

The SMEFT and its precision future

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ATLAS Exotics Searches* - 95% CL Upper Exclusion Limits

Status: May 2020

$$\int dt \mathcal{L} = (3.2 - 139) \text{ fb}^{-1}$$

$$\sqrt{s} = 8, 13 \text{ TeV}$$

Model	ℓ, γ	Jets [†]	E_{T}^{miss}	$[\mathcal{L} dt [\text{fb}^{-1}]$	Limit	Reference	
Extra dimensions	ADD $G_{KK} + \delta/\eta$	$0, e, \mu$	1-4]	Yes	36.1	M_{KK} 7.7 TeV	$n=2$ 1711.03301
	ADD non-resonant $\gamma\gamma$	$2, \gamma$	-	-	36.7	M_{KK} 8.5 TeV	$n=3$ HLZ MLO 1707.04147
	ADD QBH	-	2]	-	37.0	M_{KK} 8.9 TeV	$n=6$ 1703.09127
	ADD BH High Σp_T	$\geq 1, e, \mu$	$\geq 2]$	-	3.2	M_{KK} 8.2 TeV	$n=6, M_{Pl} = 3 \text{ TeV}$, mt BH 1606.02255
	ADD BH multijet	-	$\geq 3]$	-	3.6	M_{KK} 9.55 TeV	1512.25816
	RS1 $G_{KK} \rightarrow \gamma\gamma$	$2, \gamma$	-	-	36.7	G_{KK} mass 4.1 TeV	$k/M_{Pl} = 0.1$ 1707.04147
	Bulk RS $G_{KK} \rightarrow WW/\gamma\gamma$	multi-channel	-	-	-	G_{KK} mass 2.3 TeV	$k/M_{Pl} = 1.0$ 1604.02300
	Bulk RS $G_{KK} \rightarrow WW/\nu\tau$	$1, e, \mu$	2]/1 J	Yes	139	G_{KK} mass 2.0 TeV	$k/M_{Pl} = 1.0$ 2004.14636
	Bulk RS $G_{KK} \rightarrow \tau\tau$	$1, e, \mu$	$\geq 1, b, \geq 2 J$	Yes	36.1	G_{KK} mass 3.8 TeV	$\Gamma/m = 15\%$ 1804.10823
	2UED / RPP	$1, e, \mu$	$\geq 2, b, \geq 3 J$	Yes	36.1	KR mass 1.8 TeV	Ther (1,1), $\mathcal{R}(A^{(1,1)} \rightarrow \tau\tau) = 1$ 1803.09678
Gauge bosons	SSM $Z' \rightarrow \ell\ell$	$2, e, \mu$	-	-	139	Z' mass 5.1 TeV	1903.06248
	SSM $Z' \rightarrow \tau\tau$	$2, \tau$	-	-	36.1	Z' mass 2.42 TeV	1709.07242
	Leptophobic $Z' \rightarrow b\bar{b}$	-	$2, b$	-	36.3	Z' mass 2.1 TeV	1605.06909
	Leptophobic $Z' \rightarrow \tau\tau$	$0, e, \mu$	$\geq 1, b, \geq 2 J$	Yes	139	Z' mass 4.1 TeV	$\Gamma/m = 1.2\%$ 2005.05138
	SSM $W' \rightarrow \ell\nu$	$1, e, \mu$	-	-	139	W' mass 6.0 TeV	1906.05609
	SSM $W' \rightarrow \tau\nu$	$1, \tau$	-	-	36.1	W' mass 3.7 TeV	1801.06892
	HVT $W' \rightarrow WZ \rightarrow f\nu q\bar{q}$ model B	$1, e, \mu$	2]/1 J	Yes	139	W' mass 4.3 TeV	$g_V = 3$ 2004.14636
	HVT $W' \rightarrow W\nu \rightarrow \nu q\bar{q}$ model B	$0, e, \mu$	2 J	-	139	W' mass 3.8 TeV	1903.05589
	HVT $W' \rightarrow WH/ZH$ model B	multi-channel	-	-	36.1	W' mass 2.93 TeV	$g_V = 3$ 1712.06518
	HVT $W' \rightarrow WH$ model B	$0, e, \mu$	$\geq 1, b, \geq 2 J$	Yes	139	W' mass 3.2 TeV	$g_V = 3$ CERN-EP-2020-073
LRSM $W_R \rightarrow t\bar{b}$	multi-channel	-	-	36.1	W_R mass 3.25 TeV	1807.10473	
LRSM $W_R \rightarrow \mu N_k$	$2, \mu$	1 J	-	80	W_R mass 5.0 TeV	$m(N_k) = 0.5 \text{ TeV}$, $g_L = g_R$ 1904.12679	
CI	CI $\phi\phi\phi$	-	2]	-	37.0	A 21.8 TeV $\eta_{(1)}$	1703.09127
	CI $\ell f\phi q$	$2, e, \mu$	-	-	139	A 35.8 TeV $\eta_{(1)}$	CERN-EP-2020-068
CI $\ell r\tau\tau$	$\geq 1, e, \mu$	$\geq 1, b, \geq 1 J$	Yes	36.1	A 2.57 TeV	$ C_{\ell\tau} = 4\epsilon$ 1811.03301	
DM	Axial-vector mediator (Dirac DM)	$0, e, \mu$	1-4]	Yes	36.1	m_{med} 1.55 TeV	$g_V = 0.25, g_A = 1.0, m(\chi) = 1 \text{ GeV}$
