STUDIES

First forecast of absorption neutrino tomography using atmospheric neutrinos (for IceCube)

M. C. González-García, F. Halzen, M. Maltoni and H. K. M. Tanaka, Phys. Rev. Lett. 100:061802, 2008



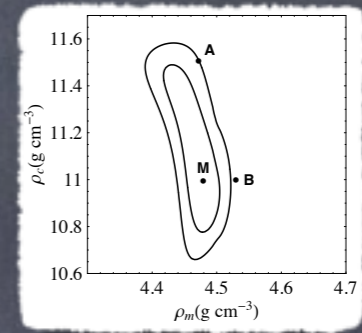
Non-homogeneity at  $(3.4-4.7)\sigma$  after 10 years

First forecast for KM3NeT

E. Borriello et al., JCAP 0906:030, 2009

E. Borriello et al., Earth Planets Space 62:211, 2010

few percent error after 10 years



Study of lateral heterogeneities (with IceCube)

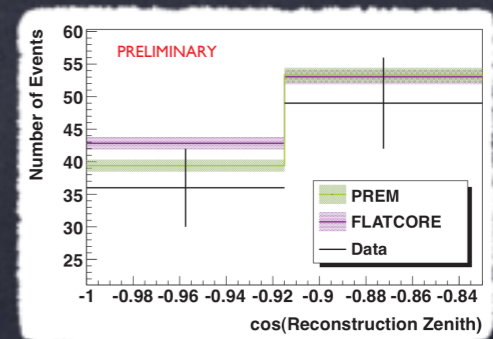
Needs ~300 years

N. Takeuchi, Earth Planets Space 62:215, 2010

Another study of Earth non-homogeneity (with IceCube)

I. Romero and O. A. Sampayo, Eur. Phys. J. C71:1696, 2011

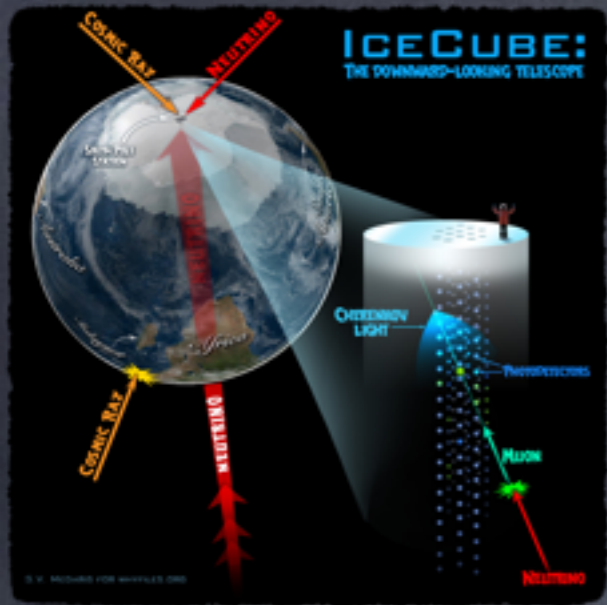
First attempt using 1 year of IC-40 data



K. Hoshina and H. K. M. Tanaka, Poster at Neutrino 2012

Earth tomography with neutrinos

# ICECUBE DATA SET

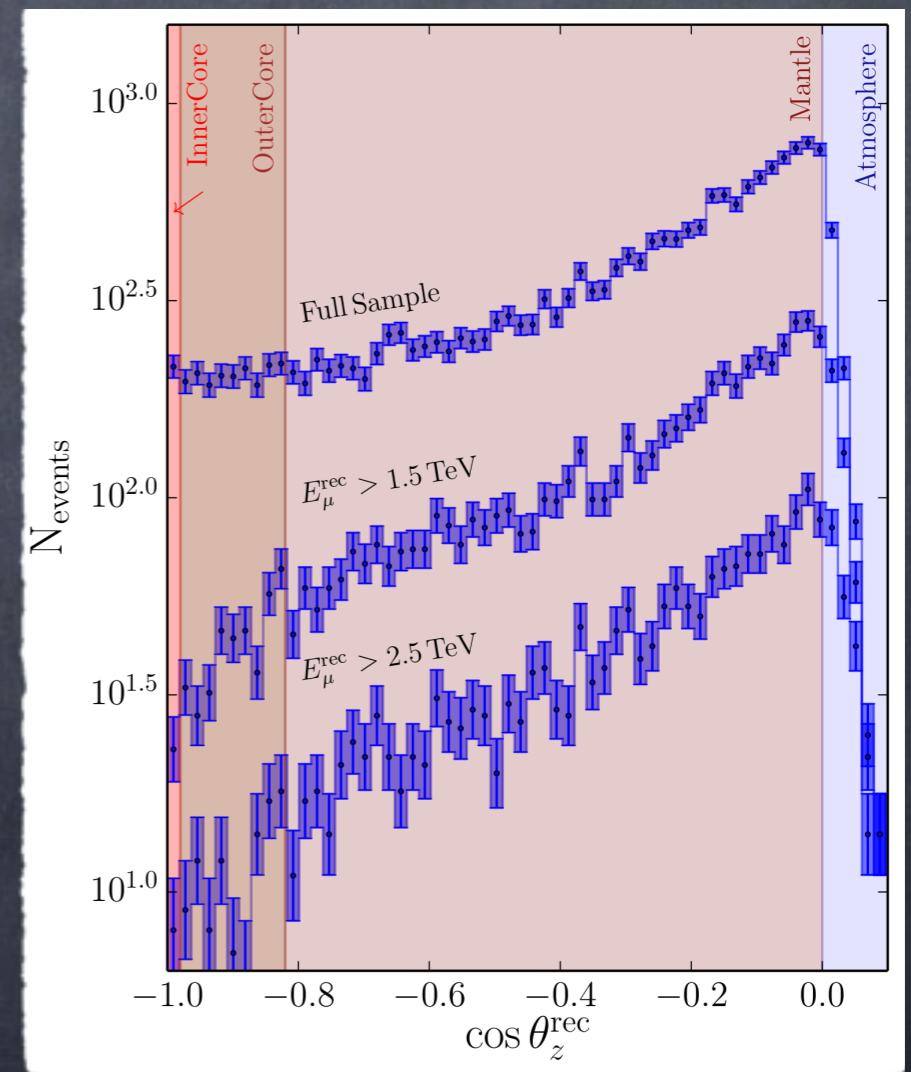


1 year of up-going high-energy muon neutrino events (IC86)  
used and prepared for the IC sterile neutrino analysis

M. G. Aartsen et al. [IceCube Collaboration], Phys. Rev. Lett. 117:071801, 2016

Energy range:  $\sim 400 \text{ GeV} - 20 \text{ TeV}$   
Zenith angle range:  $\cos \theta = [-1, 0.2]$   
Number of events: 20145 (343.7 days)  
>99.9% muon neutrino purity

Publicly available!



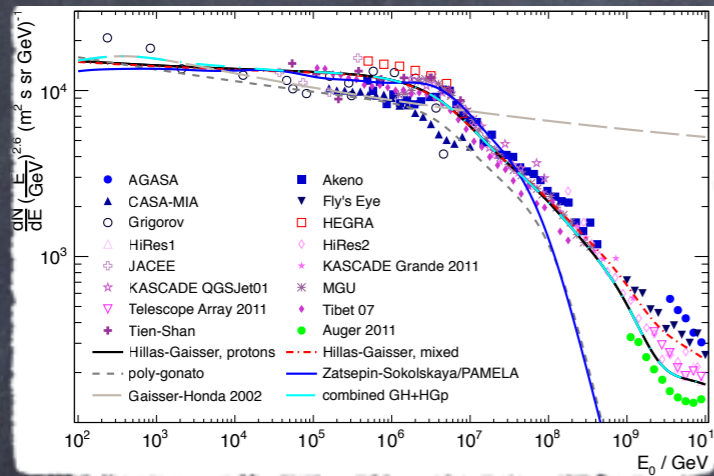
A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

Earth tomography with neutrinos

# ANALYSIS INGREDIENTS

## Primary cosmic-ray spectrum

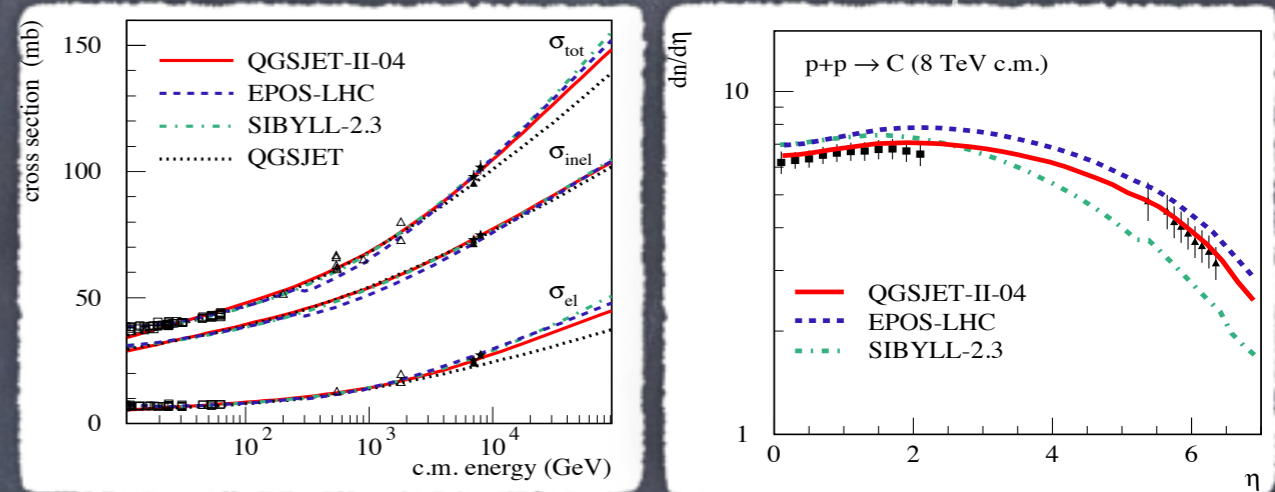
3-population models to fit cosmic-ray data