	Colored scalar mediator (Dirac DM)	$0, e, \mu$	1-4]	Yes	36.1	m_{med} 1.67 TeV	$g_V = 0.2, m(\chi) = 1 \text{ GeV}$
	$VV_{1,2}$ EFT (Dirac DM)	$0, e, \mu$	1, $b, \leq 1 J$	Yes	3.2	M_{pl} 700 GeV	$m(\chi) = 150 \text{ GeV}$
	Scalar resonant, $\phi \rightarrow \tau\tau$ (Dirac DM)	$0-1, e, \mu$	1, $b, 0-1 J$	Yes	36.1	m_ϕ 3.4 TeV	$\eta = 0.4, \lambda = 0.2, m(\chi) = 10 \text{ GeV}$ 1812.09743
LQ	Scalar LQ 1 st gen	$1, 2, e$	$\geq 2]$	Yes	36.1	LQ mass 1.4 TeV	$\beta = 1$ 1902.00377
	Scalar LQ 2 nd gen	$1, 2, \mu$	$\geq 2]$	Yes	36.1	LQ mass 1.56 TeV	$\beta = 1$ 1902.00377
	Scalar LQ 3 rd gen	$2, \tau$	$2, b$	-	36.1	LQ ₃ mass 1.03 TeV	$\mathcal{R}(LQ_3 \rightarrow b\tau) = 1$ 1902.08103
	Scalar LQ 3 rd gen	$0-1, e, \mu$	$2, b$	Yes	36.1	LQ ₃ mass 970 GeV	$\mathcal{R}(LQ_3 \rightarrow \tau\tau) = 0$ 1902.08103
Heavy quarks	$VLQ \ T\bar{T} \rightarrow Ht/Zt/Wb + X$	multi-channel	-	-	36.1	T mass 1.37 TeV	SU(2) doublet 1808.02343
	$VLQ \ B\bar{B} \rightarrow Wt/Zb + X$	multi-channel	-	-	36.1	B mass 1.34 TeV	SU(2) doublet 1808.02343
	$VLQ \ T_{3,1} T_{3,2} / T_{3,1} T_{3,3} \rightarrow Wt + X$	$2SS/2S \rightarrow e\bar{e}$	$\geq 1, b, \geq 1 J$	Yes	36.1	$T_{3,1}$ mass 1.64 TeV	$\mathcal{R}(T_{3,1} \rightarrow Wt) = 1, c_{\ell}(T_{3,1} H\bar{t}) = 1$
	$VLQ \ Y \rightarrow Wb + X$	$1, e, \mu$	$\geq 1, b, \geq 1 J$	Yes	79.8	Y mass 1.85 TeV	$\mathcal{R}(Y \rightarrow Wb) = 1, c_{\ell}(YH\bar{t}) = 1$
	$VLQ \ B \rightarrow Hb + X$	$0, e, \mu, 2, \gamma$	$\geq 1, b, \geq 1 J$	Yes	79.8	B mass 1.21 TeV	$\epsilon = 0.5$ ATLAS-COBF-2018-024
$VLQ \ QQ \rightarrow Wt/Wb$	$1, e, \mu$	$\geq 4 J$	Yes	20.3	Q mass 690 GeV	1509.04251	
Excited fermions	Excited quark $q^* \rightarrow q\bar{q}$	-	2]	-	139	q^* mass 6.7 TeV	only u' and d' , $A = m(q')$ 1910.08847
	Excited quark $q^* \rightarrow q\gamma$	$1, \gamma$	1]	-	36.7	q^* mass 5.3 TeV	only u' and d' , $A = m(q')$ 1709.10440
	Excited quark $b^* \rightarrow b\bar{g}$	-	1, $b, 1 J$	-	36.1	b^* mass 2.6 TeV	1805.09299
	Excited lepton ℓ^*	$3, e, \mu$	-	-	20.3	ℓ^* mass 3.6 TeV	1811.03301
	Excited lepton ν^*	$3, e, \mu, \tau$	-	-	20.3	ν^* mass 1.6 TeV	$A = 3.0 \text{ TeV}$ $A = 1.6 \text{ TeV}$ 1411.29291 1411.2921
Other	Type III Seesaw	$1, e, \mu$	$\geq 2]$	Yes	79.8	N^c mass 560 GeV	$m(W_2) = 4.1 \text{ TeV}$, $g_L = g_V$ ATLAS-COBF-2018-020
	LRSM Majorana ν	$2, \mu$	2]	-	36.1	N_2 mass 3.2 TeV	1509.11105
	Higgs triplet $H^{1,2} \rightarrow \ell\ell$	$2, 3, 4, e, \mu$ (SS)	-	-	36.1	$H^{1,2}$ mass 870 GeV	DY production 1710.09748
	Higgs triplet $H^{1,2} \rightarrow \ell\tau$	$3, e, \mu, \tau$	-	-	20.3	$H^{1,2}$ mass 400 GeV	DY production, $\mathcal{R}(H^{1,2} \rightarrow \ell\tau) = 1$ 1411.2921
	Multi-charged particles	-	-	-	36.1	multi-charged particle mass 1.22 TeV	DY production, $ q = 5e$ 1812.03673
	Magnetic monopoles	-	-	-	34.4	monopole mass 2.37 TeV	DY production, $ q = 1/g, \text{spin } 1/2$ 1905.10130