A. Fedynitch, J. B. Tjus and P. Desiati,  
Phys. Rev. D86:114024, 2012

## Hadronic-interaction model

Models for cascade development

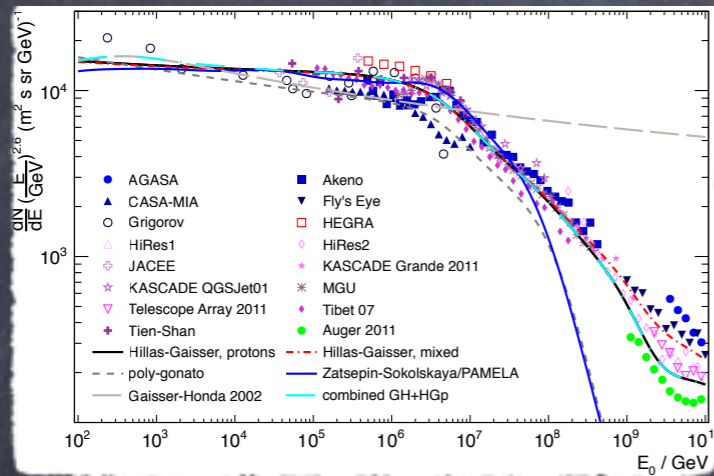


S. Ostapchenko, ECRS 2016, arXiv:1612.09461

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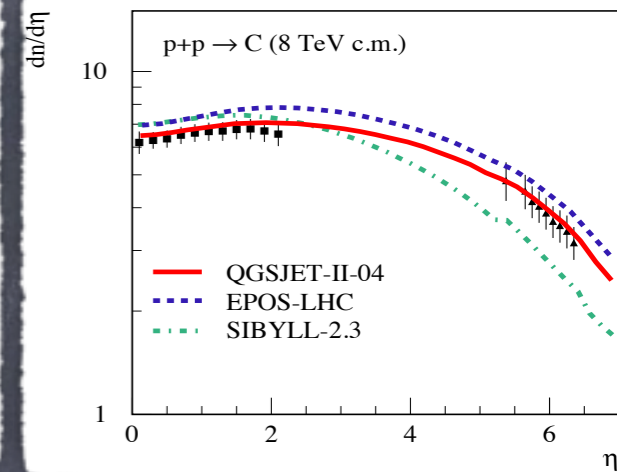
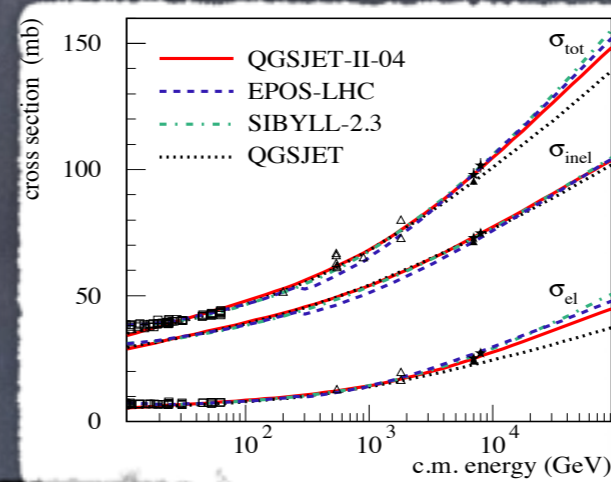
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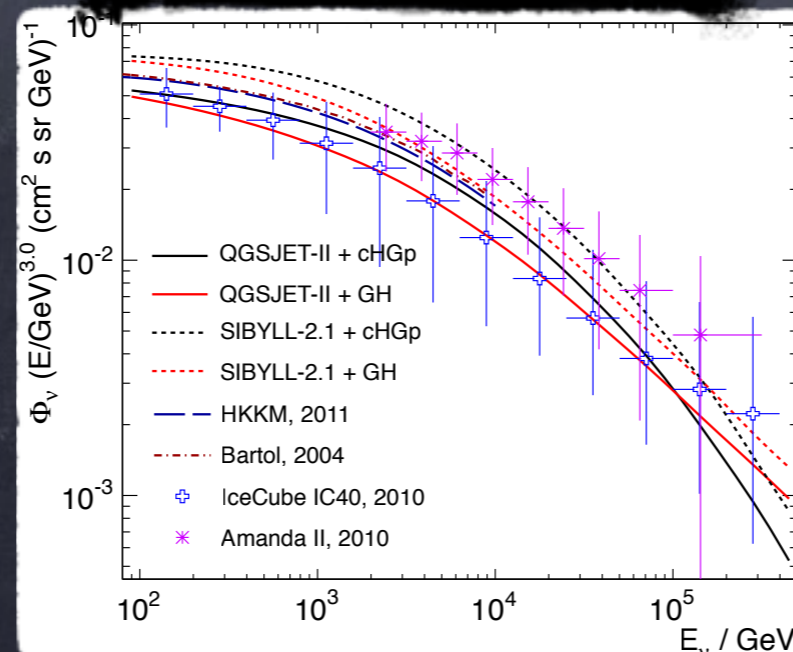
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S. Ostapchenko, ECRS 2016, arXiv:1612.09461

## Neutrino flux



A. Fedynitch, J. B. Tjus and P. Desiati,  
Phys. Rev. D86:114024, 2012

Earth tomography with neutrinos



# ANALYSIS INGREDIENTS

*Neutrino propagation through the Earth*

we propagate neutrinos with  $\nu$ -SQuIDS

C. Argüelles, J. Salvado and C. Weaver, <https://github.com/arguelles/nuSQuIDS>

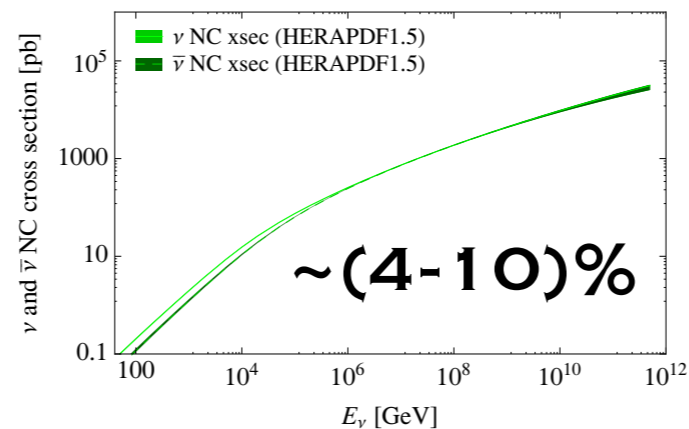
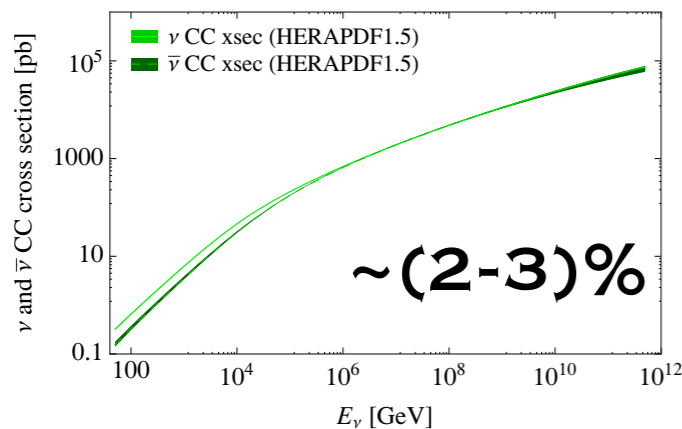
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## Neutrino interactions with nucleons



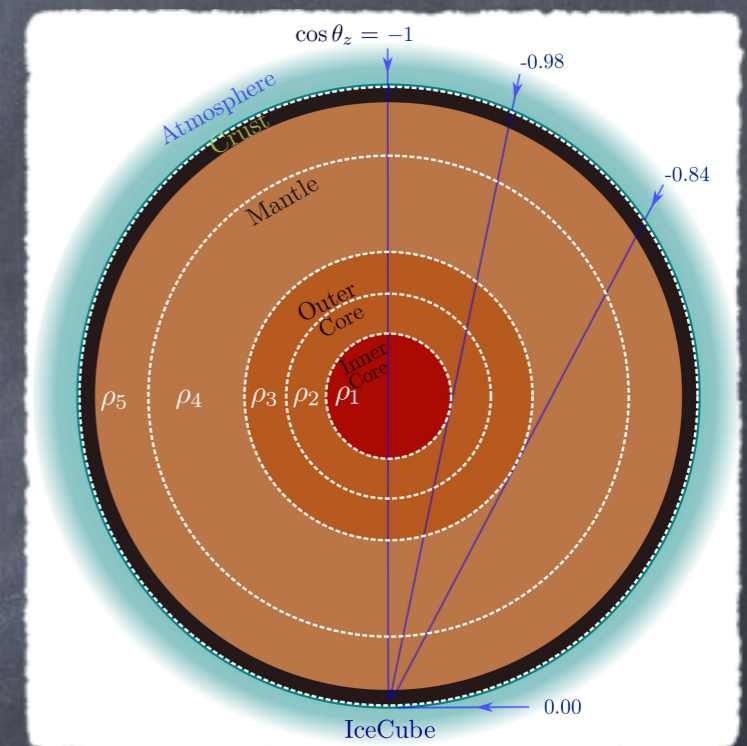
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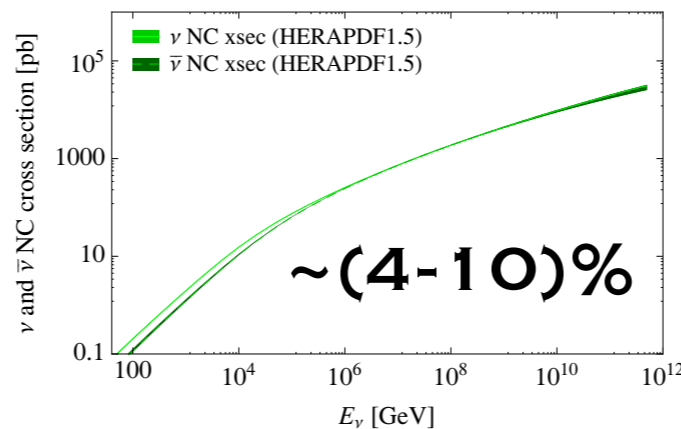
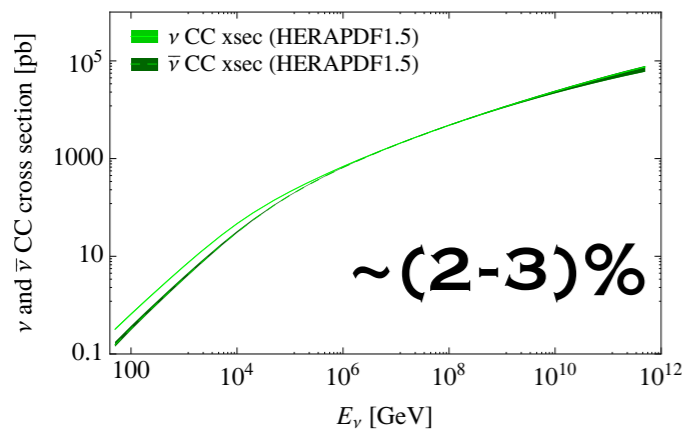
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## Earth model



## Neutrino interactions with nucleons



5 spherical layers:  
 1 for the inner core  
 2 for the outer core  
 2 for the mantle

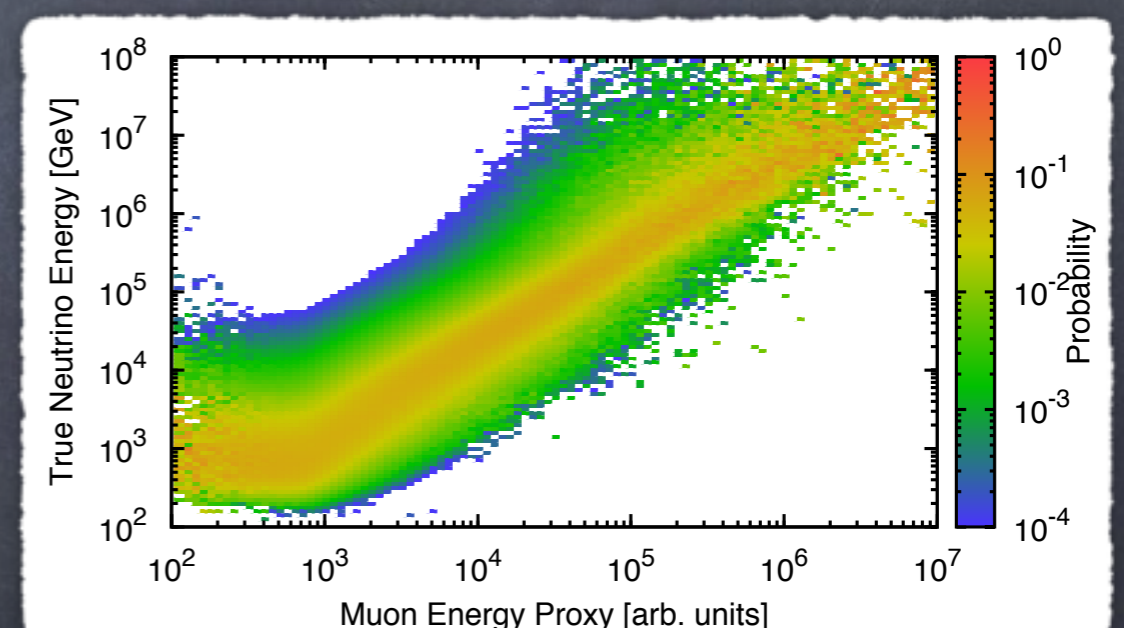
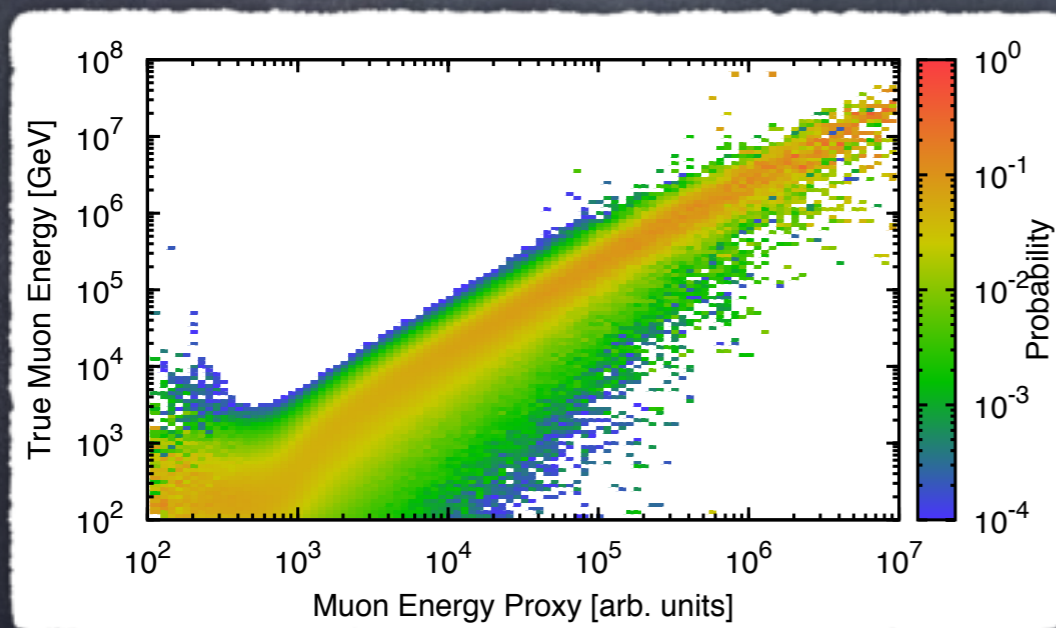
# ANALYSIS INGREDIENTS

Detector simulation

Publicly available!

We map  $E_\nu$  and  $\theta_\nu$  to  $E_{\text{rec}}$  and  $\theta_{\text{rec}}$  using the official IceCube Monte Carlo

<https://icecube.wisc.edu/science/data/IC86-sterile-neutrino>



M. G. Aartsen et al. [IceCube Collaboration], Phys. Rev. Lett. 115:081102, 2015

$$\sigma_{\log(E_\mu/\text{GeV})} \sim 0.5$$

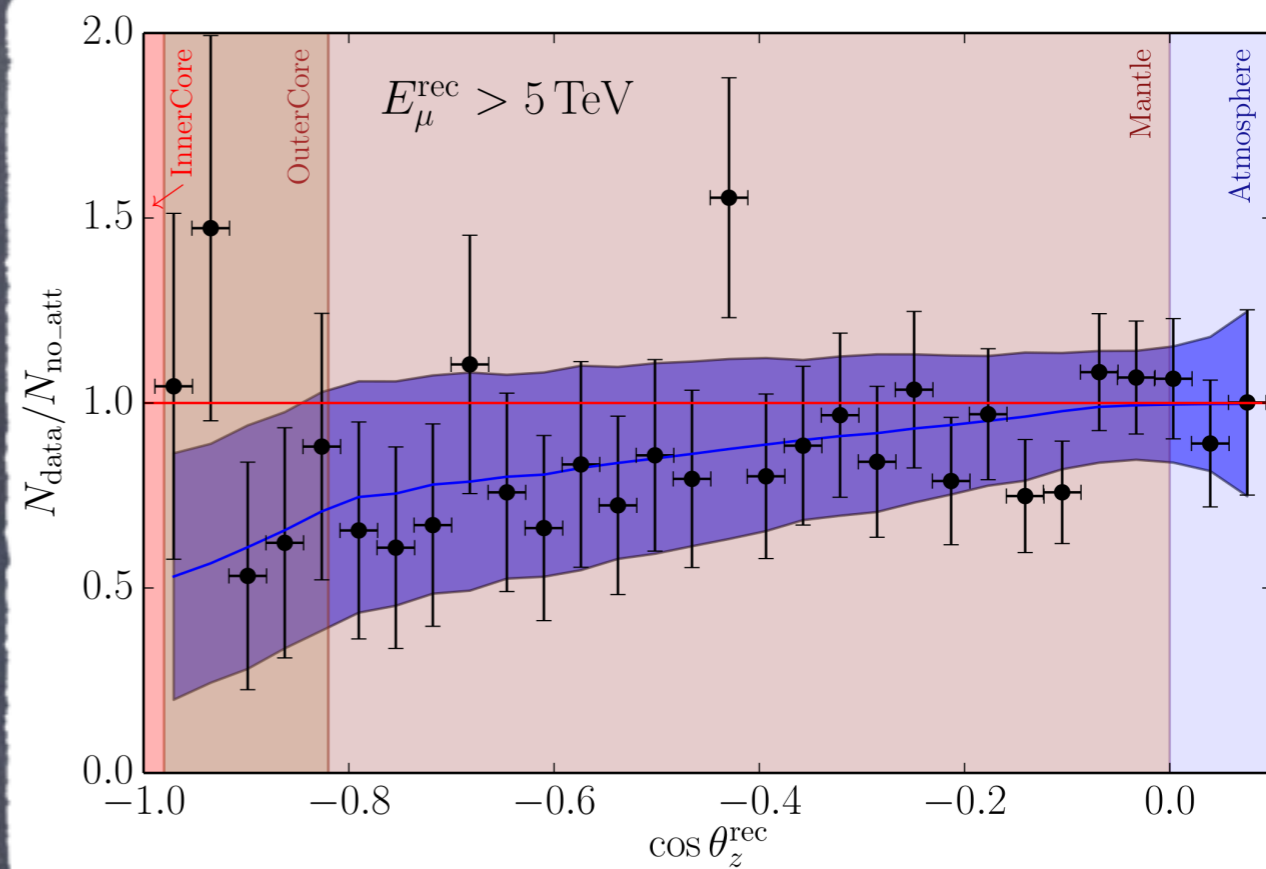
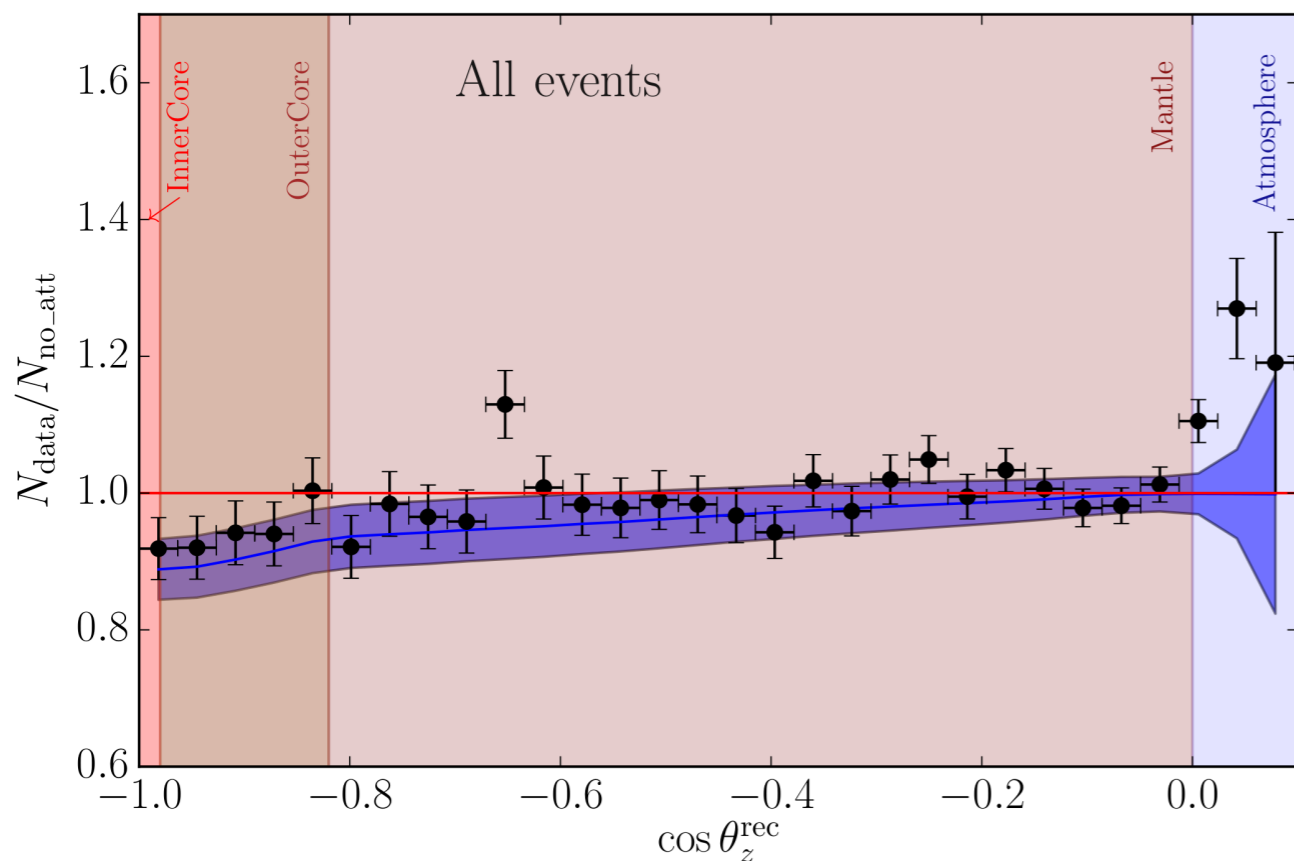
$$\sigma_{\cos(\theta)} \sim 0.005 - 0.015$$