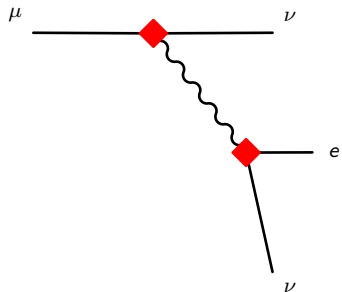
*Only a selection of the available mass limits on new states or phenomena is shown.

† Small-radius (large-radius) jets are denoted by the letter j (J).



What's an EFT?

In the SM

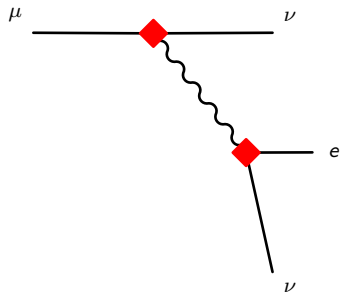


$$\mathcal{M} \sim \frac{g_W^2}{2} \frac{(\bar{\nu}_\mu \gamma^\mu P_L \mu)(\bar{e} \gamma^\mu P_L \nu_e)}{k^2 - M_W^2}$$



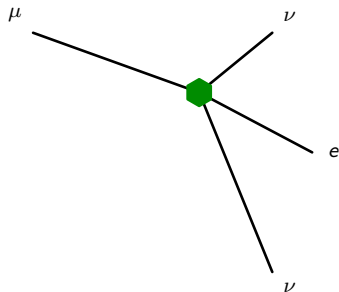
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In the Fermi theory



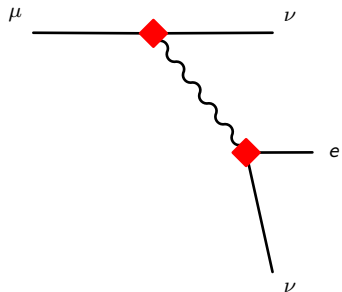
$$\frac{1}{M_W^2} (\bar{\psi} \gamma^\mu P_L \psi)^2$$

$$\mathcal{M} \sim -\frac{g_W^2}{2M_W^2} (\bar{\nu}_\mu \gamma^\mu P_L \mu)(\bar{e} \gamma^\mu P_L \nu_e) + \dots$$



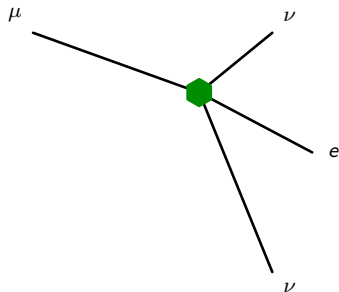
What's an EFT?