# IS THE EARTH THERE?



All events

$E > 5 \text{ TeV}$



A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

Full sample:  
useful to fix normalization

core-crossing neutrinos:  
attenuation can be 50% ( $>5 \text{ TeV}$ )

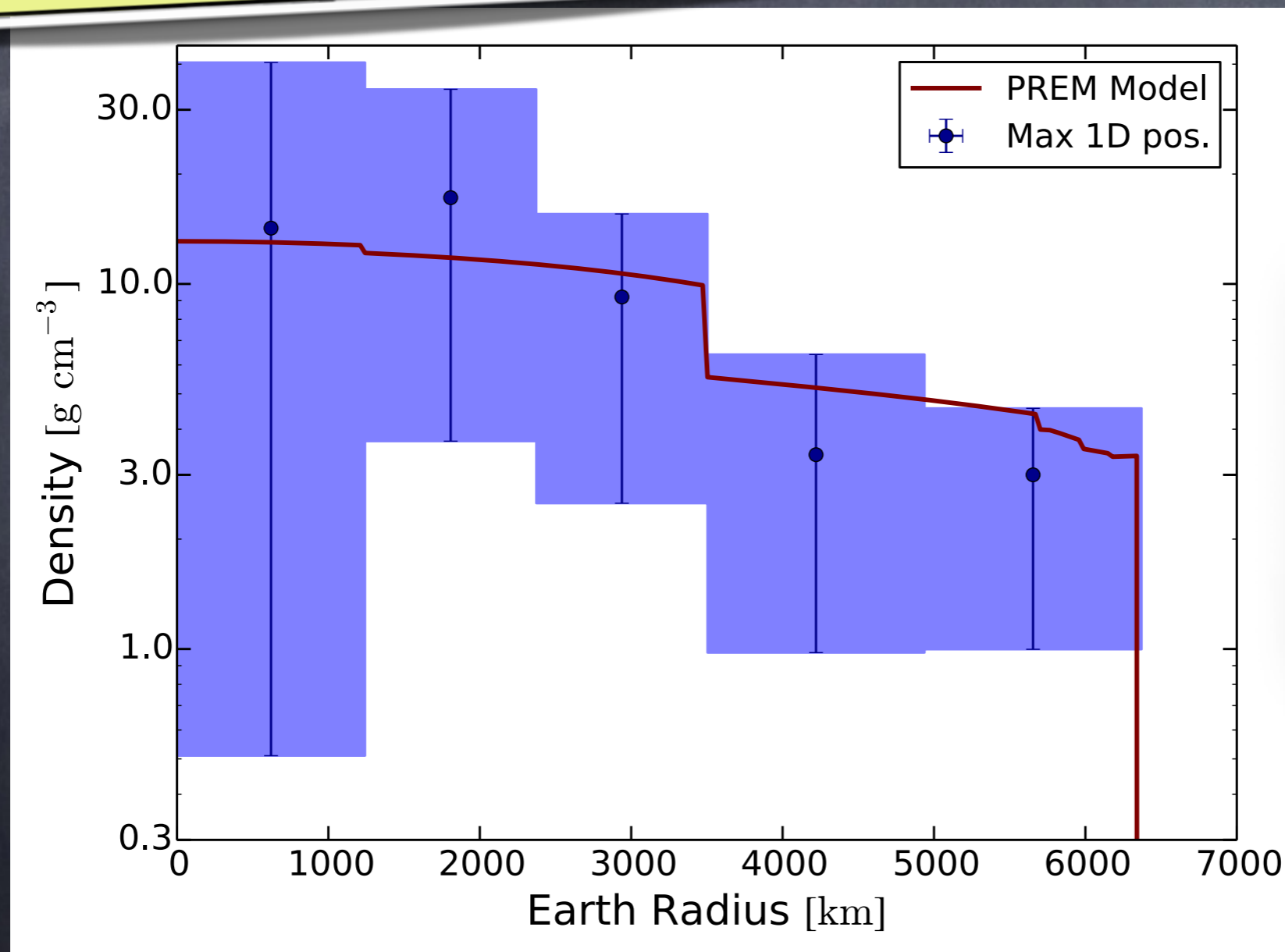
# MAIN RESULT: 1-D DENSITY PROFILE

First Earth tomography  
with neutrinos!

nature  
physics

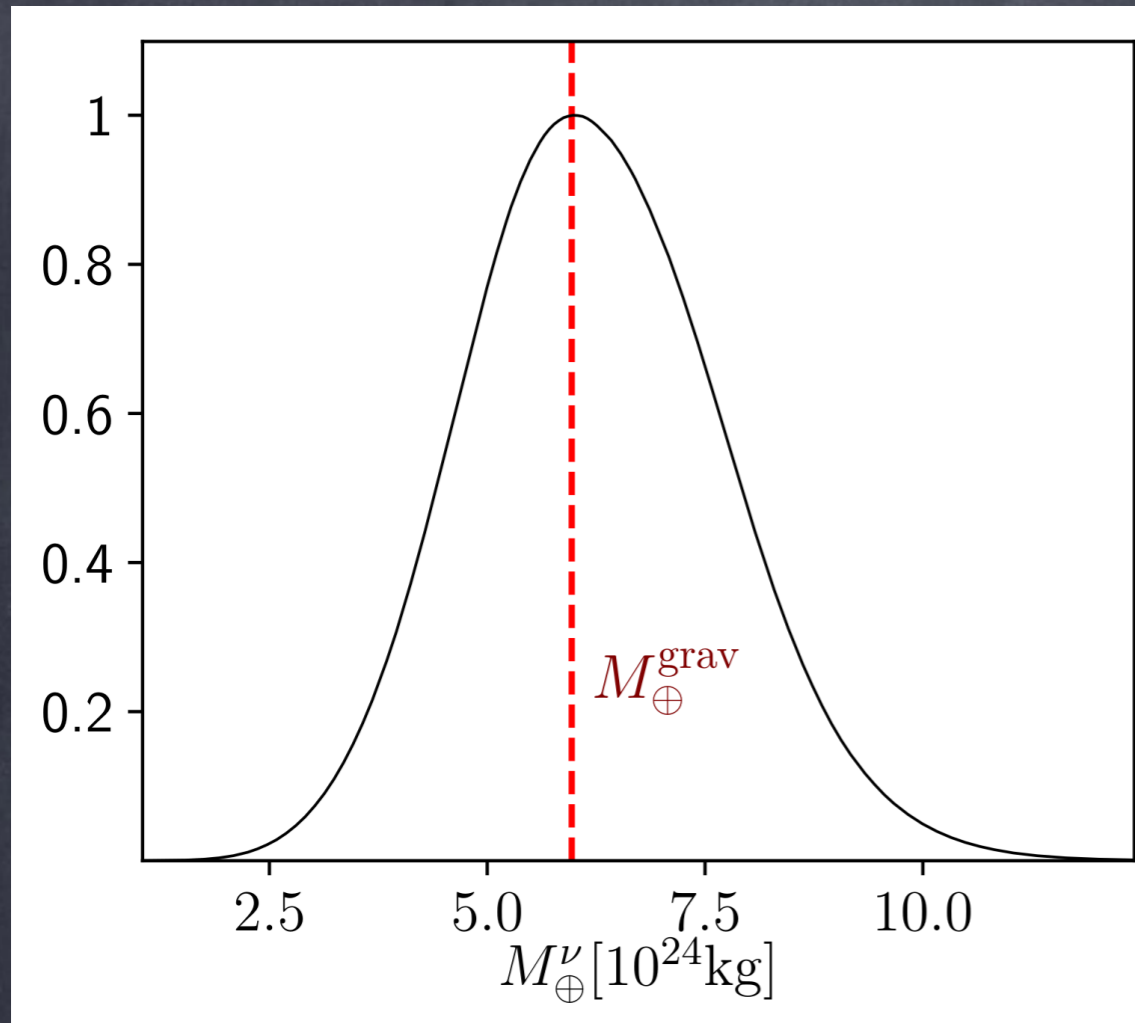
## Neutrino tomography of Earth

Andrea Donini<sup>1</sup>, Sergio Palomares-Ruiz<sup>1\*</sup> and Jordi Salvado<sup>1,2</sup>



unlike reconstructions  
with seismic data,  
NO constraint on the  
Earth mass or moment  
of inertia

# EARTH'S MASS



First measurement of the Earth's mass using the weak force!