In the SM



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In the Fermi theory



$$\frac{1}{M_W^2} (\bar{\psi} \gamma^\mu P_L \psi)^2$$

$$\frac{1}{M_W^4} \partial^2 (\bar{\psi} \gamma^\mu P_L \psi)^2$$

$$\mathcal{M} \sim -\frac{g_W^2}{2M_W^2} (\bar{\nu}_\mu \gamma^\mu P_L \mu)(\bar{e} \gamma^\mu P_L \nu_e) - \frac{g_W^2 k^2}{2M_W^4} (\bar{\nu}_\mu \gamma^\mu P_L \mu)(\bar{e} \gamma^\mu P_L \nu_e) + \dots$$



SMEFT: Effective Vertices (taking $H \rightarrow v + h$)

$$T3: Q_{H\Box} = (H^\dagger H)\Box(H^\dagger H)$$



$$T3: Q_{HD} = (H^\dagger D^\mu H)^*(H^\dagger D^\mu H)$$



$$T4: Q_{HV} = (H^\dagger H)V^{\mu\nu}V_{\mu\nu}$$



$$T4: Q_{HWB} = (H^\dagger \tau^I H)W_{\mu\nu}^I B^{\mu\nu}$$



$$T5: Q_{\psi H} = (H^\dagger H)(\bar{\Psi}H\psi)$$



$$T7: Q_{HL}^{(3)} = (H^\dagger i\bar{D}_\mu^I H)(\bar{L}\gamma^\mu L)$$



$$T7: Q_{H\Psi}^{(1,3)} = (H^\dagger \bar{D}_\mu H)(\bar{\Psi}\gamma^\mu \Psi)$$



$$T7: Q_{H\psi} = (H^\dagger \bar{D}_\mu H)(\bar{\psi}\gamma^\mu \psi)$$

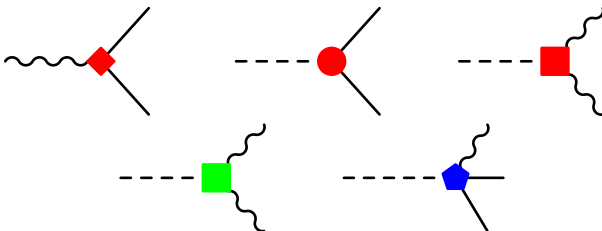


$$T8: Q_{LL} = (\bar{L}\gamma^\mu L)(\bar{L}\gamma^\mu L)$$

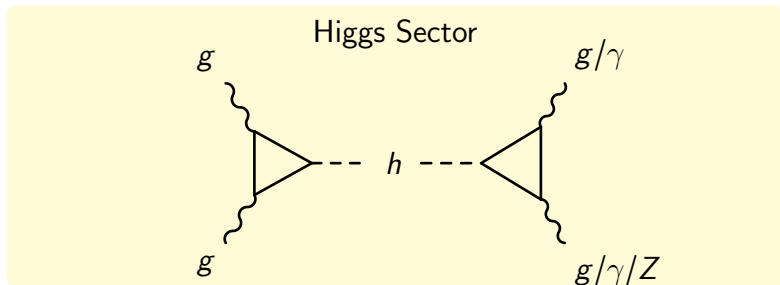


◆ ● ■ SM-like

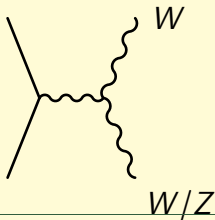
■ ◆ Non-SM-like kinematic structure



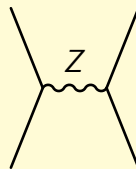
Global fits of the SMEFT



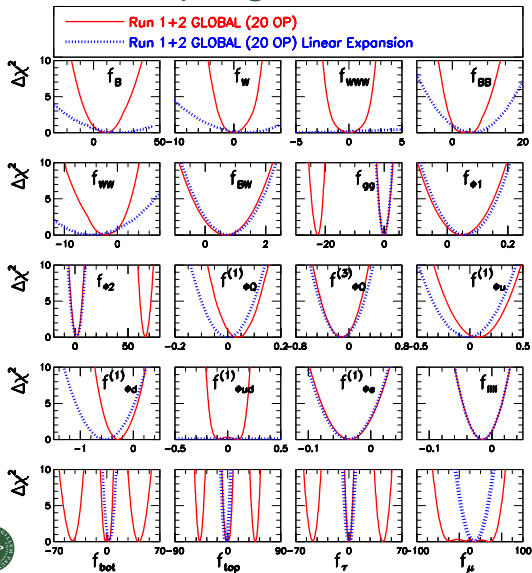
Triple Gauge Sector



Electroweak Precision Data



An example global fit



Almeida et al. 1812.01009

- ⊖ Dbl insertions of c_i in red, single in blue
- ⊖ Blind direction broken by TGC+EWPD
- ⊖ Many cases where constraints lost
- ⊖ Current status:
testing how well we can measure 0



Long term goals for the SMEFT

- ① Do these global fits
- ② Improve theory predictions, [understand theory errors](#)
- ③ Measure a deviation
 - correlations between operators reveal nature of NP
 - scale at which unitarity is violated gives scale of NP (i.e. as π scattering predicts $\rho \sim 1$ GeV)

Extremely important for FCC-ee as a precision machine

Still important for FCC-hh for physics on a (SM) pole



SMEFT Loops (short version)

Many different groups doing loops in the SMEFT

Some of the calculations done include:

- $H\gamma\gamma$ (see e.g. 1507.03568)
- EWPD (arXiv:1909.02000)
- $pp \rightarrow WW, WZ, HZ, HW$ (QCD only, see e.g. arXiv:2003.07862)

Automated QCD loops in Madgraph w/ SMEFT@NLO (2008.11743)

Background field method for analytic loops (e.g. TC arXiv:2010.15852)

Loops give us a hold on theory errors!



tt production at one loop in SMEFT@NLO

SM: $744^{+12\%}_{-12\%}$ pb

$(\bar{\psi}\psi)^2$	$\mathcal{O}(\frac{1}{\Lambda^2} = \frac{1}{\text{TeV}^2})$		$\mathcal{O}(\frac{1}{\Lambda^4} = \frac{1}{\text{TeV}^4})$	
	tree	loop	tree	loop
$(\bar{t}_R\gamma^\mu u_R)(\bar{u}_R\gamma_\mu t_R)$	$.67^{+1\%}_{-1\%}$ pb	$.41^{+13\%}_{-17\%}$ pb	$4.66^{+6\%}_{-5\%}$ pb	$5.92^{+6\%}_{-5\%}$ pb
$(\bar{t}_R\gamma^\mu d_R)(\bar{d}_R\gamma_\mu t_R)$	$-.21^{+1\%}_{-1\%}$ pb	$-.306^{+30\%}_{-22\%}$ pb	$2.62^{+6\%}_{-5\%}$ pb	$3.46^{+5\%}_{-5\%}$ pb
$(\bar{Q}_3\gamma^\mu q_i)(\bar{q}_i\gamma_\mu Q_3)$	$1.92^{+0\%}_{-1\%}$ pb	$1.05^{+17\%}_{-22\%}$ pb	$7.25^{+6\%}_{-5\%}$ pb	$9.32^{+5\%}_{-5\%}$ pb

- ① Tree level result for $\frac{1}{\Lambda^2} \Rightarrow$ error in SM which is consistent w SMEFT



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- 1 Tree level result for $\frac{1}{\Lambda^2} \Rightarrow$ error in SM which is consistent w SMEFT
- 2 Loop result for $\frac{1}{\Lambda^2} \Rightarrow$ error in tree $\frac{1}{\Lambda^2}$, $\mathcal{O}(60 - 146\%)$



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- 1 Tree level result for $\frac{1}{\Lambda^2} \Rightarrow$ error in SM which is consistent w SMEFT
- 2 Loop result for $\frac{1}{\Lambda^2} \Rightarrow$ error in tree $\frac{1}{\Lambda^2}$, $\mathcal{O}(60 - 146\%)$
- 3 Tree level result for $\frac{1}{\Lambda^4} \Rightarrow$ error in tree $\mathcal{O}(300 - 1200\%)???$

$$|\mathcal{M}|^2 \equiv |\mathcal{M}_{\text{SM}} + \frac{1}{\Lambda^2} \mathcal{M}_6|^2$$



NLO SMEFT

The consistent squared amplitude to $\mathcal{O}\left(\frac{1}{\Lambda^4}\right)$:

$$|\mathcal{M}|^2 = |\mathcal{M}_{\text{SM}}|^2 + \frac{2}{\Lambda^2} \text{Re}[\mathcal{M}_{\text{SM}}\mathcal{M}_6] + \frac{1}{\Lambda^4} (|\mathcal{M}_6|^2 + 2\text{Re}[\mathcal{M}_{6^2}\mathcal{M}_{\text{SM}} + \mathcal{M}_8\mathcal{M}_{\text{SM}}])$$



NLO SMEFT

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So SMEFT@NLO is missing $\mathcal{M}_{6^2}\mathcal{M}_{\text{SM}}$ and $\mathcal{M}_8\mathcal{M}_{\text{SM}}$ terms...

- ① \mathcal{M}_{6^2} requires \mathcal{M}_8 for consistency (renormalizability)
- ② \mathcal{M}_8 seems intractible – sooo many parameters, $\mathcal{O}(40k)$



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So SMEFT@NLO is missing $\mathcal{M}_{6^2}\mathcal{M}_{\text{SM}}$ and $\mathcal{M}_8\mathcal{M}_{\text{SM}}$ terms...