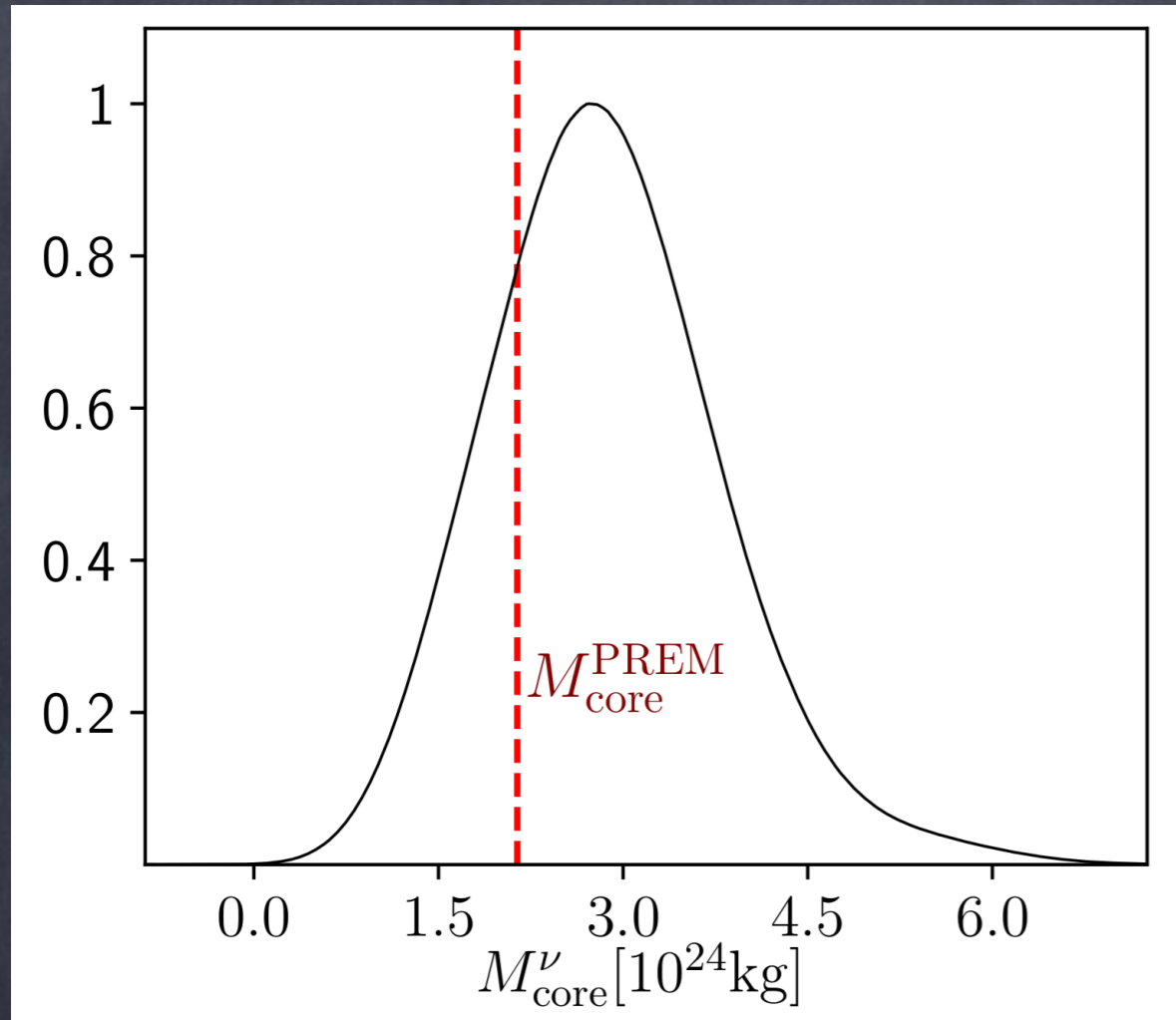
$$M_{\nu} = \left( 6.0^{+1.6}_{-1.3} \right) \times 10^{24} \text{ kg}$$

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

Gravitational measurement

$$M_{\text{grav}} = 5.9724(3) \times 10^{24} \text{ kg}$$

# EARTH'S CORE MASS



First measurement of the Earth's core mass using the weak force!

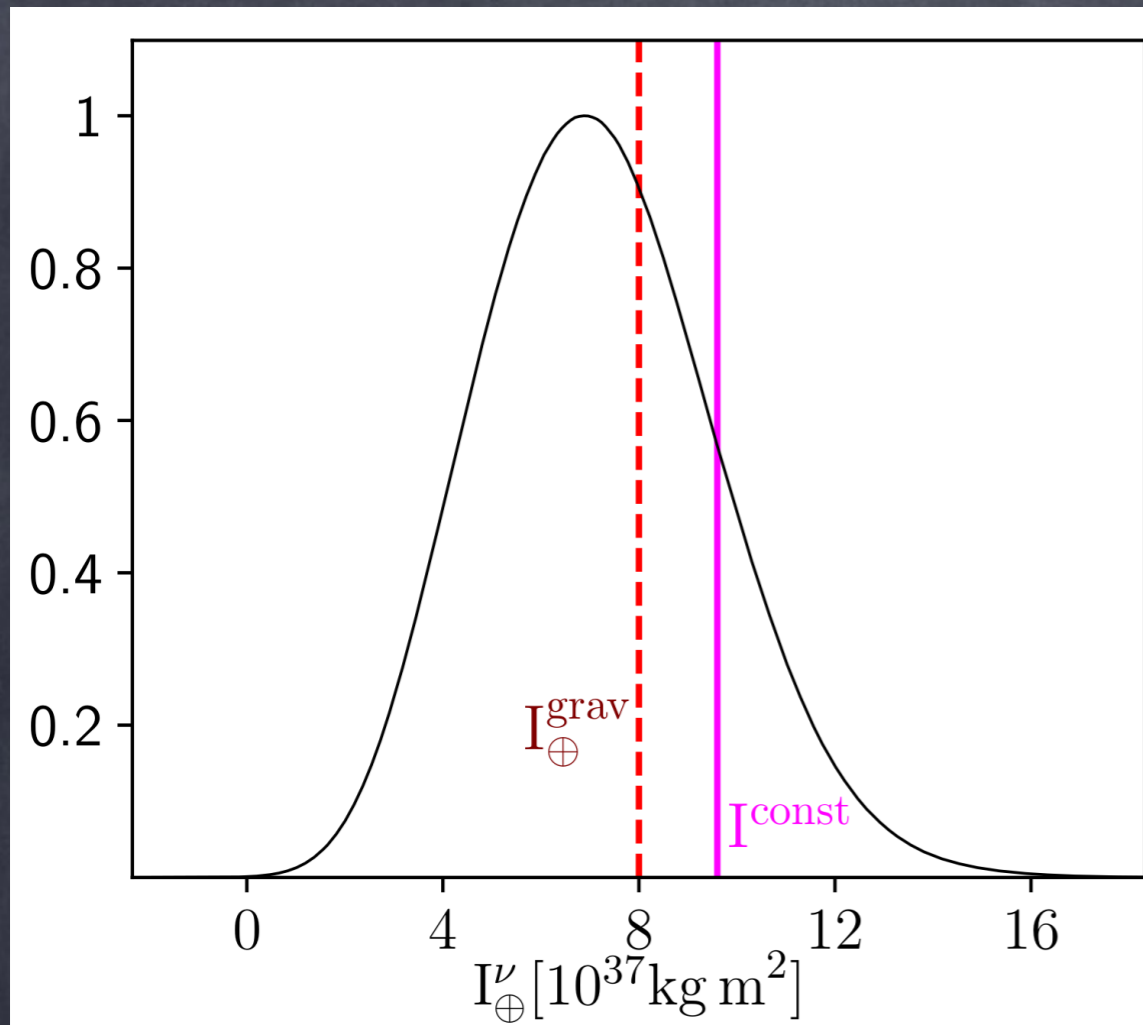
$$M_{\text{core-}\nu} = \left( 2.7^{+1.0}_{-0.9} \right) \times 10^{24} \text{ kg}$$

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

$$\frac{M_{\text{core-}\nu}}{M_{\nu}} = 0.45^{+0.21}_{-0.18}$$



# EARTH'S MOMENT OF INERTIA



First measurement of the Earth's moment of inertia using the weak force!

$$I_\nu = (6.9 \pm 2.4) \times 10^{37} \text{ kg m}^2$$

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

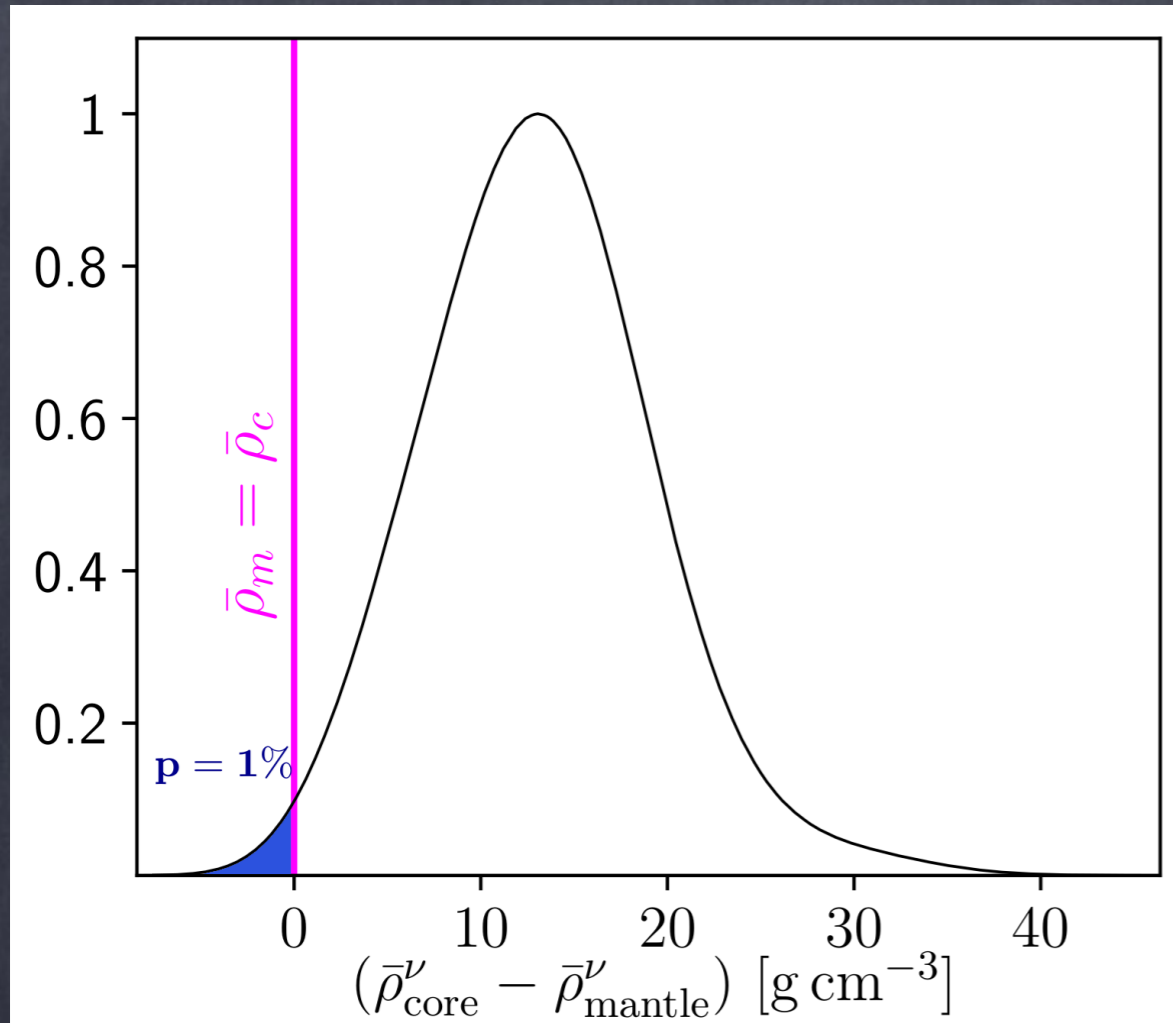
$$\frac{I_\nu}{I_{\text{sphere-}\nu}} = 0.7 \pm 0.3$$

Gravitational measurement

$$\frac{I_{\text{grav}}}{I_{\text{sphere}}} = 0.82681(11)$$

$$I_{\text{grav}} = 8.01736(96) \times 10^{37} \text{ kg m}^2$$

# CORE DENSER THAN MANTLE



First measurement of the Earth's core-mantle discontinuity using the weak force!

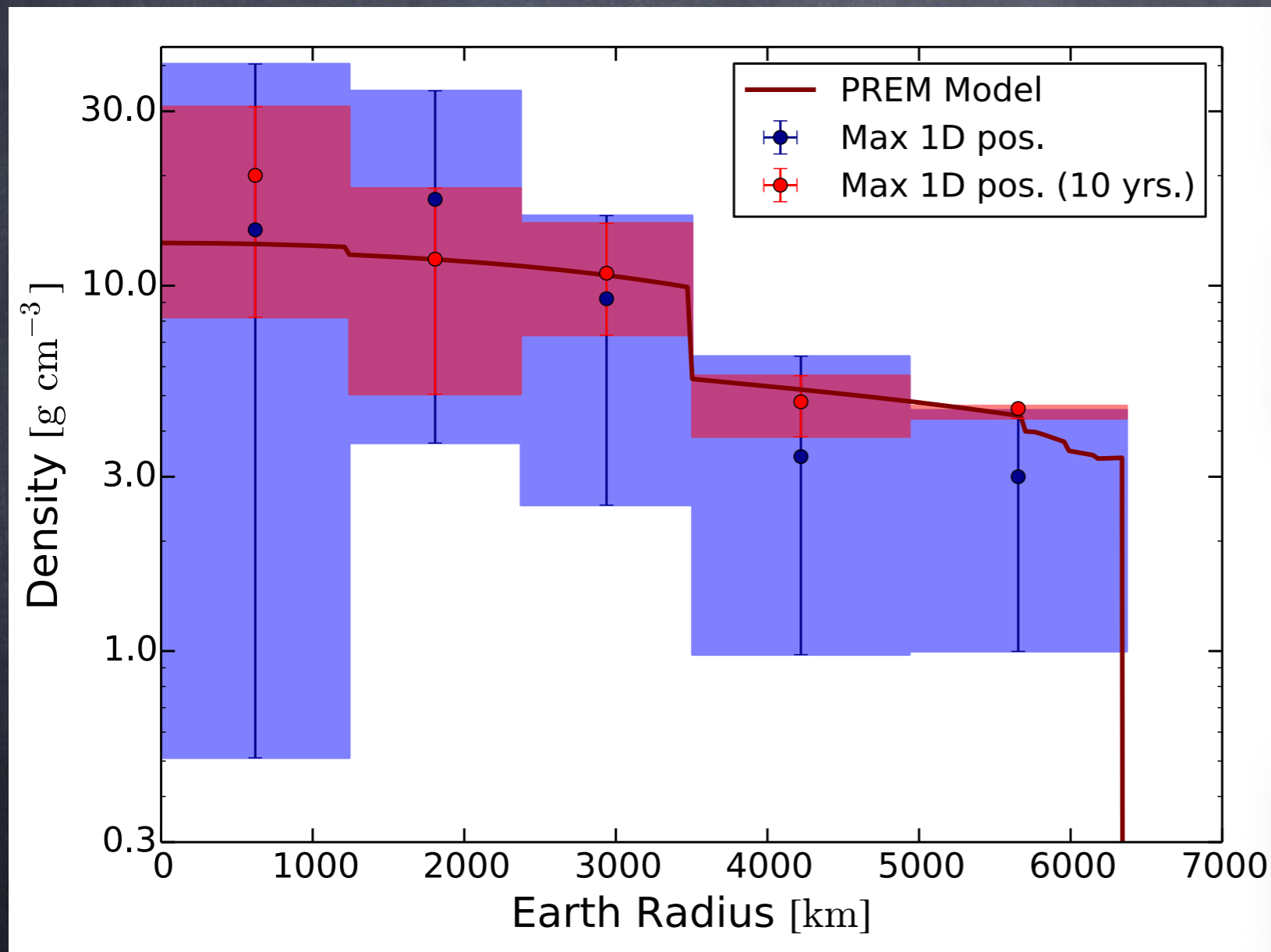
$$\left( \bar{\rho}_{core}^{\nu} - \bar{\rho}_{mantle}^{\nu} \right) = \left( 13.1^{+5.8}_{-6.3} \right) g / cm^3$$

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

A denser mantle has a p-value of  $p=0.011$

# WHAT ABOUT THE FUTURE? ... ACTUALLY PRESENT

Forecast for 10 years of data



Few per cent error in  
the mantle

A finer modeling can  
be considered

Test of  
discontinuities

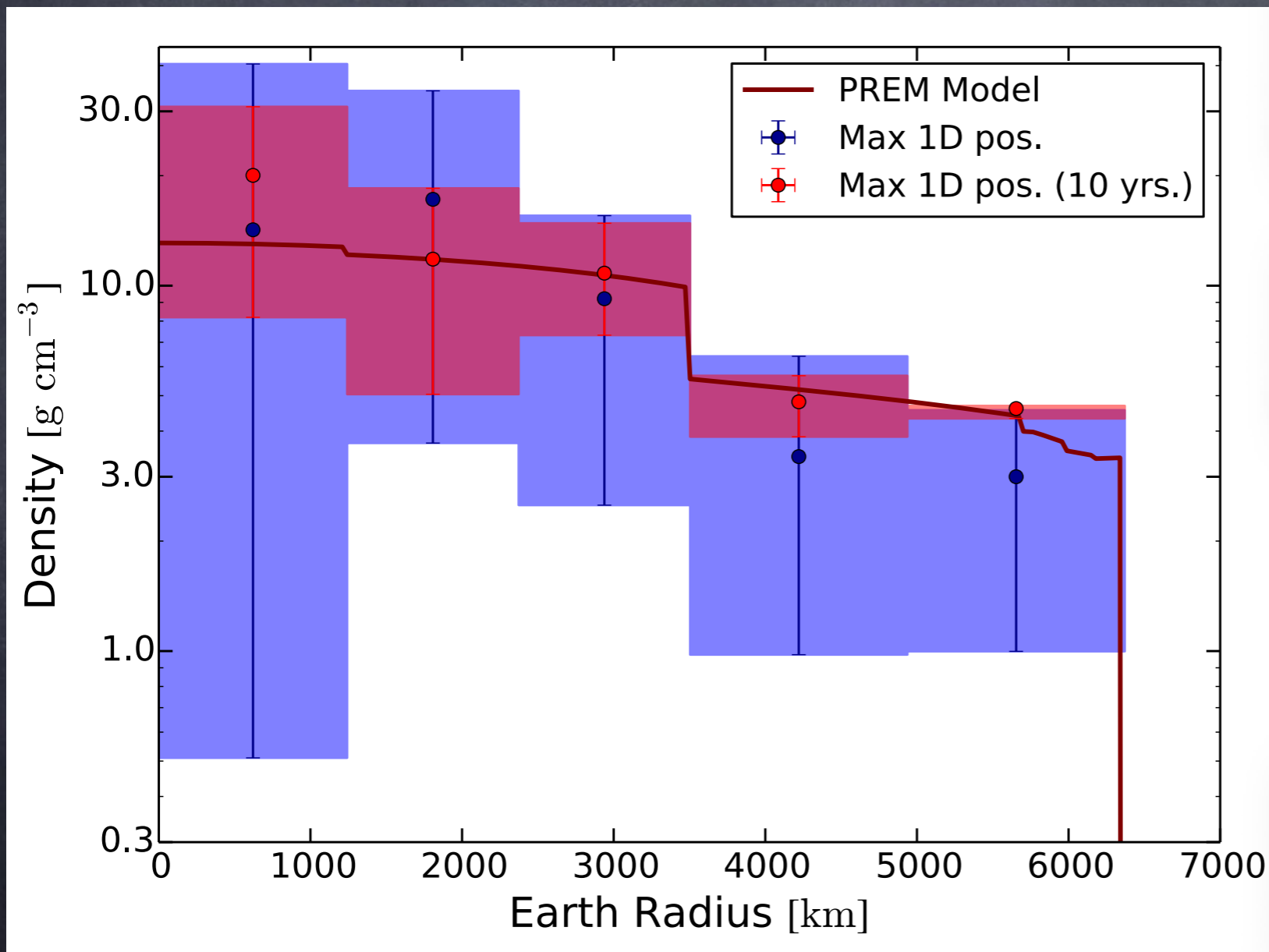
Knowledge of hadronic-  
interaction model  
impacts systematics

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

# WHAT ABOUT THE FUTURE? ... ACTUALLY PRESENT

Forecast for 10 years of data

... but at least already 8 years of actual data!