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- ② \mathcal{M}_8 seems intractible – sooo many parameters, $\mathcal{O}(40k)$

*without a consistent calculation to $\frac{1}{\Lambda^4}$ we lack understanding of theory errors...
we need a new methodology to tackle this problem*



A taste of geoSMEFT

Consider operators shifting $Z\bar{\psi}\psi$:

$$\sum_{n=0} \frac{c^{(6+2n)}}{\Lambda^{2n+2}} (H^\dagger H)^n (H^\dagger i \overleftrightarrow{D}^\mu H) (\bar{\psi} \gamma_\mu \psi)$$



A taste of geoSMEFT

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Define a **field space connection**

$$L_{J,A}^{pr} = \left. \frac{\delta^2 \mathcal{L}}{\delta(D^\mu \phi)^J \delta(\bar{\psi}_p \gamma_\mu \sigma_A \psi_r)} \right|_{\text{fields} \rightarrow 0} = -(\phi \gamma_4) \delta_{A4} \sum_{n=0}^{\infty} \frac{c_{H\psi,pr}^{1,(6+2n)}}{\Lambda^{2n}} (H^\dagger H)^n + 4 \text{ more}$$



A taste of geoSMEFT

Consider operators shifting $Z\bar{\psi}\psi$:

$$\sum_{n=0} \frac{c^{(6+2n)}}{\Lambda^{2n+2}} (H^\dagger H)^n (H^\dagger i\vec{D}^\mu H) (\bar{\psi}\gamma_\mu\psi)$$

Define a [field space connection](#)

$$L_{J,A}^{pr} = \left. \frac{\delta^2 \mathcal{L}}{\delta(D^\mu\phi)^J \delta(\bar{\psi}_p\gamma_\mu\sigma_A\psi_r)} \right|_{\text{fields} \rightarrow 0} = -(\phi\gamma_4)\delta_{A4} \sum_{n=0}^{\infty} \frac{c_{H\psi,pr}^{1,(6+2n)}}{\Lambda^{2n}} (H^\dagger H)^n + 4 \text{ more}$$

Get an [all orders](#) result:

$$\mathcal{M}_{Z\bar{\psi}\psi}^\mu = \gamma^\mu \frac{\bar{g}_Z}{2} \left[(2s_{\theta_Z}^2 Q_\psi - \sigma_3)\delta_{pr} + \bar{v}_T \langle L_{3,4}^{\psi,pr} \rangle + \sigma_3 \bar{v}_T \langle L_{3,3}^{\psi,pr} \rangle \right]$$

Go calculate [EWPD to all orders](#) (or truncate at $\frac{1}{\Lambda^4}$, TC et al. 2102.02819)



Errors from EWPD to $\frac{1}{\Lambda^4}$

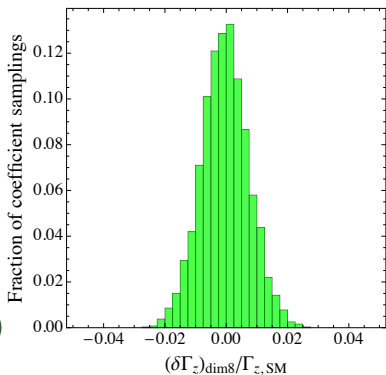
- Perform a χ^2 to EWPD
- include SM two loop results
- include SMEFT results up to $\frac{1}{\Lambda^4}$ including D8 operators
- randomly sample relevant WCs



Errors from EWPD to $\frac{1}{\Lambda^4}$

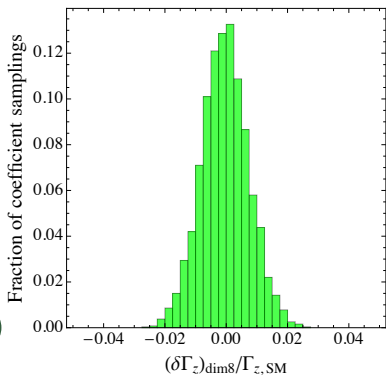
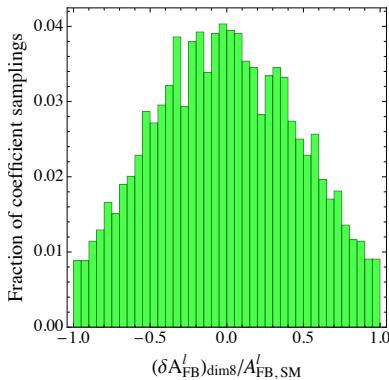
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- randomly sample relevant WCs