Few per cent error in  
the mantle

A finer modeling can  
be considered

Test of  
discontinuities

Knowledge of hadronic-  
interaction model  
impacts systematics

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

# CONCLUSIONS

After 44 years of being proposed, we have performed the **first Earth (absorption) tomography with neutrinos**

First measurement of the **Earth's mass** and **moment of inertia** using only the **weak force!**

Although still not precise, it might become a technique **complementary** to seismic wave studies

**Analysis** with **1 year** of data

**8 years** of data already **collected** by IceCube

... and other future experiments: KM3NeT, Baikal-GVD

Highlight talk at  
**EGU** General Assembly 2019  
Vienna | Austria | 7-12 April 2019

Edmund Halley,

Philosophical Transactions of the Royal Society of London XVII:195, 563 (1692):

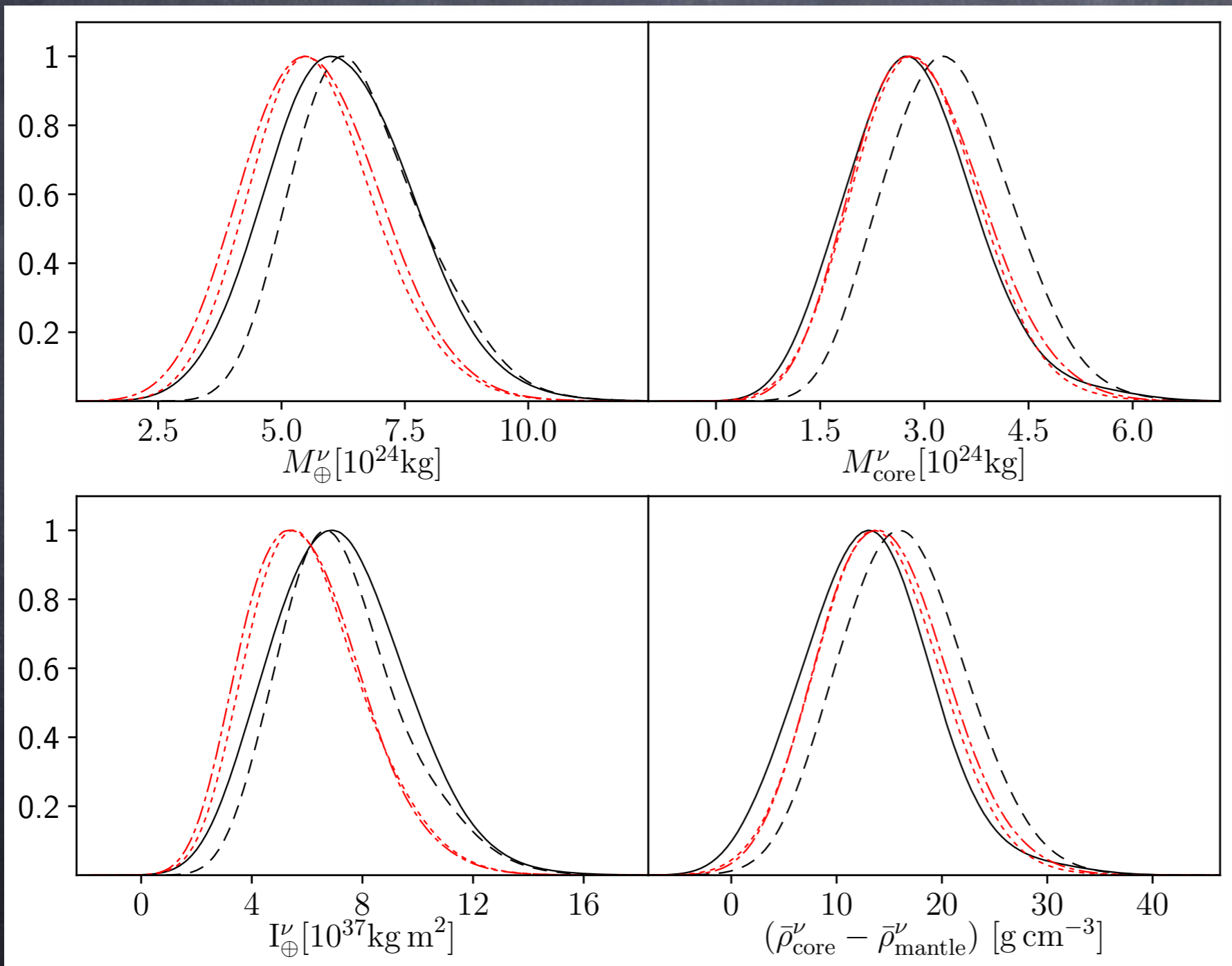
“what curiosity in the structure, what accuracy in the mixture and composition of the parts, ought not we to expect in the fabrick of this globe”

Thanks!

# IMPACT OF DISCRETE SYSTEMATICS

## Different atmospheric neutrino fluxes

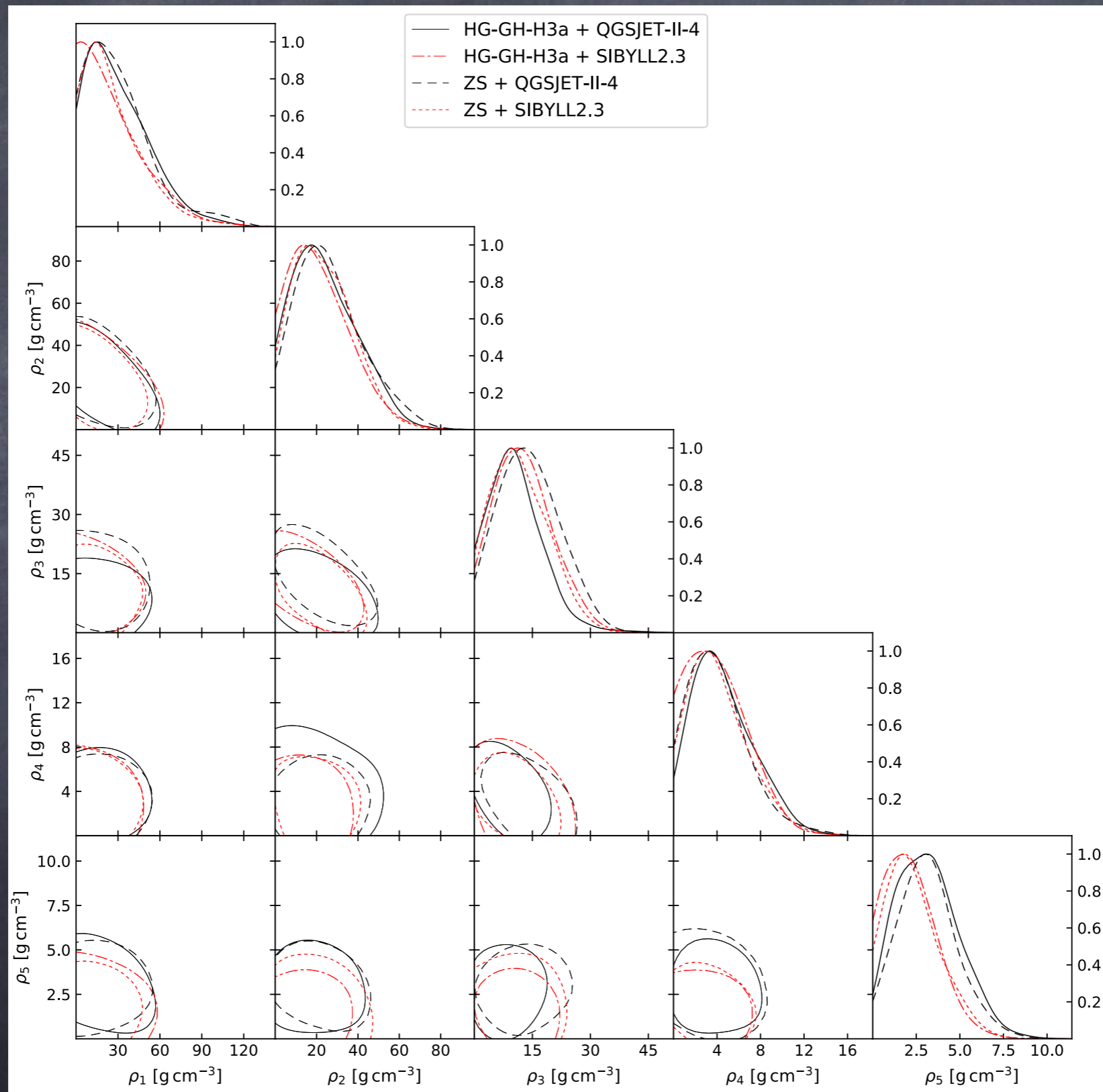
- HG-GH-H3a + QGSJET-II-4
- - - HG-GH-H3a + SIBYLL2.3
- - - ZS + QGSJET-II-4
- - - ZS + SIBYLL2.3



systematics  
 (mainly driven by the  
 hadronic-interaction  
 modeling)  
 ~ (20-30) %