Dim-8 EWPD, m_w scheme, $\Lambda = 1$ TeV











Errors from EWPD to $\frac{1}{\Lambda^4}$

- Perform a χ^2 to EWPD
- include SM two loop results
- include SMEFT results up to $\frac{1}{\Lambda^4}$ including D8 operators
- randomly sample relevant WCs

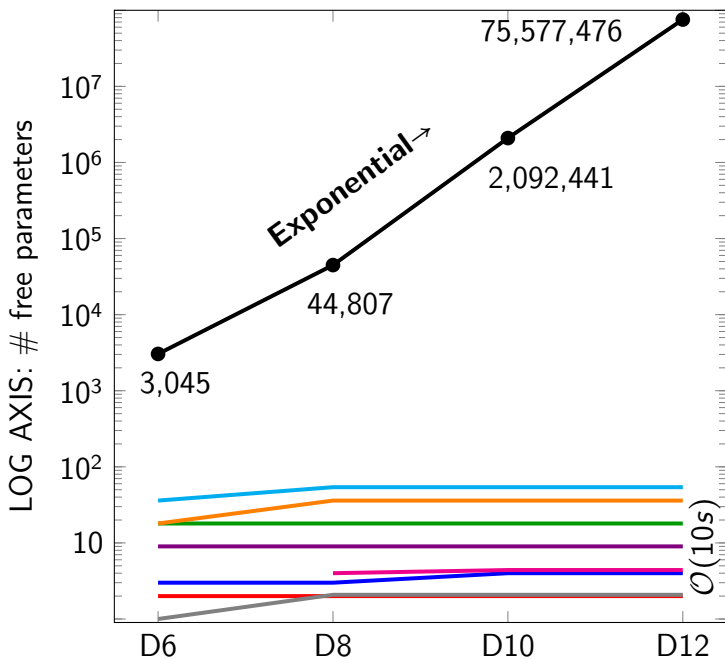
Dim-8 EWPD, m_w scheme, $\Lambda = 1$ TeVDim-8 EWPD, m_w scheme, $\Lambda = 1$ TeV

2- and 3-pt functions known in geoSMEFT

		Mass Dimension				
Operator form:		6	8	10	12	
	$h_{IJ}(D_\mu\phi)^I(D^\mu\phi)^J$	2	2	2	2	masses
	$g_{AB}W_{\mu\nu}^AW^{B,\mu\nu}$	3	4	4	4	couplings, mix. angles
	$k_{IJA}(D^\mu\phi)^I(D^\nu\phi)^JW_{\mu\nu}^A$	0	3	4	4	TGC, HVV
	$f_{ABC}W_{\mu\nu}^AW^{B,\nu\rho}W_\rho^{C,\mu}$	1	2	2	2	QGC, TGC
	$Y_{pr}^\psi\bar{\Psi}_L\psi_R + h.c.$	$2N_f^2$	$2N_f^2$	$2N_f^2$	$2N_f^2$	Yukawa
	$d_A^{\psi,pr}\bar{\Psi}_L\sigma_{\mu\nu}\psi_RW_A^{\mu\nu} + h.c.$	$4N_f^2$	$6N_f^2$	$6N_f^2$	$6N_f^2$	dipoles
	$L_{pr,J,A}^{\psi R}(D^\mu\phi)^J(\bar{\psi}_p,R\gamma_\mu\sigma_A\psi_{r,R})$	N_f^2	N_f^2	N_f^2	N_f^2	$V\bar{\psi}\psi$
	$L_{pr,J,A}^{\psi L}(D^\mu\phi)^J(\bar{\Psi}_p,L\gamma_\mu\sigma_A\Psi_{r,L})$	$2N_f^2$	$4N_f^2$	$4N_f^2$	$4N_f^2$	$V\bar{\psi}\psi$

The number of new free parameters saturates at some point!





Summarizing geoSMEFT

- geoSMEFT rewrite the SMEFT in a **curved field space**
- number of **degrees of freedom saturates** for n -point fxn
- **all orders results** in SMEFT power counting
- better **understanding of error in SMEFT interpretation**
- Further development \Rightarrow **merger loops** + $\frac{1}{\Lambda^4}$



Precision SMEFT for HL-LHC and FCC

SMEFT is the natural choice for the precision frontier:

- quantifies heavy new physics we can't produce
- systematically improvable (loops + $\frac{1}{\Lambda^{2n}}$ expansion)
- indirect evidence \rightarrow information about properties of NP

What's happening for the precision SMEFT:

- loop expansion
- geoSMEFT $\rightarrow \frac{1}{\Lambda^4}$ contributions
- further development will allow for merger of the two

Current efforts in SMEFT should help support and inform design of FCC

FCC-ee will give precision SMEFT results that will help identify NP

FCC-hh can give precision SMEFT result on poles (where $E \ll \Lambda$)

FCC-hh can give access to part of SMEFT not seen at HL-LHC
(e.g. vertices w two Higgs)



The SMEFT at dimension-six

D6 operators from SM field content \Rightarrow SMEFT @ D6



The SMEFT at dimension-six

D6 operators from SM field content \Rightarrow SMEFT @ D6

Type I: X^3		Type II, III: $H^6, H^4 D^2$		Type V: $\Psi^2 H^3 + \text{h.c.}$	
Q_G	$f^{ABC} G_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	Q_H	$(H^\dagger H)^3$	Q_{eH}	$(H^\dagger H)(\bar{L}eH)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{H\Box}$	$(H^\dagger H)\Box(H^\dagger H)$	Q_{uH}	$(H^\dagger H)(\bar{Q}u\tilde{H})$
Q_W	$\epsilon^{IJK} W_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}$	Q_{HD}	$(H^\dagger D^\mu H)^*(H^\dagger D^\mu H)$	Q_{dH}	$(H^\dagger H)(\bar{Q}dH)$
$Q_{\tilde{W}}$	$\epsilon^{IJK} \tilde{W}_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}$				
Type IV: $X^2 \Phi^2$		Type VI: $\Psi^2 H^3$		Type VII: $\Psi^2 H^2 D$	
Q_{HG}	$(H^\dagger H)G_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{L}\sigma^{\mu\nu} e)\tau^I H W_{\mu\nu}^I$	$Q_{HL}^{(1)}$	$(H^\dagger i\bar{D}_\mu H)(\bar{L}\gamma^\mu L)$
$Q_{H\tilde{G}}$	$(H^\dagger H)\tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{L}\sigma^{\mu\nu} e)\tau^I H B_{\mu\nu}$	$Q_{HL}^{(3)}$	$(H^\dagger i\bar{D}_\mu^I H)(\bar{L}\tau^I \gamma^\mu L)$
Q_{HW}	$(H^\dagger H)W_{\mu\nu}^I W^{I\mu\nu}$	Q_{uG}	$(\bar{Q}\sigma^{\mu\nu} T^A u)\tilde{H}G_{\mu\nu}^A$	Q_{He}	$(H^\dagger i\bar{D}_\mu H)(\bar{e}\gamma^\mu e)$
$Q_{H\tilde{W}}$	$(H^\dagger H)\tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	Q_{uW}	$(\bar{Q}\sigma^{\mu\nu} u)\tau^I \tilde{H}W_{\mu\nu}^I$	$Q_{HQ}^{(1)}$	$(H^\dagger i\bar{D}_\mu H)(\bar{q}\gamma^\mu q)$
Q_{HB}	$(H^\dagger H)B_{\mu\nu} B^{\mu\nu}$	Q_{uB}	$(\bar{Q}\sigma^{\mu\nu} u)\tilde{H}B_{\mu\nu}$	$Q_{HQ}^{(3)}$	$(H^\dagger i\bar{D}_\mu^I H)(\bar{q}\tau^I \gamma^\mu q)$
$Q_{H\tilde{B}}$	$(H^\dagger H)\tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{dG}	$(\bar{Q}\sigma^{\mu\nu} T^A d)H G_{\mu\nu}^A$	Q_{Hu}	$(H^\dagger i\bar{D}_\mu H)(\bar{u}\gamma^\mu u)$
Q_{HWB}	$(H^\dagger \tau^I H)W_{\mu\nu}^I B^{\mu\nu}$	Q_{dW}	$(\bar{Q}\sigma^{\mu\nu} d)\tau^I H W_{\mu\nu}^I$	Q_{Hd}	$(H^\dagger i\bar{D}_\mu H)(\bar{d}\gamma^\mu d)$
$Q_{H\tilde{W}B}$	$(H^\dagger \tau^I H)\tilde{W}_{\mu\nu}^I B^{\mu\nu}$	Q_{dB}	$(\bar{Q}\sigma^{\mu\nu} d)\tilde{H}B_{\mu\nu}$	Q_{Hud}	$(H^\dagger i\bar{D}_\mu H)(\bar{u}\gamma^\mu d)$

Type VIII: $5 \times (\bar{L}L)(\bar{L}L) + 7 \times (\bar{R}R)(\bar{R}R) + 8 \times (\bar{L}L)(\bar{R}R) + (\bar{L}R)(\bar{R}L) + 4[(\bar{L}R)(\bar{L}R) + \text{h.c.}] = 25(\bar{\Psi}\Psi)(\bar{\Psi}\Psi)$