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

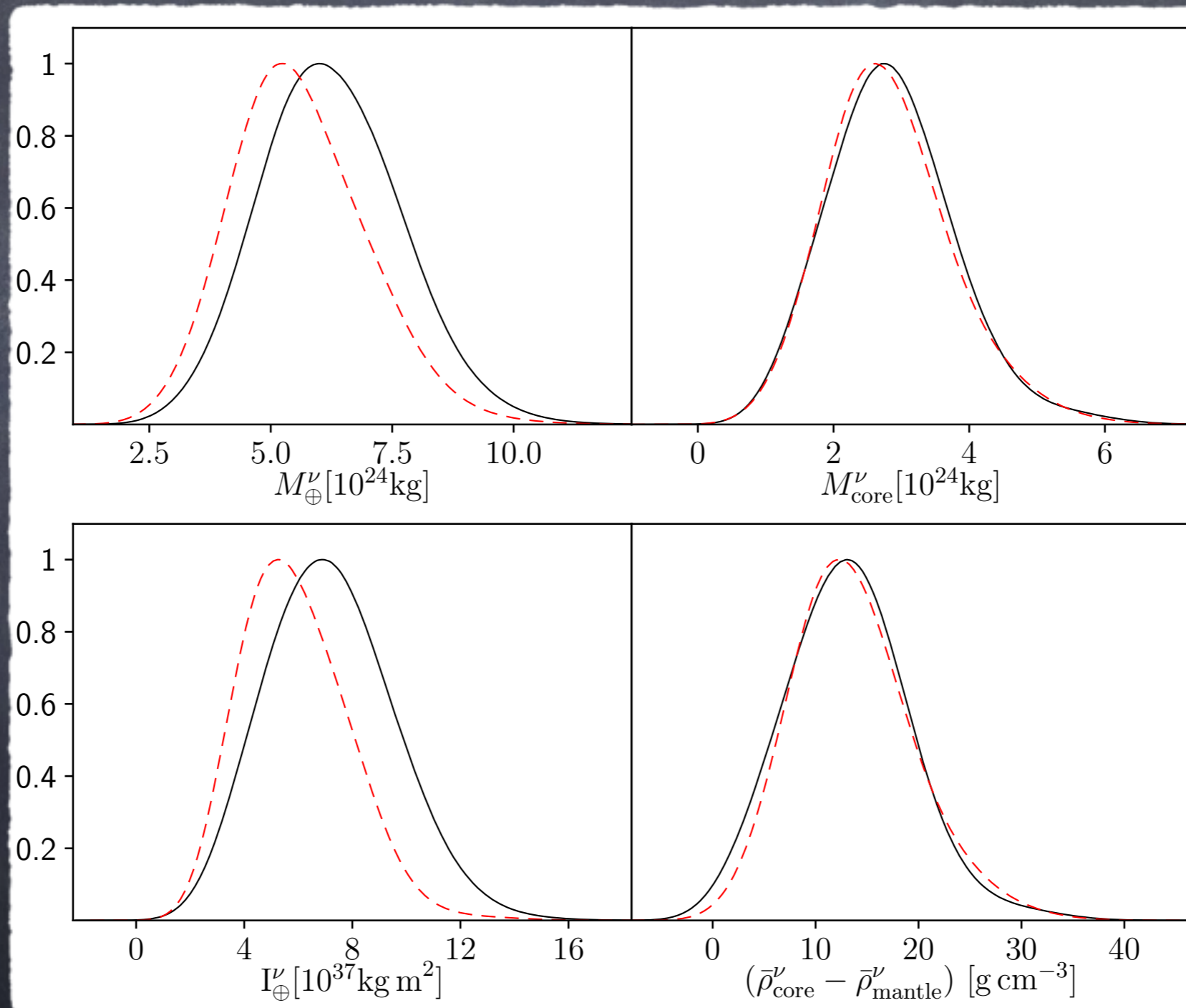
# NEUTRINO FLUXES: CORRELATIONS





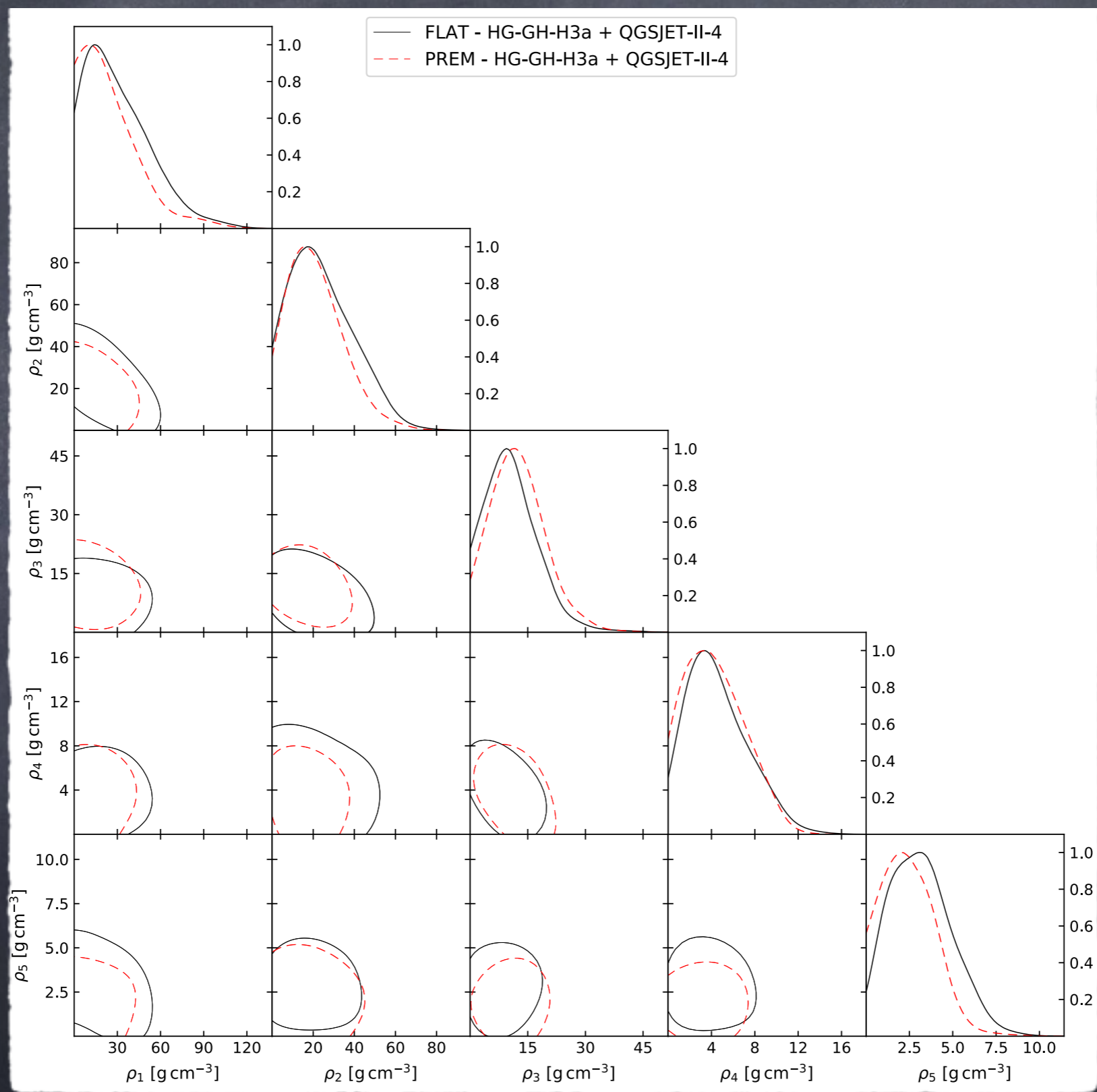
# IMPACT OF DENSITY PROFILE

— FLAT - HG-GH-H3a + QGSJET-II-4  
- - - PREM - HG-GH-H3a + QGSJET-II-4



A. Donini, SPR and J. Salvado, *Nature Physics* 15:37, 2019

# IMPACT OF DENSITY PROFILE: CORRELATIONS

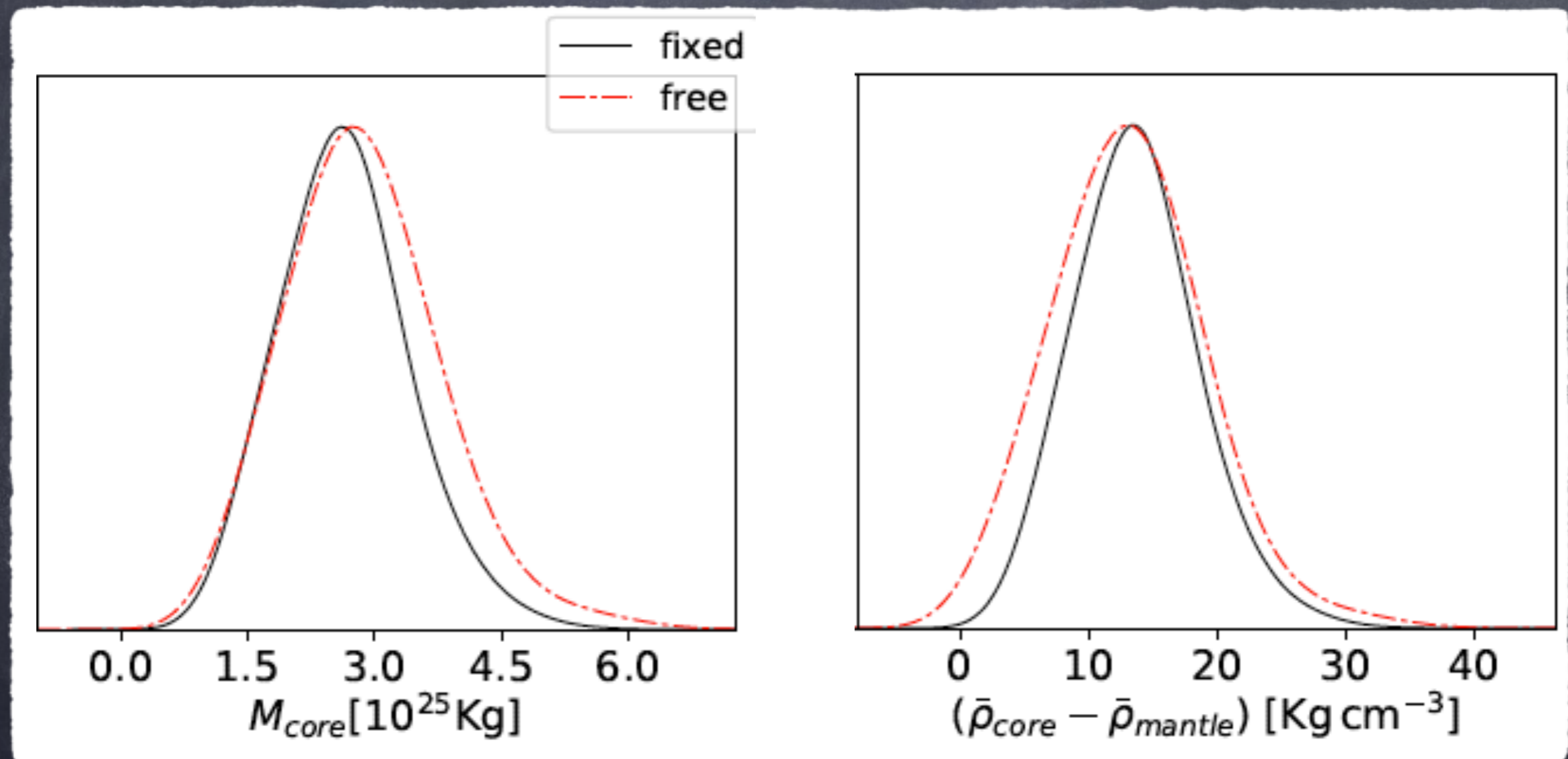


# IMPACT OF SYSTEMATICS

	Piecewise flat Earth's profile				PREM Earth's profile
	HG-GH-H3a + QGSJET-II-04	HG-GH-H3a + SIBYLL2.3	ZS + QGSJET-II-04	ZS + SIBYLL2.3	HG-GH-H3a + QGSJET-II-04
$M_{\oplus}^{\nu}$ [ $10^{24}$ kg]	$6.0^{+1.6}_{-1.3}$	$5.5^{+1.5}_{-1.3}$	$6.2^{+1.4}_{-1.2}$	$5.5^{+1.3}_{-1.2}$	$5.3^{+1.5}_{-1.3}$
$M_{\text{core}}^{\nu}$ [ $10^{24}$ kg]	$2.72^{+0.97}_{-0.89}$	$2.79^{+0.98}_{-0.85}$	$3.27^{+0.92}_{-0.89}$	$2.84^{+0.89}_{-0.88}$	$2.62^{+0.97}_{-0.84}$
$I_{\oplus}^{\nu}$ [ $10^{37}$ kg cm <sup>2</sup> ]	$6.9 \pm 2.4$	$5.4^{+2.3}_{-1.9}$	$6.7^{+2.3}_{-2.0}$	$5.5^{+2.2}_{-1.9}$	$5.3^{+2.3}_{-1.7}$
$\bar{\rho}_{\text{core}}^{\nu} - \bar{\rho}_{\text{mantle}}^{\nu}$ [g/cm <sup>3</sup> ]	$13.1^{+5.8}_{-6.3}$	$14.0^{+6.0}_{-5.9}$	$15.9^{+6.0}_{-5.9}$	$13.5^{+6.1}_{-5.5}$	$12.3^{+6.3}_{-5.4}$
$p$ – value mantle denser than core	$1.1 \times 10^{-2}$	$2.4 \times 10^{-3}$	$9.4 \times 10^{-4}$	$4.6 \times 10^{-3}$	$3.8 \times 10^{-3}$

A. Donini, SPR and J. Salvado, Nature Physics 15:37, 2019

# ADDING GRAVITY CONSTRAINTS



Density of the mantle determined at  $\sim 4\%$